GROUP QUIZ 2 QUESTIONS

Identify the following limits as Riemann sums, and evaluate the limits. Show all algebraic reasoning.

ROUP QUIZ 2 QUESTIONS

[a]
$$\lim_{n \to \infty} \frac{5}{n} \left[\frac{1}{\sqrt{4 + \frac{5}{n}}} + \frac{1}{\sqrt{4 + \frac{10}{n}}} + \dots + \frac{1}{3} \right]$$

[b]
$$\lim_{n \to \infty} \frac{3}{n} \left| \frac{1}{\left(2 + \frac{3}{n}\right)^2} + \frac{1}{\left(2 + \frac{6}{n}\right)^2} + \frac{1}{\left(2 + \frac{9}{n}\right)^2} + \dots + \frac{1}{25} \right|$$

Find the average value of $f(x) = \frac{6x-1}{\sqrt{x}}$ on [1, 4]. Simplify your answer.

Find the average value of $f(x) = \left(x^{\frac{2}{3}} - 2x^{\frac{1}{3}}\right)^2$ on [0, 1]. Simplify your answer.

Find the area between the graph of $f(x) = x^2 - 2x$ and the x-axis on [0, 3].

Find the area between the graph of $f(x) = x^2 - x$ and the x-axis on [0, 3].