

SCORE: \_\_\_\_ / 10 POINTS

**NO CALCULATORS ALLOWED**

Evaluate the following limits algebraically. Show all algebraic work.

SCORE: \_\_\_\_ / 8 POINTS

[a]  $\lim_{x \rightarrow 2} \frac{x^3 - 4x}{x^2 + x - 6}$

$$= \lim_{x \rightarrow 2} \frac{x(x^2 - 4)}{(x+3)(x-2)}$$

$$= \lim_{x \rightarrow 2} \frac{x(x+2)(\cancel{x-2})}{(x+3)(\cancel{x-2})}$$

$$= \lim_{x \rightarrow 2} \frac{x(x+2)}{x+3}$$

$$= \frac{2(2+2)}{2+3} = \frac{8}{5}$$

[c]  $\lim_{x \rightarrow -3} \frac{\frac{1}{x^2} - \frac{1}{9}}{x+3}$

$$= \lim_{x \rightarrow -3} \frac{\frac{1}{x^2} - \frac{1}{9}}{x+3} \cdot \frac{9x^2}{9x^2}$$

$$= \lim_{x \rightarrow -3} \frac{9 - x^2}{9x^2(x+3)}$$

$$= \lim_{x \rightarrow -3} \frac{(3-x)(3+x)}{9x^2(x+3)}$$

$$= \lim_{x \rightarrow -3} \frac{3-x}{9x^2} = \frac{3-(-3)}{9(-3)^2} = \frac{6}{81} = \frac{2}{27}$$

[b]  $\lim_{x \rightarrow 1} \frac{4-4x}{\sqrt{3x+1}-2}$

$$= \lim_{x \rightarrow 1} \frac{4-4x}{\sqrt{3x+1}-2} \cdot \frac{\sqrt{3x+1}+2}{\sqrt{3x+1}+2}$$

$$= \lim_{x \rightarrow 1} \frac{(4-4x)(\sqrt{3x+1}+2)}{(3x+1)-4}$$

$$= \lim_{x \rightarrow 1} \frac{(4-4x)(\sqrt{3x+1}+2)}{3x-3}$$

$$= \lim_{x \rightarrow 1} \frac{-4(x-1)(\sqrt{3x+1}+2)}{3(x-1)}$$

$$= \lim_{x \rightarrow 1} \frac{-4}{3} (\sqrt{3x+1}+2)$$

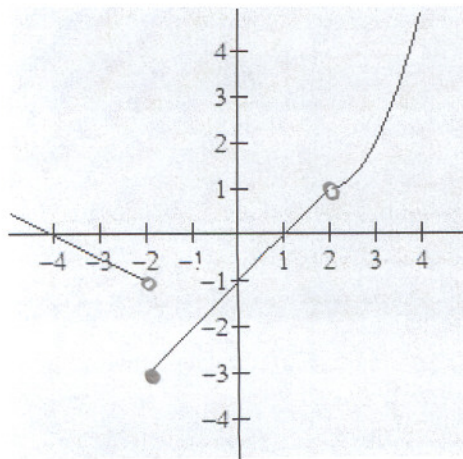
$$= -\frac{4}{3} (\sqrt{3+1}+2) = -\frac{16}{3}$$

1 POINT EACH

\* SUBTRACT  $\frac{1}{2}$  POINT FOR EACH QUESTION WHERE YOU DIDN'T WRITE "lim"  $x \rightarrow$  APPROPRIATELY (MAXIMUM  $-\frac{1}{2}$  POINTS)

Evaluate the following for the function graphed below. If a value does not exist, write DNE.

SCORE: \_\_\_\_ / 2 POINTS



[a]  $\lim_{x \rightarrow -2^-} f(x) = -1$

[b]  $\lim_{x \rightarrow 2} f(x) = 1$

[c]  $f(2) = \text{DNE}$

[d]  $\lim_{x \rightarrow -1} f(x) = -2$

 $\frac{1}{2}$  POINT EACH