

[3 POINTS] Translate into summation notation. YOU DO NOT NEED TO COMPUTE THE SUM.

"The sum of the cubes of the first 100 positive even integers"

$$\sum_{i=1}^{100} (2i)^3$$

[7 POINTS] Use summation rules/shortcuts to compute the sum $\sum_{i=1}^{100} (4 - 3i - i^2)$.

$$4(100) - 3 \cdot \frac{100(101)}{2} - \frac{100(101)(201)}{6} = -353100$$

[10 POINTS]

Use summation rules/shortcuts to compute the sum of the form $\sum_{i=1}^n f(x_i) \Delta x$ for

$$f(x) = x^2 + 2x; \quad x = 3.1, 3.2, 3.3, \dots, 4.0; \quad \Delta x = 0.1; \quad n = 10$$

$$x_i = 3 + \frac{i}{10}$$

$$\sum_{i=1}^{10} f\left(3 + \frac{i}{10}\right) 0.1$$

$$= 0.1 \sum_{i=1}^{10} \left[\left(3 + \frac{i}{10}\right)^2 + 2\left(3 + \frac{i}{10}\right) \right]$$

$$= 0.1 \sum_{i=1}^{10} \left(9 + \frac{3i}{5} + \frac{i^2}{100} + 6 + \frac{i}{5} \right)$$

$$= 0.1 \sum_{i=1}^{10} \left(15 + \frac{4i}{5} + \frac{i^2}{100} \right)$$

$$= 0.1 \left(15(10) + \frac{4}{5} \frac{10(11)}{2} + \frac{1}{100} \frac{10(11)(21)}{6} \right)$$

$$= 19.785$$