
SCORE: ____ / 10 POINTS

A spherical tank of radius 4 feet containing water is buried underground, so that its center is 8 feet below ground level. Find the work done in pumping the water to ground level if the tank is half full.

SCORE: ____ / 5 POINTS

$$\begin{aligned}
 & \int_0^4 \rho \pi (8+x)(\sqrt{16-x^2})^2 dx \\
 &= \rho \pi \int_0^4 (8+x)(16-x^2) dx \\
 &= \rho \pi \int_0^4 (128+16x-8x^2-x^3) dx \\
 &= \rho \pi \left(128x + 8x^2 - \frac{8x^3}{3} - \frac{x^4}{4} \right) \bigg|_0^4 \\
 &= \rho \pi \left(128(4) + 8(16) - \frac{8(64)}{3} - \frac{256}{4} \right) \\
 &= \frac{1216}{3} \rho \pi \text{ ft-lb}
 \end{aligned}$$

Find the hydrostatic force on the vertical window of an aquarium if the window is a triangle of height 1 foot and base 2 feet, with the base up and 10 feet below the surface of the water. (The base of the triangle is 10 feet below the surface of the water.)

SCORE: ____ / 5 POINTS

$$\begin{aligned}
 & \int_0^1 \rho (11-x)(2x) dx \\
 &= \rho \int_0^1 (22x-2x^2) dx \\
 &= \rho \left(11x^2 - \frac{2x^3}{3} \right) \bigg|_0^1 \\
 &= \rho \left(11 - \frac{2}{3} \right) \\
 &= \frac{31}{3} \rho \text{ lb}
 \end{aligned}$$