

SCORE: _____ / 140 POINTS

- ALL PROBLEMS MUST BE SOLVED ALGEBRAICALLY TO EARN CREDIT (NO GUESS & CHECK)
- PUT A BOX AROUND EACH FINAL ANSWER
- SHOW COMPLETE AND PROPER WORK TO EARN FULL CREDIT

Solve: The cost of paper needed to wrap a cylinder varies directly as the weight of the cylinder and inversely as the radius. A cylinder weighing 15 ounces with a radius of 3 inches requires 12 cents of paper to wrap. Find the cost of paper needed to wrap a cylinder with a radius of 2 inches that weighs 20 ounces. **SCORE: ____ / 15 POINTS**

FOR FULL CREDIT, YOU MUST IDENTIFY WHAT ALL YOUR VARIABLES REPRESENT, FIND THE SPECIFIC EQUATION CONNECTING THEM, AND SUMMARIZE YOUR FINAL ANSWER IN A SENTENCE USING THE CORRECT UNITS OF MEASUREMENT.

C = cost of paper (cents)
 w = weight of cylinder (ounces)
 r = radius (inches)

$$C = \frac{kw}{r} \qquad C = \frac{12w}{5r}$$

$$12 = \frac{k(15)}{3} \qquad C = \frac{12(20)}{5(2)}$$

$$12 = 5k \qquad C = 24$$

$$\frac{12}{5} = k$$

It costs 24 cents to wrap the cylinder.

Subtract and simplify: $\frac{x+1}{x^2-8x+15} - \frac{x+3}{x^2-9x+18}$

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$$= \frac{x+1}{(x-3)(x-5)} - \frac{x+3}{(x-3)(x-6)}$$

$$= \frac{x+1}{(x-3)(x-5)} \cdot \frac{x-6}{x-6} - \frac{x+3}{(x-3)(x-6)} \cdot \frac{x-5}{x-5}$$

$$= \frac{x^2-5x-6-(x^2-2x-15)}{(x-3)(x-5)(x-6)}$$

$$= \frac{-3x+9}{(x-3)(x-5)(x-6)}$$

$$= \frac{-3(x-3)}{(x-3)(x-5)(x-6)}$$

$$= \frac{-3}{(x-5)(x-6)}$$

Solve:

A number divided by four is equal to fifteen divided by four less than that number.
Find the number. **CHECK YOUR ANSWER(S).**

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$$\frac{x}{4} = \frac{15}{x-4}$$

CHECK:

$$x = 10$$

$$x = -6$$

$$x^2 - 4x = 60$$

$$\frac{10}{4} = \frac{5}{2}$$

$$\frac{-6}{4} = -\frac{3}{2}$$

$$x^2 - 4x - 60 = 0$$

$$\frac{15}{6} = \frac{5}{2}$$

$$\frac{15}{-10} = -\frac{3}{2}$$

$$(x-10)(x+6) = 0$$

$$\boxed{x = 10 \text{ or } x = -6}$$

Find the equation of the vertical asymptote of $y = \frac{5+10x}{17x-11}$.

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$$17x - 11 = 0$$

$$\boxed{x = \frac{11}{17}}$$

Find the equation of the horizontal asymptote of $y = \frac{5+10x}{17x-11}$.

$$y \approx \frac{10x}{17x} \text{ for large values of } x$$

$$\boxed{y = \frac{10}{17}}$$

Simplify: $\frac{2x^2 + 5x - 3}{6x^2 + 11x - 21}$

SPECIFY ANY RESTRICTIONS.

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$$= \frac{(2x-1)(x+3)}{(6x-7)(x+3)}$$

$$= \boxed{\frac{2x-1}{6x-7}}$$

$$x+3 \neq 0$$

$$x \neq -3$$

Solve for x: $\frac{3}{x^2 - 7x + 10} - \frac{2}{x^2 - 8x + 15} = \frac{1}{x - 2}$ CHECK YOUR ANSWER(S)

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$$(x-2)(x-5)(x-3) \left[\frac{3}{(x-2)(x-5)} - \frac{2}{(x-3)(x-5)} \right] = \frac{1}{x-2} (x-2)(x-5)(x-3)$$

$$3(x-3) - 2(x-2) = (x-5)(x-3)$$

$$3x - 9 - 2x + 4 = x^2 - 8x + 15$$

$$x - 5 = x^2 - 8x + 15$$

$$0 = x^2 - 9x + 20$$

$$0 = (x-4)(x-5)$$

$$\boxed{x = 4} \text{ or } x = 5$$

CHECK: $x = 4$

$$\frac{3}{-2} - \frac{2}{-1} = -\frac{3}{2} + 2 = \frac{1}{2}$$

$x = 5$

$$\frac{3}{0} \text{ IS UNDEFINED}$$

Simplify: $\frac{1 - \frac{6}{x-5}}{\frac{3}{x-5} - \frac{4}{x-3}}$

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$$= \frac{1 - \frac{6}{x-5}}{\frac{3}{x-5} - \frac{4}{x-3}} \cdot \frac{(x-5)(x-3)}{(x-5)(x-3)}$$

$$= \frac{(x-5)(x-3) - 6(x-3)}{3(x-3) - 4(x-5)}$$

$$= \frac{x^2 - 8x + 15 - 6x + 18}{3x - 9 - 4x + 20}$$

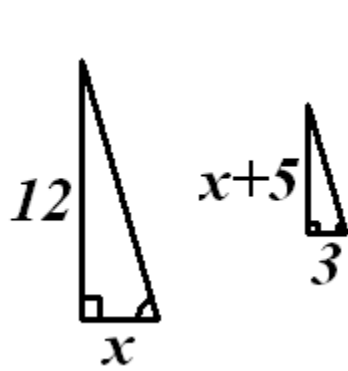
$$= \frac{x^2 - 14x + 33}{-x + 11}$$

$$= \frac{(x-11)(x-3)}{-(x-11)}$$

$$= \boxed{-(x-3) \text{ or } 3-x}$$

Solve for x in the following similar triangles:

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$$\frac{12}{x} = \frac{x+5}{3}$$

$$36 = x^2 + 5x$$

$$0 = x^2 + 5x - 36$$

$$0 = (x+9)(x-4)$$

$$x = -9 \text{ or } \boxed{x = 4}$$

Divide and simplify: $\frac{32x^2 - 18}{45x^2 - 30x^3} \div \frac{24x - 18}{10x^2 - 15x}$

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$$= \frac{2(16x^2 - 9)}{-15x^2(2x - 3)} \div \frac{6(4x - 3)}{5x(2x - 3)}$$

$$= \frac{2(4x + 3)(4x - 3)}{-15x^2(2x - 3)} \times \frac{5x(2x - 3)}{6(4x - 3)}$$

$$= \frac{4x + 3}{-3x} \times \frac{1}{3}$$

$$= \frac{4x + 3}{-9x}$$

$$= \boxed{-\frac{4x + 3}{9x}}$$

Subtract and simplify: $\frac{7x^2 - 5x - 2}{x^2 + x - 2} - \frac{5x^2 - 6x + 1}{x^2 + x - 2}$

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$$= \frac{2x^2 + x - 3}{x^2 + x - 2}$$

$$= \frac{(x-1)(2x+3)}{(x-1)(x+2)}$$

$$= \boxed{\frac{2x+3}{x+2}}$$