

**YOU MAY USE ANY OF THE IDENTITIES YOU FOUND ON PAGE 1 OF
THE HYPERBOLIC SUPPLEMENT WITHOUT PROVING THEM HERE**

[3 POINTS] Using implicit differentiation, prove the derivative of $y = \sinh^{-1} x$.

Evaluate the following derivatives and anti-derivatives and simplify. Write your final answers in terms of hyperbolic functions if possible.
(You may use the derivatives and anti-derivatives of the hyperbolic and inverse hyperbolic functions without proving them.)

[2 POINTS EACH]

$$\frac{d}{dx} e^{-2x} \cosh^{-1} 3x$$

$$\frac{d}{dx} \tanh^{-1}(\cos x)$$

$$\int \sinh^3 x \cosh^4 x \, dx$$

$$\frac{d}{dx} \sin^{-1}(\tanh x)$$

[3 POINTS EACH]

$$\frac{d}{dx} \frac{\sinh x}{1 - \cosh x}$$

$$\int e^{-2x} \cosh 3x \, dx$$

$$\int \tanh(\ln x) \, dx$$