

You should be able to solve the following without a calculator

[1] Find the domains of the following functions.

[a] $f(x) = 4^x$

[b] $f(x) = \log_3 x$

[2] Find the ranges of the following functions.

[a] $f(x) = 5^x$

[b] $f(x) = \log_7 x$

[3] Evaluate the following. Write “UNDEFINED” if the value does not exist.

[a] $\log_3 81$

[b] $\log_6 36$

[c] $\log_5 125$

[d] $\log_7 0$

[e] $\log_8 -8$

[f] $\log_6 1$

[g] $\log_2 64$

[h] $\log 10000$

[i] $\log_4 4^6$

[j] $\log_8 8^{-3}$

[k] $3^{\log_3 7}$

[l] $6^{\log_6 0}$

[m] $5^{\log_5 -10}$

[n] $10^{\log 5}$

[4] Find the exact solutions of the following equations. **Check your answers.**

[a] $3^{2-x} = 81$

[b] $8^{3x-7} = 4^{6-x}$

[c] $\log_4(5x+9) = 3$

[d] $\log_3(x^2 - 7) - \log_3(1 - x) = 1$

[e] $\log_2(10x - 2) - \log_2(x + 1) = 3$

[f] $\log(2x + 6) + \log(x - 2) = 2$

[5] Write as the logarithm of a single quantity. Simplify your answer.

[a] $\log 8 + \log 5$

[b] $\log 42 - \log 6$

[c] $5 \log 2$

[d] $3 \log x + 2 \log y$

[e] $2 \log x - \log y + \log z$

[f] $\log z - 2 \log y - \log x$

[g] $2 \log y + 3 \log z - \log x$

[h] $4 \log z + \log x + 3 \log y$

[6] Write as the sums and/or differences and/or multiples of logarithms of numbers or single variables.

[a] $\log(7 \times 11)$

[b] $\log\left(\frac{13}{5}\right)$

[c] $\log 3^8$

[d] $\log r^4 s$

[e] $\log \frac{a^5}{b^2}$

[f] $\log \frac{m}{n^2 p^3}$

[g] $\log \frac{x^2}{\sqrt{yz}}$

[7] **MULTIPLE CHOICE**

[a] The graph of $f(x) = 3 \log(x + 4)$ has an asymptote at

[i] $x = 4$

[ii] $x = -4$

[iii] $y = -4$

[iv] $y = 4$

[v] $y = 3$

[b] The graph of $f(x) = -5 \cdot 2^{x-3}$ has an asymptote at

[i] $x = 3$

[ii] $x = 0$

[iii] $y = -5$

[iv] $y = 3$

[v] $y = 0$

[c] For the logarithm curve $f(x) = \log_2 x$, as the value of $x \rightarrow \infty$, the value of $y \rightarrow$

[i] ∞

[ii] $-\infty$

[iii] 0

[iv] 1

[v] -1

[d] For the logarithm curve $f(x) = \log_5 x$, as the value of $x \rightarrow 0$, the value of $y \rightarrow$

[i] ∞

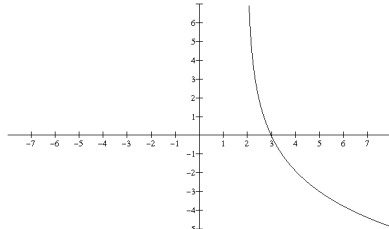
[ii] $-\infty$

[iii] 0

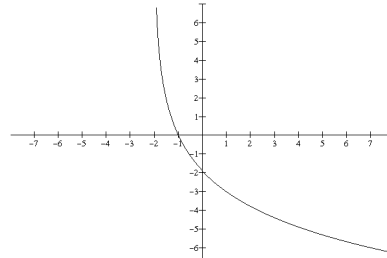
[iv] 1

[v] -1

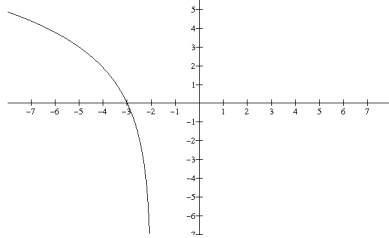
[8] The graph of $f(x) = -3\log_2(x+2)$ is



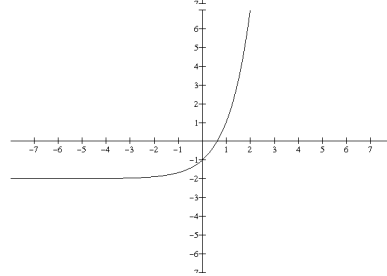
[a]



[b]



[c]



[d]

You may use a non-graphing calculator for the following

[9] Draw the graph of $f(x) = -3 \cdot 2^{-(x-1)}$ by finding and plotting functions values, and connecting to get the shape of the graph. Show the functions values of at least 5 points on your graph. LABEL ALL ASYMPTOTES CLEARLY.

