Math 114

Rational Expressions Review

Solve.

- [1] w varies directly as y and inversely as z. w = 12 when y = 8 and z = 5. Find the value of w when y = 6 and z = 15.
- [2] b varies directly as the square root of c. b = 12 when c = 16. Find the value of c when b = 18.
- [3] The height of a 1 liter water bottle varies inversely with the square of the radius of its base. A bottle with radius 5.4 cm is 11 cm tall. How tall is a bottle with radius 4.1 cm?
- [4] The cost of insuring a delivery varies jointly with the number of items in the delivery and the value of each item. It costs \$15 to insure a delivery of 25 items each valued at \$20 dollars. How much does it cost to insure a delivery of 3 items each valued at \$80?
- [5] **DELETED**

[6] **DELETED**

[7] **DELETED**

Write equations for the following problems, then solve.

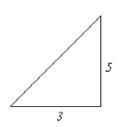
- [8] A number divided by twelve is equal to eight divided by three.
- [9] Five divided by four is equal to the sum of a number and seven divided by twelve.
- [10] A number divided by six is equal to the sum of that number and two divided by twelve.
- [11] A number divided by seven is equal to one divided by the sum of that number and six.

Write proportions for the following problems. YOU DO NOT NEED TO SOLVE THEM.

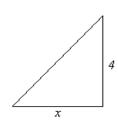
- [12] A car can travel 387 kilometers on 24 liters of gas. How far can it travel on 17 liters of gas?
- [13] A car can travel 185 kilometers on 13 liters of gas. How many liters of gas does it need to travel 243 kilometers?
- [14] On a blueprint, 3 centimeters represents 20 meters. What length on the blueprint represents 37 meters?
- [15] A music service charges \$17 for 19 downloads. How many downloads can be purchased for \$68?

Solve for x in the following similar triangles.

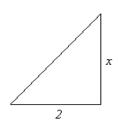
[16]

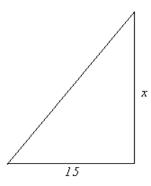


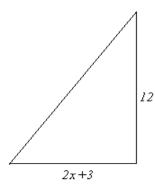
[17]

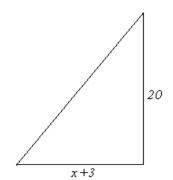


[18]









Simplify.

[19]
$$\frac{x^3 + 8x^2 - 48x}{3x^2 + 6x - 72}$$

$$\frac{x^3 + 8x^2 - 48x}{3x^2 + 6x - 72} \qquad [20] \qquad \frac{6x^2 - x - 1}{2x^2 + 9x - 5}$$

$$[21] \quad \frac{\frac{3}{x-2} - 2}{\frac{4}{x-2} + 1}$$

[22]
$$\frac{\frac{2}{x-3} - \frac{3}{x}}{\frac{5}{x-3} + \frac{2}{x}}$$

Perform the algebraic operations and simplify.

[23]
$$\frac{4x^2 - 1}{x^2 - 16} \cdot \frac{x^2 - 4x}{2x + 1}$$

[24]
$$\frac{2x^2 - x - 6}{3x^2 + 4x + 1} \cdot \frac{3x^2 + 7x + 2}{2x^2 + 7x + 6}$$

[25]
$$\frac{x^2 + 2x - 15}{x^2 + 3x - 10} \div \frac{x^2 - 9}{x^2 - 9x + 14}$$

[26]
$$\frac{9x^2 - 25}{2x - 2} \div \frac{6x - 10}{x^2 - 1}$$

[27]
$$\frac{x^2 - 5x}{2x - 8} + \frac{12 - 2x}{2x - 8}$$

[28]
$$\frac{2x^2 - x}{x^2 - 9} - \frac{x^2 + 12}{x^2 - 9}$$

[29]
$$\frac{x}{x+2} + \frac{2}{x-3}$$

[30]
$$\frac{x}{x+2} - \frac{6}{x^2 + x - 2}$$

[31]
$$\frac{x+1}{x^2-7x+6} - \frac{x-2}{x^2-4x-12}$$

Solve for x.

$$[32] \qquad \frac{x-1}{3} = \frac{x+3}{15}$$

[32]
$$\frac{x-1}{3} = \frac{x+3}{15}$$
 [33] $\frac{x-1}{3} = \frac{8}{x+4}$ [34] $\frac{3}{x} + \frac{10}{x^2} = 1$

$$[34] \qquad \frac{3}{x} + \frac{10}{x^2} = 1$$

[35] Find the equations of the horizontal and vertical asymptotes of
$$y = \frac{7-9x}{12x+8}$$
.

ANSWERS

[1]
$$w = 3$$

[2]
$$c = 36$$

[8]
$$\frac{x}{12} = \frac{8}{3}, x = 32$$

[9]
$$\frac{5}{4} = \frac{x+7}{12}, x = 8$$

[10]
$$\frac{x}{6} = \frac{x+2}{12}, x = \frac{x}{2}$$

[10]
$$\frac{x}{6} = \frac{x+2}{12}$$
, $x = 2$ [11] $\frac{x}{7} = \frac{1}{x+6}$, $x = 1$ or $x = -7$

$$[12] \qquad \frac{387}{24} = \frac{x}{17}$$

[13]
$$\frac{185}{13} = \frac{243}{x}$$
 [14]
$$\frac{3}{20} = \frac{x}{37}$$
 [15]

$$[14] \qquad \frac{3}{20} = \frac{x}{37}$$

[15]
$$\frac{17}{19} = \frac{68}{x}$$

[16]
$$x = 25$$

[17]
$$x = 3$$

[18]
$$x = 5$$

[19]
$$\frac{x(x+12)}{3(x+6)}$$

$$[20] \qquad \frac{3x+1}{x+5}$$

$$[21] \qquad \frac{7-2x}{x+2}$$

[22]
$$\frac{9-x}{7x-6}$$

[23]
$$\frac{x(2x-1)}{x+4}$$
[27]
$$\frac{x-3}{2}$$

$$[24] \qquad \frac{x-2}{x+1}$$

$$[21] \qquad \frac{7-2x}{x+2}$$

$$[25] \qquad \frac{x-7}{x+3}$$

[22]
$$\frac{9-x}{7x-6}$$
[26]
$$\frac{(3x+5)(x+1)}{4}$$

[27]
$$\frac{x-3}{2}$$

$$[28] \qquad \frac{x-4}{x-3}$$

$$[29] \qquad \overline{(x+2)(x-3)}$$

$$[30] \quad \frac{x-3}{x-1}$$

[31]
$$\frac{6x}{(x-1)(x-6)(x+2)}$$

[32]
$$x = 2$$

[33]
$$x = 4 \text{ or } x = -7$$

[34]
$$x = 5 \text{ or } x = -2$$

[28]
$$\frac{x+1}{x-3}$$
 [29] $\frac{x^2-x+4}{(x+2)(x-3)}$ [30] $\frac{x-3}{x-1}$ [32] $x=2$ [33] $x=4$ or $x=-7$ [34] $x=5$ or $x=-2$ [35] horizontal asymptote: $y=-\frac{3}{4}$, vertical asymptote: $x=-\frac{2}{3}$