

Sunday evening, June 22, 2008

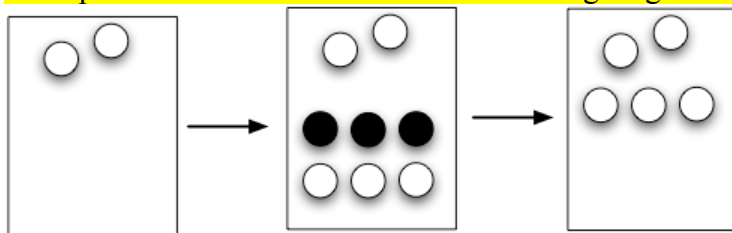
Math 46 class, this is what your final looks like so far. Some of the problems will be extremely similar to problems you've had on exams already!

Take-home essay question, worth 15% of grade – see web site, we discussed this in class. Make sure that EACH sentence contains factual support for your ideas!

- (1) Problem on dividing a circle up into fractional parts. This involves representing fractions as portions of circles, and also involves adding fractions, and is like the Egyptian fraction problems we went over carefully on the last day of class.
Example: use Egyptian fractions to divide 6 pies among 7 people.
- (2) Alternate multiplication methods, like Russian Peasant method, as on the take-home exam.
Example: use Russian Peasant multiplication to multiply 255 by 312.
- (3) Pigeonhole principle problem. Like the one on your first exam, and those we went over in detail on the last day of class.
Example: Given any seven numbers chosen from $\{-32, -16, -8, -4, -2, -1, 1, 2, 4, 8, 16, 32\}$, explain why there will always be
 - (a) A pair with sum 0.
 - (b) A pair with quotient of -1 .
 - (c) A pair with quotient of 2.
 - (d) A pair with product of -32 .
 - (e) A pair whose sum is evenly divisible by 5.
 - (f) In each case above, can you find six numbers that don't exhibit the property?
- (4) Methods for comparing two fractions, without finding a common denominator or converting both to decimals (which is like finding a common denominator!) Like the class activity in which we used "alternative" methods to make the comparisons!
Example: explain which is larger, $8/21$ or $16/45$.
- (5) Pattern problem, like that on exam 1: given a pattern in boxes 0 through 6 or 7, extend the pattern to a different part of the plane.
Example: see exam 1.
- (6) Divisibility tests for 2,3,4,5,6,9,10, and 11. I'll give you a problem involving 2 or 3 of these. Note that if m and n have no factors in common, then a number is divisible by mn only if it passes the divisibility tests for m and n separately. Thus in order to be divisible by 10, a number must be divisible by both 2 and 5 (in other words, end in a 0!) So, for example, what is a divisibility test for 15?
Example: What digit must A be in order for $23232357A5323232$ to be divisible by 9? To be divisible by 11? Is there a digit that makes the number divisible by 198? (Hint $198=2 \times 99$.)
- (7) Some true/false or select the correct answer problems on the history of number systems. If you've read the chapter, you'll be able to find the answers, even if you don't remember them quickly, by quickly finding your way to the answer in the book!
- (8) Changing from base ten to another base or vice versa, as in the take-home test.
Example: Rewrite 1234_5 in base ten. Rewrite 1234_{10} in base six and base two.
- (9) Proportion problem like the calculations you had to do in the Barbie activity, or a calculation involving proportional reasoning.
Example: A six foot tall tree casts a shadow of length $42''$. At the same time a taller tree casts a shadow of length $8\frac{1}{2}$ feet. How tall is the tree, in feet and inches, to the nearest inch?
- (10) Venn diagram problem like the one on your first exam.
Example: see first exam.
- (11) Visual and other explanations for fraction multiplication and division.
Example: give a visual explanation for the common algorithm for multiplying the fractions $4/9$ and $5/7$.

Give an explanation for how to divide $4/9$ by $5/7$ without using “invert and multiply” or use of a calculator.

- (12) Finding the factors, prime factorization, GCD, and LCM of two numbers.
 Example: Find the LCM and GCD of 2700 and 25,200. How many factors does 2700 have?
- (13) Expressing fractions as repeating or terminating decimals; expressing terminating or repeating decimals as fractions.
 Example: Express $7/13$ as a repeating decimal, clearly showing the repeating digits. Express $.207207207\dots = \overline{.207}$ as a fraction in lowest terms.
- (14) Mental arithmetic techniques – be familiar with how to apply several techniques.
 Examples: see the homework under mental arithmetic.
- (15) A simple cryptarithm problem, which requires a written explanation.
 Example: the “cryptarithm” problem in the take-home test, but a simpler version.
- (16) Using manipulatives to do addition and subtraction with positive and negative integers.
 Example: What calculation does the following diagram help teach?



- (17) Making a “Poinset Star” by showing the multiples of a given number on a “mod clock,” as we did when we played names with claps and slaps.
 Example: Like the review problem in the last class.
- (18) An applied problem which requires converting from fractions to percentages, and vice versa.
 Examples: Non-applied problems that are similar might be “What percent does $1/4$ represent?” Or “40% is what fraction of 50%; 40% is what percent of 50%? A decline from $3/4$ of the population to $1/3$ of the population is a decline of what percent of the total population?”
- (19) What are the Fibonacci numbers, how are they constructed, how does the symbolism $F_1=1, F_2=1, F_3=2, F_4=3, F_5=5$, etc., work?
 Example: Give the next row of the following pattern, and complete the general formula for the “even case”:

$(1)(3) = (1)(2) + 1$	$(F_1)(F_4) = (F_2)(F_3) + 1$
$(1)(5) = (2)(3) - 1$	$(F_2)(F_5) = (F_3)(F_4) - 1$
$(2)(8) = (3)(5) + 1$	$(F_3)(F_6) = (F_4)(F_5) + 1$
$(3)(13) = (5)(8) - 1$	$(F_4)(F_7) = (F_5)(F_6) - 1$

(Show numbers here)

(Use the F notation here.)

General pattern or formula when k is an even number: $(F_k)(F_{k+3}) = \underline{\hspace{2cm}}$

True or False. The Fibonacci numbers are found in all plant life, with no exceptions.

True or False? Fibonacci was best known during his lifetime as the discoverer of what are now known as the Fibonacci numbers.