

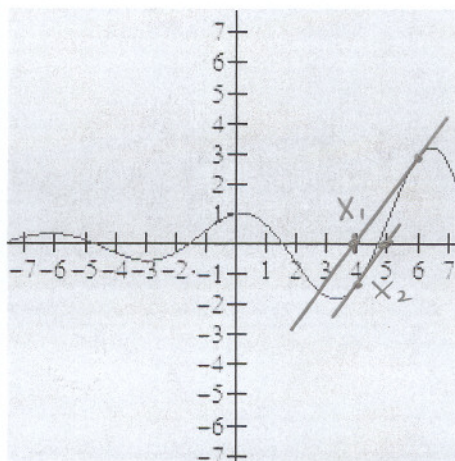
SCORE: \_\_\_\_ / 10 POINTS

# NO CALCULATORS ALLOWED

••■■■■■■■■•• You should probably get back to the quiz, instead of spending time looking at the interstitials. ••■■■■■■■■••

Using Newton's method to solve  $f(x) = 0$  for the function shown below,  
find an approximate value of  $x_2$  if  $x_0 = 6$ .

SCORE: \_\_\_\_ / 2 POINTS



$$x_1 \approx 4$$

$$x_2 \approx 5$$

••■■■■■■■■•• Seriously, stop looking at the interstitials. ••■■■■■■■■••

Using Newton's method to solve  $x^2 + 4 = 6x$ , find the value of  $x_2$  if  $x_0 = 4$ .

SCORE: \_\_\_\_ / 2 POINTS

You must show all relevant values that were calculated.

$$\begin{aligned} & \left[ \begin{aligned} & x^2 - 6x + 4 = 0 \\ & f(x) \\ & f'(x) = 2x - 6 \end{aligned} \right] \end{aligned}$$

$$\begin{aligned} x_0 &= 4 \\ x_1 &= 4 - \frac{f(4)}{f'(4)} = 4 - \frac{-4}{2} = 6 \\ x_2 &= 6 - \frac{f(6)}{f'(6)} = 6 - \frac{4}{6} = 5\frac{1}{3} \end{aligned}$$

••■■■■■■■■•• Why did the chicken cross the road? She didn't – she was too busy looking at the interstitials. ••■■■■■■■■••

Evaluate the following limits.

SCORE: \_\_\_\_ / 6 POINTS

[a]  $\lim_{x \rightarrow 0^+} \left( \frac{1}{x} - 1 \right)^x$  CONSIDER  $\lim_{x \rightarrow 0^+} \ln \left( \frac{1}{x} - 1 \right)^x$  [b]

$$\begin{aligned} & \lim_{x \rightarrow 0^+} \ln \left( \frac{1}{x} - 1 \right)^x \quad \frac{0}{0} \\ &= \lim_{x \rightarrow 0^+} x \ln \left( \frac{1}{x} - 1 \right) \quad 0 \cdot \infty \\ &= \lim_{x \rightarrow 0^+} \frac{\ln \left( \frac{1}{x} - 1 \right)}{\frac{1}{x}} \quad \frac{\infty}{\infty} \\ &= \lim_{x \rightarrow 0^+} \frac{\frac{1}{\frac{1}{x} - 1} \cdot -\frac{1}{x^2}}{-\frac{1}{x^2}} \quad \frac{1}{\infty} \\ &= 0 \quad \frac{1}{2} \\ & \text{so } \lim_{x \rightarrow 0^+} \left( \frac{1}{x} - 1 \right)^x = e^0 = 1 \end{aligned}$$

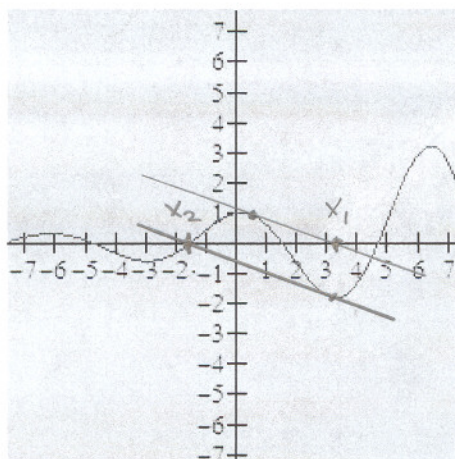
$$\begin{aligned} & \lim_{x \rightarrow 0} \frac{x \sin x}{1 - \cos x} \quad \frac{0}{0} \\ &= \lim_{x \rightarrow 0} \frac{\sin x + x \cos x}{\sin x} \quad \frac{0}{0} \\ &= \lim_{x \rightarrow 0} \frac{\cos x + \cos x - x \sin x}{\cos x} \quad 1 \\ &= \frac{2}{1} \\ &= 2 \quad \frac{1}{2} \end{aligned}$$

**NO CALCULATORS ALLOWED**

**SCORE:**      / 2 POINTS

SEE OTHER KEY

**SCORE:     / 2 POINTS**



$$x_1 \approx 3.2$$
$$x_2 \approx -1.6$$

**SCORE:** \_\_\_\_ / 6 POINTS

[b]  $\lim_{x \rightarrow 0^+} \left( \frac{1}{x} - 1 \right)^x$

SEE OTHER KEY