| Math 114 (7:30am - 8:20am) |
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| Midterm 2 Version N |
| Wed Nov 9, 2011 |

Name you asked to be called:

SCORE: _____/ 140 POINTS

- **▶** YOU MUST SHOW LOGICAL, NEAT AND ORGANIZED WORK TO EARN FULL CREDIT (NO GUESS & CHECK)
- **▶** IT MUST BE CLEAR HOW YOU ARRIVED AT YOUR ANSWER
- **▶** PUT A BOX AROUND YOUR FINAL ANSWER
- **→** ALL FINAL ANSWERS WHICH ARE RADICALS MUST BE SIMPLIFIED
- **→** ALL FRACTIONS MUST BE IN SIMPLEST FORM

Find the distance between the points (1, -3) and (-2, -9). Write your final answer using radicals.

SCORE: ___ / 6 POINTS

$$\sqrt{(-2-1)^2 + (-9-(-3))^2} = \sqrt{(-3)^2 + (-6)^2} = \sqrt{9+36} = \sqrt{45} = 3\sqrt{5}$$

Divide. Rationalize the denominator and simplify.

$$\frac{\sqrt{21}}{\sqrt{56x}}$$

$$= \frac{\sqrt{7}\sqrt{3}}{\sqrt{7}\sqrt{8x}} = \frac{\sqrt{3}}{\sqrt{8x}} = \frac{\sqrt{3}}{2\sqrt{2x}} = \frac{\sqrt{3}}{2\sqrt{2x}}\frac{\sqrt{2x}}{\sqrt{2x}} = \frac{\sqrt{6x}}{4x}$$

Translate the following sentence into an absolute value equation or inequality.

SCORE: ___ / 6 POINTS

"x is no less than 9 away from 5"

The distance between x and 5 is greater than or equal to 9

$$|x-5| \ge 9$$

If
$$f(x) = 2x^2 - 6x - 5$$
, find $f(a-3)$.

$$2(a-3)^2-6(a-3)-5$$

$$= 2(a^2 - 6a + 9) - 6a + 18 - 5$$

$$= 2a^2 - 12a + 18 - 6a + 18 - 5$$

$$= 2a^2 - 18a + 31$$

Check your answer.

$$-|9-3x| = -3$$

 $|9-3x| = 3$
 $9-3x = 3$ OR $9-3x = -3$
 $-3x = -6$ OR $-3x = -12$
 $x = 2$ OR $x = 4$

CHECK:

$$5 - |9 - 3(4)| = 5 - |9 - 12| = 5 - |-3| = 5 - 3 = 2$$

Solve the equation $13 - 4\sqrt{1 - h} = 5$ using algebra. Check your answer(s).

$$-4\sqrt{1-h} = -8$$

$$\sqrt{1-h} = 2$$

$$1-h=4$$

$$-h=3$$

$$h=-3$$

CHECK:

$$13 - 4\sqrt{1 - (-3)} = 13 - 4\sqrt{4} = 13 - 4(2) = 13 - 8 = 5$$

Solve the equation $m + \sqrt{7 - 2m} = 2$ using algebra. Check your answer(s).

SCORE: ___ / 12 POINTS

$$\sqrt{7-2m} = 2-m$$

$$7-2m = (2-m)^2$$

$$7-2m = 4-4m+m^2$$

$$0 = m^2 - 2m - 3$$

$$0 = (m-3)(m+1)$$

$$m = 3 \text{ OR } m = -1$$

$$\text{CHECK:}$$

$$m = 3$$

$$3 + \sqrt{7-2(3)} = 3 + \sqrt{7-6} = 3 + \sqrt{1} = 3 + 1 = 4$$

$$3+\sqrt{7-2(3)} = 3+\sqrt{7-6} = 3+\sqrt{1} = 3+1 = 4$$

 $m=-1$
 $-1+\sqrt{7-2(-1)} = -1+\sqrt{7+2} = -1+\sqrt{9} = -1+3 = 2$

Solve
$$|11 - 2x| \ge 3$$
.

