

What day of the month is your birthday ?

What are the last 2 digits of your address ?

What are the last 2 digits of your zip code ?

What are the last 2 digits of your social security number ?

[IF YOU DO NOT HAVE A SOCIAL SECURITY NUMBER,
USE YOUR STUDENT ID NUMBER]**NO CALCULATORS ALLOWED**

Complete the following definition:

$$\text{The derivative of the function } f \text{ is } \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$$

SCORE: ___ / 3 POINTS

Use the definition of the derivative to find the derivative of $f(x) = \frac{3}{1-2x}$.

SCORE: ___ / 5 POINTS

NO DIFFERENTIATION SHORTCUTS ALLOWED.

$$f'(x) = \lim_{h \rightarrow 0} \frac{\frac{3}{1-2(x+h)} - \frac{3}{1-2x}}{h}$$

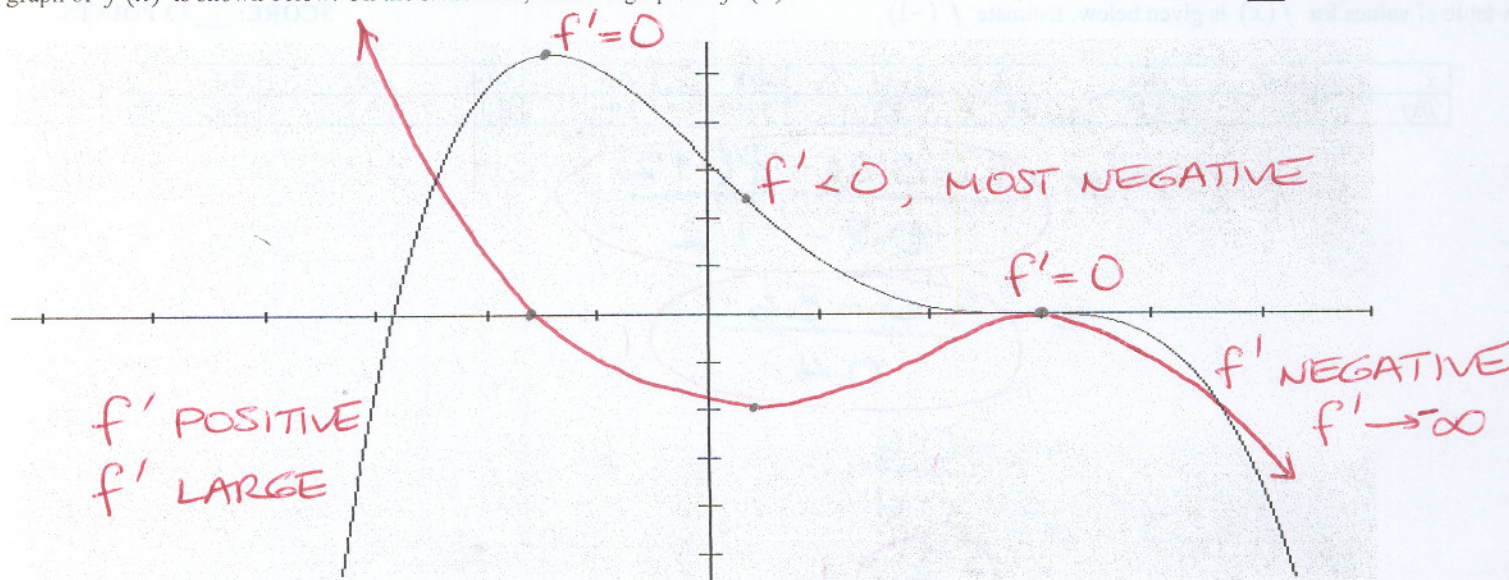
$$= \lim_{h \rightarrow 0} \frac{3(1-2x) - 3(1-2(x+h))}{h(1-2(x+h))(1-2x)}$$

$$= \lim_{h \rightarrow 0} \frac{3 - 6x - 3 + 6x + 6h}{h(1-2(x+h))(1-2x)} = \lim_{h \rightarrow 0} \frac{6}{(1-2(x+h))(1-2x)}$$

$$= \frac{6}{(1-2x)^2}$$

The graph of $f(x)$ is shown below. On the same axes, sketch a graph of $f'(x)$.

SCORE: ___ / 4 POINTS



Use the definition of the derivative to find the derivative of $f(x) = \sqrt{4-3x}$.

SCORE: ___ / 5 POINTS

NO DIFFERENTIATION SHORTCUTS ALLOWED.

$$\begin{aligned}
 f'(x) &= \lim_{h \rightarrow 0} \frac{\sqrt{4-3(x+h)} - \sqrt{4-3x}}{h} \quad 2 \\
 &= \lim_{h \rightarrow 0} \frac{4-3(x+h) - (4-3x)}{h(\sqrt{4-3(x+h)} + \sqrt{4-3x})} \quad 1 \\
 &= \lim_{h \rightarrow 0} \frac{\cancel{4} - 3x - 3h - \cancel{4} + 3x}{h(\sqrt{4-3(x+h)} + \sqrt{4-3x})} = \lim_{h \rightarrow 0} \frac{-3}{\sqrt{4-3(x+h)} + \sqrt{4-3x}} \quad 1 \\
 &= \frac{-3}{2\sqrt{4-3x}} \quad 1
 \end{aligned}$$

A table of values for $f(x)$ is given below. Estimate $f'(-1)$.

SCORE: ___ / 3 POINTS

x	-1.6	-1.4	-1.2	-1	-0.8	-0.6	-0.4	-0.2	0
$f(x)$	4.9	4.1	3.6	3.5	3.0	2.9	3.1	3.7	4.3

$$\begin{aligned}
 f'(-1) &\approx \frac{f(-0.8) - f(-1.2)}{-0.8 - -1.2} \quad 1 \\
 &= \frac{3.0 - 3.6}{0.4} \quad 1 \\
 &= \frac{-0.6}{0.4} \\
 &= -\frac{3}{2} \quad 1
 \end{aligned}$$