

What day of the month is your birthday? ___

What are the last 2 digits of your address? ___

What are the last 2 digits of your zip code? ___

What are the last 2 digits of your social security number? ___

[IF YOU DO NOT HAVE A SOCIAL SECURITY NUMBER,
USE YOUR STUDENT ID NUMBER]**NO CALCULATORS ALLOWED**

Complete the following definition:

The derivative of the function f is

$$\lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$$

SCORE: ___ / 3 POINTS

Use the definition of the derivative to find the derivative of $f(x) = \sqrt{2-5x}$.

SCORE: ___ / 5 POINTS

NO DIFFERENTIATION SHORTCUTS ALLOWED.

$$f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h} = \lim_{h \rightarrow 0} \frac{\sqrt{2-5(x+h)} - \sqrt{2-5x}}{h}$$

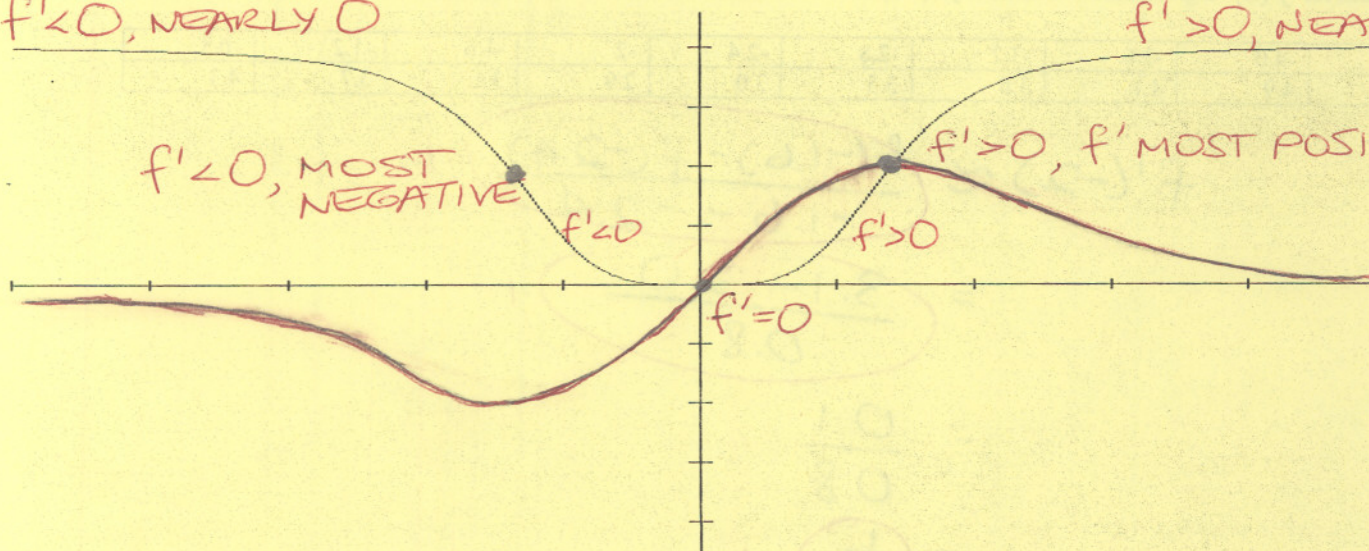
$$= \lim_{h \rightarrow 0} \frac{2 - 5(x+h) - (2 - 5x)}{h(\sqrt{2-5(x+h)} + \sqrt{2-5x})}$$

$$= \lim_{h \rightarrow 0} \frac{2 - 5x - 5h - 2 + 5x}{h(\sqrt{2-5(x+h)} + \sqrt{2-5x})} = \lim_{h \rightarrow 0} \frac{-5}{\sqrt{2-5(x+h)} + \sqrt{2-5x}}$$

$$= \frac{-5}{2\sqrt{2-5x}}$$

The graph of $f(x)$ is shown below. On the same axes, sketch a graph of $f'(x)$.

SCORE: ___ / 4 POINTS

 $f' < 0$, NEARLY 0 $f' > 0$, NEARLY 0 $f' < 0$, MOST NEGATIVE $f' > 0$, f' MOST POSITIVE

Use the definition of the derivative to find the derivative of $f(x) = \frac{4}{1-5x}$.

SCORE: ___ / 5 POINTS

NO DIFFERENTIATION SHORTCUTS ALLOWED.

$$\begin{aligned}
 f'(x) &= \lim_{h \rightarrow 0} \frac{\frac{4}{1-5(x+h)} - \frac{4}{1-5x}}{h} \quad 2 \\
 &= \lim_{h \rightarrow 0} \frac{4(1-5x) - 4(1-5(x+h))}{h(1-5(x+h))(1-5x)} \quad 1 \\
 &= \lim_{h \rightarrow 0} \frac{\cancel{4} - \cancel{20}x - \cancel{4} + 20x + 20h}{h(1-5(x+h))(1-5x)} = \lim_{h \rightarrow 0} \frac{20}{(1-5(x+h))(1-5x)} \quad 1 \\
 &= \frac{20}{(1-5x)^2} \quad 3 \quad 1
 \end{aligned}$$

A table of values for $f(x)$ is given below. Estimate $f'(-2)$.

SCORE: ___ / 3 POINTS

x	-4.0	-3.6	-3.2	-2.8	-2.4	-2	-1.6	-1.2	-0.8
$f(x)$	4.9	4.1	3.6	3.5	3.0	2.9	3.1	3.7	4.3

$$\begin{aligned}
 f'(-2) &\approx \frac{f(-1.6) - f(-2.4)}{-1.6 - -2.4} \quad 1 \\
 &= \frac{3.1 - 3.0}{0.8} \quad 1 \\
 &= \frac{0.1}{0.8} \\
 &= \frac{1}{8} \quad 1
 \end{aligned}$$