

SCORE: _____ / 140 POINTS

- ALL PROBLEMS MUST BE SOLVED ALGEBRAICALLY TO EARN CREDIT (NO GUESS & CHECK)
- PUT A BOX AROUND EACH FINAL ANSWER
- SHOW COMPLETE AND PROPER WORK TO EARN FULL CREDIT

Solve: The cost of paper needed to wrap a cylinder varies directly as the weight of the cylinder and inversely as the radius. A cylinder weighing 18 ounces with a radius of 2 inches requires 24 cents of paper to wrap. Find the cost of paper needed to wrap a cylinder with a radius of 4 inches that weighs 15 ounces. **SCORE: ____ / 15 POINTS**

FOR FULL CREDIT, YOU MUST IDENTIFY WHAT ALL YOUR VARIABLES REPRESENT, FIND THE SPECIFIC EQUATION CONNECTING THEM, AND SUMMARIZE YOUR FINAL ANSWER IN A SENTENCE USING THE CORRECT UNITS OF MEASUREMENT.

C = cost of paper (cents)
 w = weight of cylinder (ounces)
 r = radius (inches)

$$C = \frac{kw}{r} \qquad C = \frac{8w}{3r}$$

$$24 = \frac{k(18)}{2} \qquad C = \frac{8(15)}{3(4)}$$

$$24 = 9k \qquad C = 10$$

$$\frac{8}{3} = k$$

It costs 10 cents to wrap the cylinder.

Subtract and simplify: $\frac{x+3}{x^2-1} - \frac{x+6}{x^2-3x-4}$

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$$= \frac{x+3}{(x+1)(x-1)} - \frac{x+6}{(x+1)(x-4)}$$

$$= \frac{x+3}{(x+1)(x-1)} \frac{x-4}{x-4} - \frac{x+6}{(x+1)(x-4)} \frac{x-1}{x-1}$$

$$= \frac{x^2 - x - 12 - (x^2 + 5x - 6)}{(x+1)(x-1)(x-4)}$$

$$= \frac{-6x - 6}{(x+1)(x-1)(x-4)}$$

$$= \frac{-6(x+1)}{(x+1)(x-1)(x-4)}$$

$$= \frac{-6}{(x-1)(x-4)}$$

Solve:

A number divided by twelve is equal to four divided by two less than that number.
Find the number. **CHECK YOUR ANSWER(S).**

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$$\frac{x}{12} = \frac{4}{x-2}$$

CHECK:

$$x = 8$$

$$x = -6$$

$$x^2 - 2x = 48$$

$$\frac{8}{12} = \frac{2}{3}$$

$$\frac{-6}{12} = -\frac{1}{2}$$

$$x^2 - 2x - 48 = 0$$

$$\frac{4}{6} = \frac{2}{3}$$

$$\frac{4}{-8} = -\frac{1}{2}$$

$$(x-8)(x+6) = 0$$

$$\boxed{x = 8 \text{ or } x = -6}$$

Find the equation of the vertical asymptote of $y = \frac{5+11x}{17x-10}$.

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$$17x - 10 = 0$$

$$\boxed{x = \frac{10}{17}}$$

Find the equation of the horizontal asymptote of $y = \frac{5+11x}{17x-10}$.

$$y \approx \frac{11x}{17x} \text{ for large values of } x$$

$$\boxed{y = \frac{11}{17}}$$

Simplify: $\frac{2x^2 + 5x - 3}{6x^2 + 13x - 15}$

SPECIFY ANY RESTRICTIONS.

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$$= \frac{(2x-1)(x+3)}{(6x-5)(x+3)}$$

$$= \boxed{\frac{2x-1}{6x-5}}$$

$$x+3 \neq 0$$

$$x \neq -3$$

Solve for x: $\frac{3}{x^2 - x - 2} - \frac{4}{x^2 - 4} = \frac{1}{x + 1}$ CHECK YOUR ANSWER(S)

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$$(x-2)(x+1)(x+2) \left[\frac{3}{(x-2)(x+1)} - \frac{4}{(x-2)(x+2)} \right] = \frac{1}{x+1} (x-2)(x+1)(x+2)$$

$$3(x+2) - 4(x+1) = (x-2)(x+2)$$

$$3x + 6 - 4x - 4 = x^2 - 4$$

$$-x + 2 = x^2 - 4$$

$$0 = x^2 + x - 6$$

$$0 = (x+3)(x-2)$$

$$\boxed{x = -3} \text{ or } x = 2$$

CHECK:

$$x = -3$$

$$\frac{3}{10} - \frac{4}{5} = \frac{3}{10} - \frac{8}{10} = -\frac{5}{10} = -\frac{1}{2}$$

$$\frac{1}{-2} = -\frac{1}{2}$$

$$x = 2$$

$$\frac{3}{0} \text{ IS UNDEFINED}$$

Simplify: $\frac{1 - \frac{8}{x-6}}{\frac{2}{x-6} - \frac{3}{x-2}}$

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$$= \frac{1 - \frac{8}{x-6}}{\frac{2}{x-6} - \frac{3}{x-2}} \cdot \frac{(x-6)(x-2)}{(x-6)(x-2)}$$

$$= \frac{(x-6)(x-2) - 8(x-2)}{2(x-2) - 3(x-6)}$$

$$= \frac{x^2 - 8x + 12 - 8x + 16}{2x - 4 - 3x + 18}$$

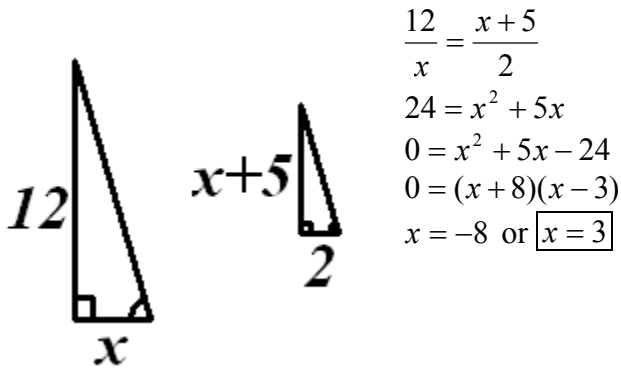
$$= \frac{x^2 - 16x + 28}{-x + 14}$$

$$= \frac{(x-14)(x-2)}{-(x-14)}$$

$$= \boxed{-(x-2) \text{ or } 2-x}$$

Solve for x in the following similar triangles:

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Divide and simplify: $\frac{27x^2 - 12}{50x^2 - 40x^3} \div \frac{27x + 18}{20x^2 - 25x}$

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$$= \frac{3(9x^2 - 4)}{-10x^2(4x - 5)} \div \frac{9(3x + 2)}{5x(4x - 5)}$$

$$= \frac{3(3x + 2)(3x - 2)}{-10x^2(4x - 5)} \times \frac{5x(4x - 5)}{9(3x + 2)}$$

$$= \frac{3x - 2}{-2x} \times \frac{1}{3}$$

$$= \frac{3x - 2}{-6x}$$

$$= \boxed{-\frac{(3x - 2)}{6x} \text{ or } \frac{2 - 3x}{6x}}$$

Subtract and simplify: $\frac{7x^2 - 9x - 5}{x^2 - x - 6} - \frac{5x^2 - 6x + 4}{x^2 - x - 6}$

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$$= \frac{2x^2 - 3x - 9}{x^2 - x - 6}$$

$$= \frac{(x - 3)(2x + 3)}{(x - 3)(x + 2)}$$

$$= \boxed{\frac{2x + 3}{x + 2}}$$