

SCORE: ____ / 20 POINTS

**UNLESS STATED OTHERWISE
 WRITE DOWN THE CALCULATIONS USED TO FIND YOUR ANSWERS**

To find $\lim_{x \rightarrow -4^+} p(x)$, name 3 values of x for which you might want to know the value of $p(x)$.

SCORE: ____ / 2 POINTS

$-3.9, -3.99, -3.999$

Some values for a function f are given in the table below.

SCORE: ____ / 4 POINTS

x	-5	-3	-1	1	3	5
$f(x)$	13	5	2	-2	-11	-7

[a] Estimate the slope of the tangent line to $y = f(x)$ at $x = 1$ by finding and averaging the slope of 2 appropriate secant lines.

$$m_1 = \frac{2 - (-2)}{-1 - 1} = -2$$

$$m_2 = \frac{-11 - (-2)}{3 - 1} = -\frac{9}{2}$$

$\frac{1}{2}$ POINT EACH

$$\frac{1}{2}(-2 + -\frac{9}{2}) = -\frac{13}{4}$$

[b] Do you think your estimate in [a] would be close to the actual slope of the tangent line? Why or why not?

NO. -1 AND 3 ARE NOT VERY CLOSE TO 1.
 $\frac{1}{2}$ $\frac{1}{2}$

The position of an object travelling along a straight line is given by $s(t) = \sqrt{t-2}$.

SCORE: ____ / 2 POINTS

Find the average velocity of the object for the time period beginning when $t = 3$ and lasting 0.1 second.
Round your answer to 3 decimal places.

$$\frac{\sqrt{3.1-2} - \sqrt{3-2}}{3.1-3} = \frac{\sqrt{1.1} - 1}{3.1-3} \approx 0.488$$

OR



Sketch the graphs of functions that satisfy the following conditions, or write N/A if no such functions exist.

SCORE: ___ / 3 POINTS

$$f(-1) \text{ exists,}$$

$$\lim_{x \rightarrow 2^-} g(x) = -1,$$

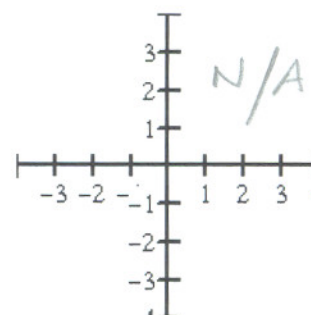
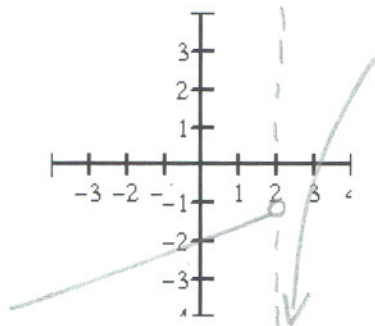
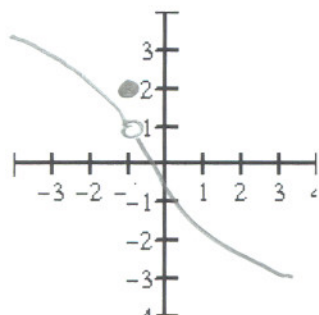
$$\lim_{x \rightarrow -3^-} h(x) = -1,$$

$$\lim_{x \rightarrow -1} f(x) \text{ exists,}$$

$$\lim_{x \rightarrow 2^+} g(x) = -\infty$$

$$\lim_{x \rightarrow -3} h(x) = 1$$

$$\lim_{x \rightarrow -1} f(x) \neq f(-1)$$



The point P lies on the curve $y = \frac{x^3}{1+x}$. The x -coordinate of P is 1.

SCORE: ___ / 5 POINTS

- [a] If Q is the point $(x, \frac{x^3}{1+x})$, use your calculator to find the slope of the secant line PQ (correct to 3 decimal places) for the following values of x . You do NOT need to write down the calculations you used.

$\frac{1}{2}$ POINT EACH

x	0.7	0.97	0.997	1.003	1.03	1.3
slope of secant line	0.994	1.224	1.247	1.253	1.276	1.517

- [b] Using the results of part (a) (and any additional values), guess the value of the slope of the tangent line to the curve at P .

1.25

OR

- [c] Using the slope from part (b), find an equation of the tangent line to the curve at P .

AT $x=1, y=\frac{1}{2}$

$y - \frac{1}{2} = 1.25(x - 1)$ OR $y = 1.25x - 0.75$

FILL IN THE BLANKS. The graph of a function f is shown on the right.

SCORE: ___ / 4 POINTS

State the values of the following expressions, if they exist. Write DNE where appropriate.

You do NOT need to show work.

[a] $f(3) =$

2

[e] $\lim_{x \rightarrow 3^-} f(x) =$

-4

[b] $\lim_{x \rightarrow 3} f(x) =$

DNE

[f] $f(1) =$

DNE

[c] $\lim_{x \rightarrow 1} f(x) =$

-2

[g] $\lim_{x \rightarrow -2} f(x) =$

1

[d] $f(-2) =$

-1

[h] $\lim_{x \rightarrow 2} f(x) =$

-3

$\frac{1}{2}$ POINT EACH

