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SCORE: \_\_\_\_ / 10 POINTS

**For these 3 questions, you may NOT use any hyperbolic identities, nor the derivatives or anti-derivatives of any hyperbolic functions, unless you prove them.**

Rewrite  $\cosh^2 x + \sinh^2 x$  in terms of exponential functions, simplify, then rewrite in terms of hyperbolic functions, if possible.

Prove a formula for  $\cosh(x - y)$  in terms of hyperbolic functions.

Given that  $\tanh x = \frac{\sinh x}{\cosh x}$ , find  $\lim_{x \rightarrow \infty} \tanh x$  algebraically.

**For all remaining questions, you may use the hyperbolic identity  $\cosh^2 x - \sinh^2 x = 1$ , and the derivatives and anti-derivatives of  $\sinh x$  and  $\cosh x$ , without proving them. You must prove any other hyperbolic identity, derivative or anti-derivative you use.**

Prove an identity involving  $\operatorname{csch} x$  and  $\operatorname{coth} x$ , which resembles the Pythagorean identity involving  $\csc x$  and  $\cot x$ .

Find  $\frac{d}{dx} \frac{\sinh x}{1 - \cosh x}$ . Simplify your answer.

Find  $\int e^{-2x} \cosh 3x \, dx$ . Simplify your answer.

Find  $\int \tanh(\ln x) dx$  . Simplify your answer.

Find a formula for  $\tanh^{-1} x$  .

Find  $\frac{d}{dx} \cosh^{-1} x$  by implicit differentiation on  $y = \cosh^{-1} x$  .

Find  $\frac{d}{dx} \tanh^{-1}(\cos x)$ . Simplify your answer.

**For this question only, you may use the derivative of  $\tanh^{-1} x$  that you found in the handout without proving it, if useful.**

Find  $\int \sinh^{-1} x \, dx$ .