
SCORE: ____ / 10 POINTS

Find the hydrostatic force on the vertical window of an aquarium if the window is a triangle of height 1 foot and base 2 feet, with the base down and 10 feet below the surface of the water. (The base of the triangle is 10 feet below the surface of the water.) **SCORE: ____ / 5 POINTS**

$$\begin{aligned} & \int_0^1 \rho(9+x)(2x) dx \\ &= \rho \int_0^1 (18x + 2x^2) dx \\ &= \rho \left(9x^2 + \frac{2x^3}{3} \right) \Big|_0^1 \\ &= \rho \left(9 + \frac{2}{3} \right) \\ &= \frac{29}{3} \rho \text{ lb} \end{aligned}$$

A spherical tank of radius 4 feet containing water is buried underground, so that its center is 8 feet below ground level. Find the work done in pumping the top half of the water to ground level if the tank is full.

SCORE: ____ / 5 POINTS

$$\begin{aligned} & \int_0^4 \rho \pi (8-x)(\sqrt{16-x^2})^2 dx \\ &= \rho \pi \int_0^4 (8-x)(16-x^2) dx \\ &= \rho \pi \int_0^4 (128 - 16x - 8x^2 + x^3) dx \\ &= \rho \pi \left(128x - 8x^2 - \frac{8x^3}{3} + \frac{x^4}{4} \right) \Big|_0^4 \\ &= \rho \pi \left(128(4) - 8(16) - \frac{8(64)}{3} + \frac{256}{4} \right) \\ &= \frac{832}{3} \rho \pi \text{ ft}\cdot\text{lb} \end{aligned}$$