

SCORE: ____ / 20 POINTS

**UNLESS STATED OTHERWISE
 WRITE DOWN THE CALCULATIONS USED TO FIND YOUR ANSWERS**

To find $\lim_{x \rightarrow -6^+} p(x)$, name 3 values of x for which you might want to know the value of $p(x)$.

SCORE: ____ / 2 POINTS

$-5.9, -5.99, -5.999$

Some values for a function f are given in the table below.

SCORE: ____ / 4 POINTS

x	-5	-3	-1	1	3	5
$f(x)$	13	5	2	-2	-11	-7

[a] Estimate the slope of the tangent line to $y = f(x)$ at $x = -3$ by finding and averaging the slope of 2 appropriate secant lines.

$$m_1 = \frac{13-5}{-5-3} = -4$$

$$m_2 = \frac{2-5}{-1-3} = -\frac{3}{2}$$

$$\frac{1}{2}(-4 + -\frac{3}{2}) = -\frac{11}{4}$$

$\frac{1}{2}$ POINT EACH

[b] Do you think your estimate in [a] would be close to the actual slope of the tangent line? Why or why not?

NO. -5 AND -1 ARE NOT VERY CLOSE TO -3.

The position of an object travelling along a straight line is given by $s(t) = \sqrt{t+1}$.

SCORE: ____ / 2 POINTS

Find the average velocity of the object for the time period beginning when $t = 3$ and lasting 0.2 second.

Round your answer to 3 decimal places.

$$\frac{\sqrt{3.2+1} - \sqrt{3+1}}{3.2-3} = \frac{\sqrt{4.2} - 2}{3.2-3} \approx 0.247$$

OR

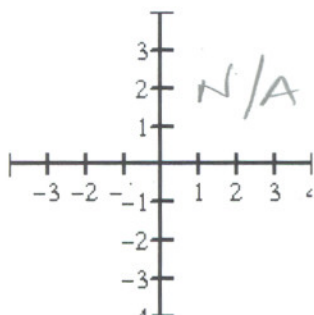


Sketch the graphs of functions that satisfy the following conditions, or write N/A if no such functions exist.

SCORE: ___ / 3 POINTS

$$\lim_{x \rightarrow -3^-} f(x) = -1,$$

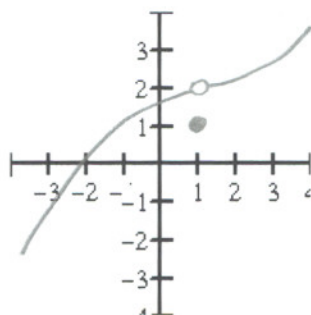
$$\lim_{x \rightarrow -3^+} f(x) = 1$$



$$g(1) \text{ exists,}$$

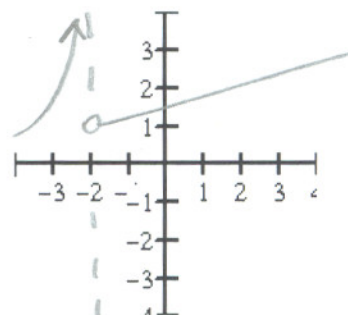
$$\lim_{x \rightarrow 1} g(x) \text{ exists,}$$

$$\lim_{x \rightarrow 1} g(x) \neq g(1)$$



$$\lim_{x \rightarrow -2^+} h(x) = 1,$$

$$\lim_{x \rightarrow -2^-} h(x) = \infty$$



The point P lies on the curve $y = \frac{x^3}{1+x}$. The x -coordinate of P is 1.

SCORE: ___ / 5 POINTS

- [a] If Q is the point $(x, \frac{x^3}{1+x})$, use your calculator to find the slope of the secant line PQ (correct to 3 decimal places) for the following values of x . You do NOT need to write down the calculations you used. 1/2 POINT EACH

x	0.8	0.98	0.998	1.002	1.02	1.2
slope of secant line	1.078	1.233	1.248	1.252	1.268	1.427

- [b] Using the results of part (a) (and any additional values), guess the value of the slope of the tangent line to the curve at P .

1.25

- [c] Using the slope from part (b), find an equation of the tangent line to the curve at P .

AT $x=1, y=\frac{1}{2}$

OR
 $y - \frac{1}{2} = 1.25(x - 1)$ or $y = 1.25x - 0.75$

FILL IN THE BLANKS. The graph of a function f is shown on the right.

State the values of the following expressions, if they exist. Write DNE where appropriate.

You do NOT need to show work.

[a] $\lim_{x \rightarrow -2} f(x) = 3$

[e] $f(2) = 1$

[b] $\lim_{x \rightarrow 2} f(x) = -1$

[f] $\lim_{x \rightarrow -1} f(x) = 2$

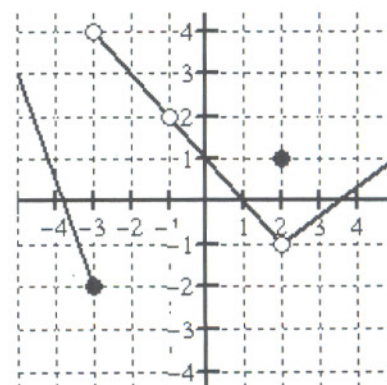
[c] $f(-1) = \text{DNE}$

[g] $\lim_{x \rightarrow -3} f(x) = \text{DNE}$

[d] $\lim_{x \rightarrow -3^+} f(x) = 4$

[h] $f(-3) = -2$

SCORE: ___ / 4 POINTS



1/2 POINT EACH