

ERRORS FROM MIDTERM 1

The Fundamental Theorem of Calculus states that

If f is continuous on $[a, b]$, then the definite integral of f on the interval $[a, b]$ is denoted by

$$\int_a^b f(x) dx = \lim_{n \rightarrow \infty} \sum_{i=1}^n f(x_i^*) \Delta x \quad \text{where } a + (i-1)\Delta x \leq x_i^* \leq a + i\Delta x.$$

$$(2t^2)^3 = 2t^5 \quad \text{or} \quad 2t^3 \quad \text{or} \quad 2t^6 \quad \text{or} \quad 16t^6$$

$$\sqrt{x+4} = \sqrt{x} + 2$$

$$\frac{x^2}{\sqrt{x+4}} = \frac{x^4}{x+4}$$

$$(u^2 - 4)^2 = u^2 - 8u + 16$$

$$\frac{d}{dx}(\sqrt{x+4}) = \frac{x+4}{2}$$

$$\int (u^2 - 4)^2 du = \frac{(u^2 - 4)^3}{3} + C$$

$$\int (u^2 - 8u + 16) du = 2u - 8 + C$$

$$\int \frac{1}{\sqrt[3]{u+4}} du = \ln|\sqrt[3]{u+4}| + C$$

$$(e^{2x})^2 = e^{4x^2} = 2e^{4x}$$

$$(e^{2x} - 1)^2 = e^{4x} + 2e^{2x} - 1$$

$$(e^{4x} - 2e^{2x} + 1) \left(\frac{1}{-2e^{2x}} \right) = e^{4x} + 1$$

$$\frac{d}{dx}(e^{2x} - 1) = 2e^{2x} - 1 \quad \text{or} \quad -2e^{2x}$$

$$\int (e^{4x} - e^{2x}) dx = \frac{e^{5x}}{5} - \frac{e^{3x}}{3} + C \quad \text{or} \quad 4e^{4x} - 2e^{2x} + C$$

$$\int (e^{4x^2} - e^{2x}) dx = 4x^2 e^{4x^2} 8x - 4xe^2 + C$$

$$\int e^{4x^2} dx = \frac{e^{4x^2}}{8x} + C$$

$$\int \frac{(e^{2x} - 1)^2}{2e^{2x}} dx = \frac{1}{2e^{2x}} \int (e^{2x} - 1)^2 dx$$

$$\sin \frac{\pi}{6} = \cos \frac{2\pi}{3} = \cos \frac{\pi}{3} = \sqrt{2}$$

$$\int \left(3 \cos \frac{1}{2} x + \sin 2x \right) dx = 3 \sin \frac{1}{2} x - \cos 2x + C \quad \text{or} \quad -\frac{3}{2} \sin \frac{1}{2} x + 2 \cos 2x + C \quad \text{or} \quad \frac{3}{2} \sin \frac{1}{2} x - 2 \cos 2x + C \quad \text{or} \quad -6 \sin \frac{1}{2} x + \frac{1}{2} \cos 2x + C$$

$$\int \sec x \tan x dx = \sec^2 x + C \quad \text{or} \quad \sec^3 x + \tan^3 x + C$$

$$\frac{3u}{13-u^2} = \frac{3u \cdot (-u^{-2})}{13} = \frac{-3u^{-1}}{13} = \frac{-3}{13u}$$

$$\int \frac{6+3x}{9-4x-x^2} dx = \frac{6x + \frac{3}{2}x^2}{9x - 2x^2 - \frac{1}{3}x^3} + C$$

$$\frac{d}{dx} e^{2x} = 2xe^{2x} \cdot 2 \quad \text{or} \quad \frac{1}{2} e^{2x}$$

$$\frac{d}{dx} 4xe^{2x} = 8x^2 e^{2x} \cdot 2$$