

SCORE: \_\_\_\_ / 6 POINTS

Give the name of the law that justifies each step in the following proof that if  $B$  is a Boolean algebra with operations  $+$  and  $\cdot$ , then for all  $a \in B$ ,  $a + a = a$ .

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PROOF: Let  $a$  be any element of  $B$ .

$$a + a$$

$$= (a + a) \cdot 1$$

LAW: IDENTITY

$$= (a + a) \cdot (a + \bar{a})$$

LAW: COMPLEMENT

$$= a + a \cdot \bar{a}$$

LAW: DISTRIBUTIVE

$$= a + 0$$

LAW: COMPLEMENT

$$= a$$

LAW: IDENTITY

Determine if the following statement is true or false.

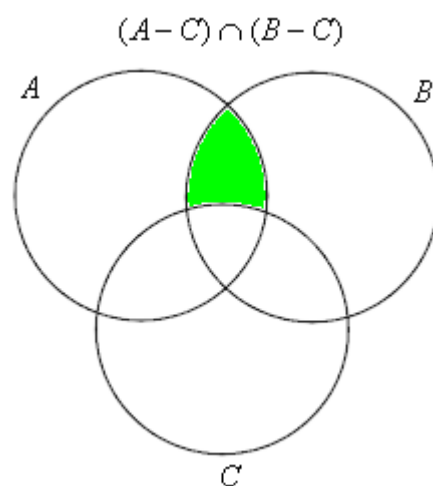
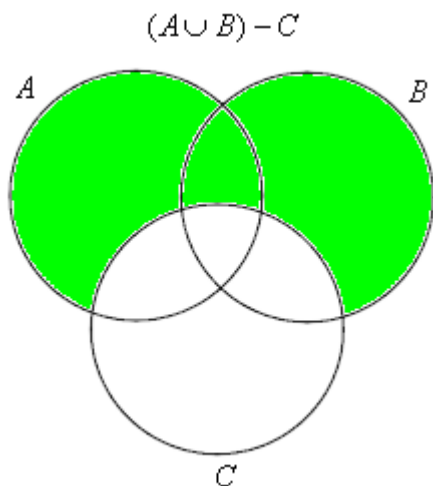
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If it is true, prove the statement using set algebra/identities. If it is false, disprove the statement.

**You may use Venn diagrams to help you determine whether the statement is true or false, but that will not be enough to earn points.**

For all sets  $A, B, C$  which are subsets of a universal set  $U$ ,

$$(A \cup B) - C = (A - C) \cap (B - C)$$



FALSE.

If  $A = \{1\}$  and  $B = C = \emptyset$ ,

$$\text{then } (A \cup B) - C = (\{1\} \cup \emptyset) - \emptyset = \{1\} - \emptyset = \{1\}$$

$$\text{but } (A - C) \cap (B - C) = (\{1\} - \emptyset) \cap (\emptyset - \emptyset) = \{1\} \cap \emptyset = \emptyset$$