

SCORE: \_\_\_\_ / 30 POINTS

**NO CALCULATORS ALLOWED**

**SHOW PROPER ALGEBRAIC WORK  
 USE PROPER NOTATION & SIMPLIFY ALL ANSWERS WHERE REASONABLE**

**MULTIPLE CHOICE: CIRCLE THE CORRECT ANSWER**

SCORE: \_\_\_\_ / 3 POINTS

A 5 foot long chain weighing 16 pounds hangs from a hook in the ceiling of an 11 foot tall room. (So, the bottom of the chain is 6 feet from the floor.) How many foot-pounds of work are done lifting the bottom loop of the chain to the ceiling so that it touches the top loop ?

(HINT: Draw "before" and "after" diagrams.)

- [a] 25 [b] 10 [c] 20 [d] 30 [e] 15

A 50 foot chain weighing 4 pounds per foot hangs over the edge of a 50 foot tall building. The chain is used to lift a 25 pound tabletop from ground level to a window 20 feet above ground.

SCORE: \_\_\_\_ / 6 POINTS

Write, **BUT DO NOT EVALUATE**, an expression involving an integral (or sum of integrals) for the work done.

SEE 7:30 VERSION 8

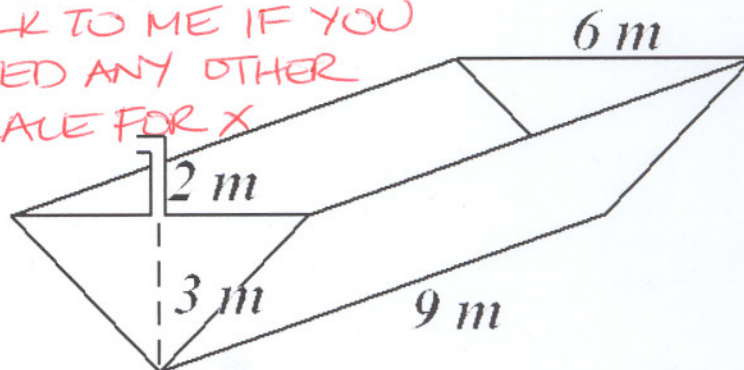
A tank in the shape of the triangular prism shown on the right is filled with water.

SCORE: \_\_\_\_ / 6 POINTS

Write, **BUT DO NOT EVALUATE**, an integral for the work required to pump the water out of the spout.

IF  $x=0$  IS BOTTOM OF TANK  
 AND  $x=3$  IS TOP OF TANK  
 AND  $x=5$  IS TOP OF SPOUT

TALK TO ME IF YOU  
 USED ANY OTHER  
 SCALE FOR  $x$



$$\int_0^3 (9.8)(1000) \left( 9 \left( 2x \right) \right) (5-x) dx$$

OR

IF  $x=0$  IS TOP OF TANK  
 AND  $x=3$  IS BOTTOM OF TANK  
 AND  $x=-2$  IS TOP OF SPOUT

IF  $x=0$  IS TOP OF SPOUT

AND  $x=2$  IS TOP OF TANK  
 AND  $x=5$  IS BOTTOM OF TANK

$$\int_{-2}^3 (9.8)(1000) \left( 9 (6-2x) \right) (x+2) dx$$

$$\int_2^5 (9.8)(1000) \left( 9 (10-2x) \right) (x) dx$$

The region bounded by  $x = 1$ ,  $y = \ln x$  and  $y = 1$  is revolved around the  $y$ -axis.  
Find the volume of the solid.

SCORE: \_\_\_\_ / 6 POINTS

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The region bounded by  $y = -2$ ,  $y = \frac{1}{2}x - 1$  and  $y = x - 2$  is revolved around the line  $y = 1$ .

SCORE: \_\_\_\_ / 9 POINTS

[a] Write, **BUT DO NOT EVALUATE**, an integral (or sum of integrals) for the volume of the solid using the shell method.

SEE 7:30 VERSION 8

[b] Write, **BUT DO NOT EVALUATE**, an integral (or sum of integrals) for the volume of the solid using the washer method.

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[c] Find the volume of the solid by evaluating the appropriate integral(s) from either [a] or [b].

SEE 7:30 VERSION 8