



SCORE: \_\_\_ / 20 POINTS

What day of the month is your birthday?  
 What are the last 2 digits of your address?  
 What are the last 2 digits of your zip code?  
 What are the last 2 digits of your social security number?  
 [IF YOU DO NOT HAVE A SOCIAL SECURITY NUMBER,  
 USE YOUR STUDENT ID NUMBER]

## NO CALCULATORS ALLOWED

Find the maximum and minimum values of  $r$  (and the corresponding values of  $\theta$ ) for  $r = 5 \sin 3\theta$ .

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$$r = 5 \text{ when } \sin 3\theta = 1$$

$$0 \leq \theta < 2\pi$$

$$0 \leq 3\theta < 6\pi$$

$$\begin{aligned} 3\theta &= \frac{\pi}{2}, \frac{5\pi}{2}, \frac{9\pi}{2} \\ \theta &= \frac{\pi}{6}, \frac{5\pi}{6}, \frac{3\pi}{2} \end{aligned}$$

$$r = -5 \text{ when } \sin 3\theta = -1$$

$\frac{1}{2}$  POINT  
EACH

$$\begin{aligned} 3\theta &= \frac{3\pi}{2}, \frac{7\pi}{2}, \frac{11\pi}{2} \\ \theta &= \frac{\pi}{2}, \frac{7\pi}{6}, \frac{11\pi}{6} \end{aligned}$$

Find all zeros of  $r = 2 + 4 \cos \theta$ .

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$$r = 0 \text{ when } 2 + 4 \cos \theta = 0$$

$$\begin{aligned} \cos \theta &= -\frac{1}{2}, \\ \theta &= \frac{2\pi}{3}, \frac{4\pi}{3} \end{aligned}$$

Consider the conic  $r = \frac{6}{2 - 3 \cos \theta} = \frac{3}{1 - \frac{3}{2} \cos \theta}$ .  $e = \frac{3}{2}$

SCORE: \_\_\_ / 6 POINTS

[a] Classify the type of the conic.

HYPERBOLA

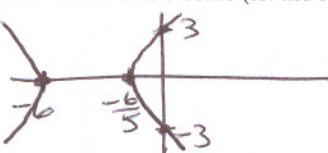
[b] Find the rectangular equation of the directrix.

$$\begin{aligned} ep &= 3 \\ \frac{3}{2}P &= 3, \frac{1}{2} \\ P &= 2 \text{ LEFT OF POLE} \end{aligned}$$

$$\frac{1}{2}x = -2, \frac{1}{2}$$

[c] Find the rectangular coordinates of the other focus of the conic (ie. the focus that is NOT the pole).

$$\begin{array}{cccccc} \theta & 0 & \frac{\pi}{2} & \pi & \frac{3\pi}{2} \\ r & -6 & 3 & \frac{6}{5} & 3 \end{array}$$



$$\text{CENTER}_2 = \frac{1}{2}(-6 + -\frac{6}{5}) = -\frac{18}{5}, \frac{1}{2}$$

$$\text{FOCUS} = 2(-\frac{18}{5}) = -\frac{36}{5}, \frac{1}{2}$$

$$(0, -\frac{36}{5})$$

Find a polar equation for the ellipse with a focus at the pole, and vertices at  $\left(8, \frac{\pi}{2}\right)$  and  $\left(4, \frac{3\pi}{2}\right)$

SCORE: \_\_\_ / 6 POINTS



$$r = \frac{ep}{1 - e \sin \theta}$$

OR

$$8 = \frac{ep}{1 - e}, \frac{1}{2}$$

$$\text{CENTER} = \frac{1}{2}(8 + 4) = 6$$

$$e = \frac{c}{a} = \frac{2}{6} = \frac{1}{3}$$

$$4 = \frac{ep}{1 + e}, \frac{1}{2}$$

$$8(1 - e) = 4(1 + e), \frac{1}{2}$$

$$8 - 8e = 4 + 4e$$

$$-12e = -4$$

$$e = \frac{1}{3}, 1$$

$$4 = \frac{\frac{1}{3}P}{1 + \frac{1}{3}}, \frac{1}{2}$$

$$4 = \frac{P}{3 + 1} = \frac{P}{4}$$

$$P = 16, 1$$

$$\begin{aligned} r &= \frac{\frac{1}{3}P}{1 + \frac{1}{3} \sin \theta}, \frac{1}{2} \\ r &= \frac{16}{3 + \sin \theta}, \frac{1}{2} \end{aligned}$$