

SCORE: ____ / 10 POINTS

NO CALCULATORS ALLOWED

Find the equation of the tangent line to $y = \sqrt{x^2 + 3}$ at $x = -1$.

SCORE: ____ / 5 POINTS

DO NOT USE DIFFERENTIATION SHORTCUTS.

POINT = $(-1, 2)$

$$\begin{aligned} m_{\text{tan}} &= \lim_{h \rightarrow 0} \frac{\sqrt{(-1+h)^2 + 3} - 2}{h} \\ &= \lim_{h \rightarrow 0} \frac{\sqrt{h^2 - 2h + 4} - 2}{h} \\ &= \lim_{h \rightarrow 0} \frac{h^2 - 2h + 4 - 4}{h(\sqrt{h^2 - 2h + 4} + 2)} \\ &= \lim_{h \rightarrow 0} \frac{h - 2}{\sqrt{h^2 - 2h + 4} + 2} \\ &= \frac{-2}{\sqrt{4} + 2} = -\frac{1}{2} \end{aligned}$$

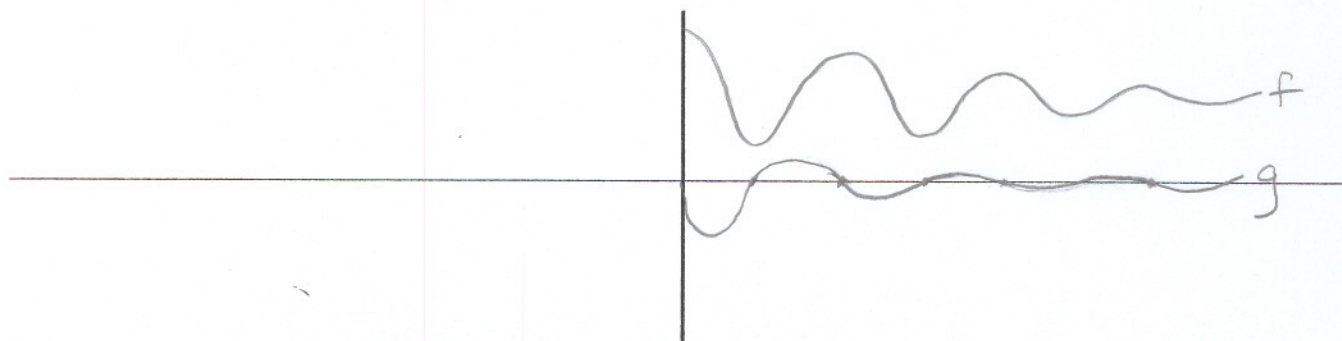
$$\begin{aligned} y - 2 &= -\frac{1}{2}(x - (-1)) \\ y &= 2 - \frac{1}{2}(x + 1) \end{aligned}$$

Let $f(t)$ represent the height of a bungee jumper t seconds after she jumps from a bridge.

SCORE: ____ / 3 POINTS

Let $g(t)$ represent her velocity (use + for upward velocity and - for downward velocity).

Sketch graphs of $f(t)$ and $g(t)$ on the same set of axes.



1/2 POINT EACH

Suppose that $f(t)$ represents Graham's weight (in kilograms) t months after he committed to starting a new

SCORE: ____ / 2 POINTS

exercise regimen. Interpret the statement $\frac{f(3) - f(1)}{2} = 5$. Be as specific as possible, using the correct units for all relevant numbers.

FROM THE FIRST MONTH TO THE THIRD MONTH AFTER HE COMMITTED TO STARTING A NEW EXERCISE REGIMEN, GRAHAM GAINED AN AVERAGE OF 5 kg PER MONTH