SCORE: ___/ 10 POINTS

The distance between 11 and
$$2x$$
 is greater than or equal to 3 $2x \le 8$ OR $2x \ge 14$ $x \le 4$ OR $x \ge 7$

OR
$$11-2x \le -3 \text{ OR } 11-2x \ge 3$$

 $-2x \le -14 \text{ OR } -2x \ge -8$
 $x \ge 7 \text{ OR } x \le 4$

Write using fractional and/or negative exponents (where applicable).

SCORE: ___/8 POINTS

[a]
$$(\sqrt[3]{n})^8 = n^{\frac{8}{3}}$$

$$[b] \qquad \sqrt{b^9} = b^{\frac{9}{2}}$$

[c]
$$\frac{1}{\sqrt[6]{n^{24}}} = n^{-\frac{24}{6}} = n^{-4}$$

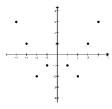
Find the equation of the circle with center (25, -1) and radius 4.

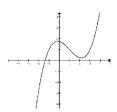
SCORE: ___/ 6 POINTS

$$(x-25)^2 + (y-(-1))^2 = 4^2$$
$$(x-25)^2 + (y+1)^2 = 16$$

Circle the \underline{two} graphs below that represent functions.

SCORE: ___ / 6 POINTS





Simplify $\sqrt{56r^9a^{16}v^{11}}$. Write your final answer using radicals.

SCORE: ____ / 6 POINTS

$$2r^4a^8v^5\sqrt{14rv}$$

Simplify $\sqrt{504}$.

SCORE: ___/ 6 POINTS

$$504 = 2 \times 2 \times 2 \times 3 \times 3 \times 7$$
$$\sqrt{504} = 2 \times 3\sqrt{2 \times 7} = 6\sqrt{14}$$

$$x^{2} - 10x + y^{2} + 18y = -42$$

$$x^{2} - 10x + 25 + y^{2} + 18y + 81 = -42 + 25 + 81$$

$$(x - 5)^{2} + (y + 9)^{2} = 64$$

$$CENTER = (5, -9)$$

RADIUS = 8

Perform the indicated operations and simplify. Write your final answers using radicals.

SCORE: ___/ 14 POINTS

[a]
$$\sqrt{6g^{11}} \sqrt{21g^9}$$
$$= \sqrt{126g^{20}}$$
$$= 3g^{10} \sqrt{14}$$

[b]
$$(\sqrt{5} + 4\sqrt{2})(3\sqrt{6} - \sqrt{15})$$

$$= 3\sqrt{30} - \sqrt{75} + 12\sqrt{12} - 4\sqrt{30}$$

$$= 3\sqrt{30} - 5\sqrt{3} + 12(2\sqrt{3}) - 4\sqrt{30}$$

$$= -5\sqrt{3} + 24\sqrt{3} - \sqrt{30}$$

$$= 19\sqrt{3} - \sqrt{30}$$

Perform the indicated operations and simplify. Write your final answers using fractional exponents.

SCORE: ___/8 POINTS

[a]
$$\frac{\sqrt[6]{w}}{\sqrt[10]{w}}$$

$$=\frac{w^{\frac{1}{6}}}{w^{\frac{1}{10}}}$$

$$=w^{\frac{1}{6}\frac{1}{10}}$$

$$=w^{\frac{1}{15}}$$

[b]
$$k^6 k^{\frac{3}{8}}$$

$$=k^{\frac{6+\frac{3}{8}}}$$

$$=k^{\frac{51}{8}}$$

Rationalize the denominator and simplify.

SCORE: ___ / 12 POINTS

$$[a] \qquad \frac{14}{5\sqrt{21}}$$

$$= \frac{14}{5\sqrt{21}} \frac{\sqrt{21}}{\sqrt{21}}$$

$$= \frac{14\sqrt{21}}{5(21)}$$

$$= \frac{2\sqrt{21}}{5(3)} = \frac{2\sqrt{21}}{15}$$

[b]
$$\frac{15}{7 + \sqrt{13}}$$

$$= \frac{15}{7 + \sqrt{13}} \frac{7 - \sqrt{13}}{7 - \sqrt{13}}$$

$$= \frac{15(7 - \sqrt{13})}{49 - 13}$$

$$= \frac{15(7 - \sqrt{13})}{36} = \frac{5(7 - \sqrt{13})}{12}$$