[10] Find the exact solution of the following equations. Also, use your calculator to find a decimal answer, rounded to 4 decimal places.

[a] $7^x = 3$

[b] $6^{x-2} = 4^{x+1}$

[11] The number of bacteria in a colony is given by $B(t) = 1.3(2.1)^t$.

[a] How many bacteria were there at time $t = 4$? Round your answer to 1 decimal place.

[b] At what time were there at least 41 bacteria? Round your answer to 2 decimal places.

[12] [a] Find the intensity (in microns) of an earthquake with a Richter magnitude of 5.6.

[b] Find the Richter magnitude of an earthquake of intensity 56,000,000 microns.

[13] [a] If you deposit \$200 into an account that pays 2.35% interest annually, what is the value of the account 3 years later?

[b] If you deposit \$200 into an account that pays 2.35% interest annually, when will the value of the account be \$300?

[c] How much should you deposit into an account that pays 2.35% interest annually, if you want the value of the account to be \$200 4 years later?

[b] You deposit \$200 into an account, and 5 years later, the value of the account is \$250. What is the annual interest rate on the account?

ANSWERS

- [1]

[a]

all real numbers

[b]

$\{x > 0\}$
- [2]

[a]

$\{y > 0\}$

[b]

all real numbers
- [3]

[a]

4

[b]

2

[c]

3

[d]

UNDEFINED

[e]

UNDEFINED

[f]

0

[g]

6

[h]

4

[i]

6

[j]

-3

[k]

7

[l]

UNDEFINED

[m]

UNDEFINED

[n]

5
- [4]

[a]

-2

[b]

3

[c]

11

[d]

-5

[e]

5

[f]

7
- [5]

[a]

$\log 40$

[b]

$\log 7$

[c]

$\log 32$

[d]

$\log x^3 y^2$

[e]

$\log \frac{x^2 z}{y}$

[f]

$\log \frac{z}{y^2 x}$

[g]

$\log \frac{y^2 z^3}{x}$

[h]

$\log z^4 xy^3$
- [6]

[a]

$\log 7 + \log 11$

[b]

$\log 13 - \log 5$

[c]

$8 \log 3$

[d]

$4 \log r + \log s$

[e]

$5 \log a - 2 \log b$

[f]

$\log m - 2 \log n - 3 \log p$
- [g]

$2 \log x - \frac{1}{2} \log y - \frac{1}{2} \log z$
- [7]

[a]-[ii]

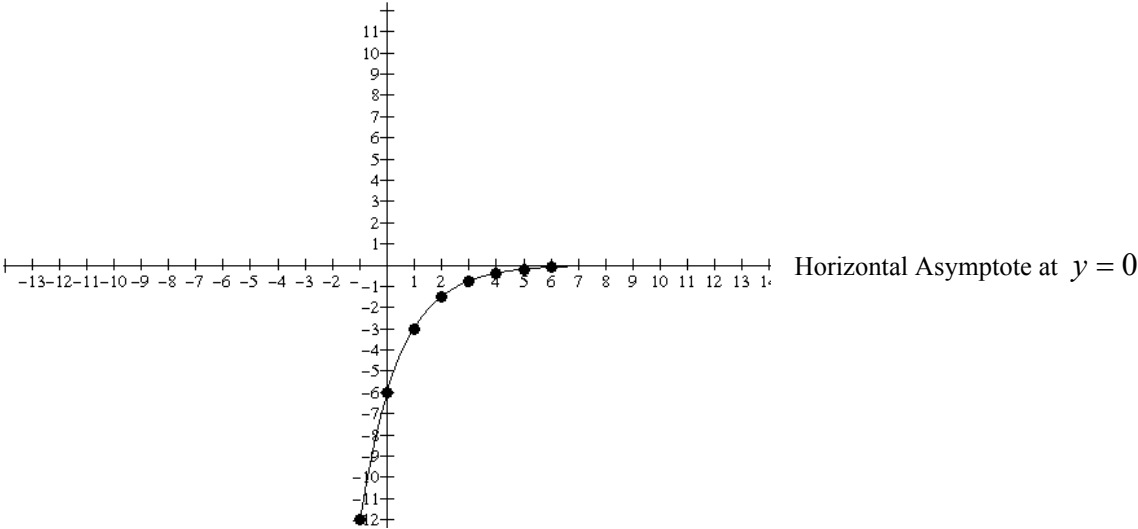
[b]-[v]

[c]-[i]

[d]-[ii]
- [8]

[b]
- [9]

x	-1	0	1	2	3	4	5	6
$f(x)$	-12	-6	-3	-3/2	-3/4	-3/8	-3/16	-3/32



- [10]

[a]

0.5646

[b]

12.2571
- [11]

[a]

25.3 bacteria

[b]

4.65 units of time
- [12]

[a]

398107 microns

[b]

7.748
- [13]

[a]

\$214.43

[b]

17.46 years later

[c]

\$182.25

[d]

4.564%