

SCORE: 10 / 10 POINTS

What month is your birthday?

What are the first 2 digits of your address?

What are the last 2 digits of your zip code?

What are the last 2 digits of your social security number?

[IF YOU DO NOT HAVE A SOCIAL SECURITY NUMBER,
USE YOUR STUDENT ID NUMBER]

0	1
1	2
8	9
3	6

Estimate the slope of $f(x) = \ln x$ at $x = 3$ by using the method of secant lines discussed in class.SCORE: 4 / 4 POINTSShow 6 points you used, and the corresponding slopes. You must use 3 points on each side of $x = 3$. Round your slopes to 4 decimal places.

POINT

SLOPE OF SECANT LINE

POINT

SLOPE OF SECANT LINE

$$(2.9, \ln 2.9) \quad \underline{0.3390} \quad \frac{1}{2}$$

$$(3.1, \ln 3.1) \quad \underline{0.3279} \quad \frac{1}{2}$$

$$(2.99, \ln 2.99) \quad \underline{0.3339} \quad \frac{1}{2}$$

$$(3.01, \ln 3.01) \quad \underline{0.3328} \quad \frac{1}{2}$$

$$(2.999, \ln 2.999) \quad \underline{0.3334} \quad \frac{1}{2}$$

$$(3.001, \ln 3.001) \quad \underline{0.3333} \quad \frac{1}{2}$$

ESTIMATED SLOPE OF $f(x) = \ln x$ AT $x = 3$: 0.3333 1You want to estimate the length of the curve $f(x) = x^2 - 4x$ from $x = 0$ to $x = 12$ to four decimal places using 4 line segments (at equally spaced x -values).SCORE: 4 / 4 POINTS

[a] Write down the numerical expression you would need to enter into your calculator to find that length.

$$\begin{aligned} & (0,0) \quad (3,-3) \quad (6,12) \quad (9,45) \quad (12,96) \\ & d = \sqrt{(3-0)^2 + (-3-0)^2} + \sqrt{(6-3)^2 + (12-(-3))^2} + \sqrt{(9-6)^2 + (45-12)^2} + \sqrt{(12-9)^2 + (96-45)^2} \\ & = \sqrt{3^2 + (-3)^2} + \sqrt{3^2 + 15^2} + \sqrt{3^2 + 33^2} + \sqrt{3^2 + 51^2} \end{aligned}$$

[b] Use your calculator to find the length using the method in [a]. Round your answer to 4 decimal places.

$$d = \underline{103.7639} \quad (\text{corr to 4 d.p.})$$

[MULTIPLE CHOICE] Estimate the length of the curve $f(x) = x^3$ from $x = -1$ to $x = 5$ to four decimal places using 3 line segments (at equally spaced x -values).SCORE: 2 / 2 POINTS

[a] 126.5704

[b] 126.8031

[c] 126.9256

[d] 127.0337

LETTER OF CORRECT ANSWER: [C]

$$\begin{aligned} & (-1, -1) \\ & (1, 1) \\ & (3, 27) \\ & (5, 125) \end{aligned}$$