

SCORE: ____ / 10 POINTS

NO CALCULATORS ALLOWED

Find the equation of the tangent line to $y = \frac{x}{2-x}$ at $x = -1$.

SCORE: ____ / 5 POINTS

DO NOT USE DIFFERENTIATION SHORTCUTS.

$$\begin{aligned} \text{POINT} &= (-1, -\frac{1}{3}) \\ m_{\text{tan}} &= \lim_{h \rightarrow 0} \frac{\frac{-1+h}{2-(-1+h)} - \frac{1}{3}}{h} \quad 1 \\ &= \lim_{h \rightarrow 0} \frac{\frac{h-1}{3-h} + \frac{1}{3}}{h} \\ &= \lim_{h \rightarrow 0} \frac{3(h-1) + 3-h}{3h(3-h)} \\ &= \lim_{h \rightarrow 0} \frac{2h}{3h(3-h)} \quad 2 \\ &= \frac{2}{9} \quad 1 \end{aligned}$$

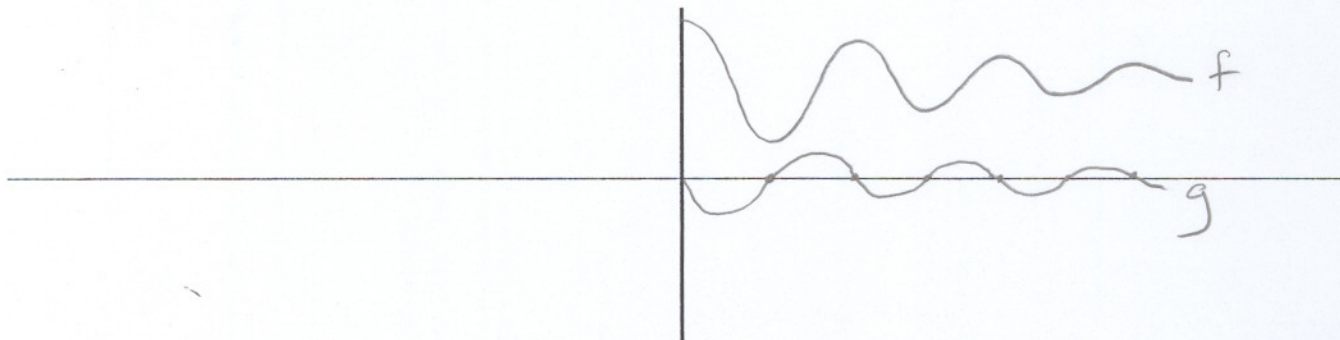
$$\begin{aligned} y - (-\frac{1}{3}) &= \frac{2}{9}(x - (-1)) \\ y &= -\frac{1}{3} + \frac{2}{9}(x+1) \end{aligned}$$

Let $f(t)$ represent the height of a bungee jumper t seconds after she jumps from a bridge.

SCORE: ____ / 3 POINTS

Let $g(t)$ represent her velocity (use + for upward velocity and - for downward velocity).

Sketch graphs of $f(t)$ and $g(t)$ on the same set of axes.



Suppose that $f(t)$ represents Harpo's weight (in pounds) t weeks after he committed to starting a new diet.

SCORE: ____ / 2 POINTS

Interpret the statement $\lim_{h \rightarrow 0} \frac{f(5+h) - f(5)}{h} = \frac{1}{2}$. Be as specific as possible, using the correct units for all relevant numbers.

FIVE WEEKS AFTER HE COMMITTED TO STARTING A NEW DIET,
HARPO WAS GAINING WEIGHT AT $\frac{1}{2}$ POUND PER WEEK