

SCORE: \_\_\_\_ / 20 POINTS

**UNLESS STATED OTHERWISE  
 WRITE DOWN THE CALCULATIONS USED TO FIND YOUR ANSWERS**

To find  $\lim_{x \rightarrow -7^+} p(x)$ , name 3 values of  $x$  for which you might want to know the value of  $p(x)$ .

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$-6.9, -6.99, -6.999$

Some values for a function  $f$  are given in the table below.

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$x$	-5	-3	-1	1	3	5
$f(x)$	13	5	2	-2	-11	-7

[a] Estimate the slope of the tangent line to  $y = f(x)$  at  $x = -1$  by finding and averaging the slope of 2 appropriate secant lines.

$$m_1 = \frac{5-2}{-3-(-1)} = -\frac{3}{2}$$

$$m_2 = \frac{-2-2}{1-(-1)} = -2$$

$$\frac{1}{2} \left( -\frac{3}{2} + -2 \right) = -\frac{7}{4}$$

$\frac{1}{2}$  POINT EACH

[b] Do you think your estimate in [a] would be close to the actual slope of the tangent line? Why or why not?

NO.  $-3$  AND  $1$  ARE NOT VERY CLOSE TO  $-1$ .

$\frac{1}{2}$   $\frac{1}{2}$

The position of an object travelling along a straight line is given by  $s(t) = \sqrt{t-2}$ .

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Find the average velocity of the object for the time period beginning when  $t = 3$  and lasting 0.2 second.

Round your answer to 3 decimal places.

$$\frac{\sqrt{3.2-2} - \sqrt{3-2}}{3.2-3} = \frac{\sqrt{1.2}-1}{3.2-3} \approx 0.477$$

OR



Sketch the graphs of functions that satisfy the following conditions, or write N/A if no such functions exist.

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$f(1)$  exists,

$\lim_{x \rightarrow -2^+} g(x) = 1$ ,

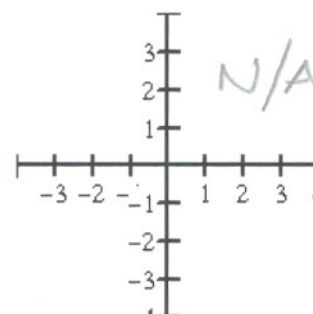
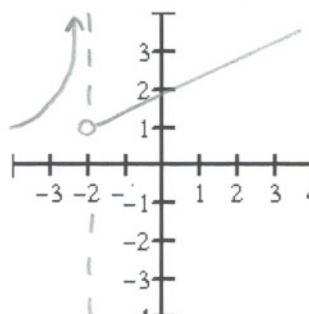
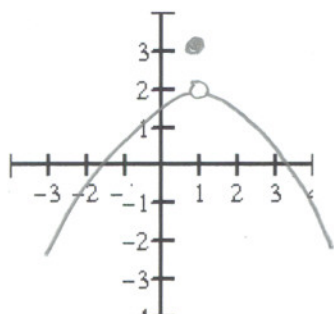
$\lim_{x \rightarrow -3^-} h(x) = -1$ ,

$\lim_{x \rightarrow 1} f(x)$  exists,

$\lim_{x \rightarrow -2^-} g(x) = \infty$

$\lim_{x \rightarrow -3} h(x) = 1$

$\lim_{x \rightarrow 1} f(x) \neq f(1)$



The point  $P$  lies on the curve  $y = \frac{x^3}{1+x}$ . The  $x$ -coordinate of  $P$  is  $-2$ .

SCORE: \_\_\_ / 5 POINTS

- [a] If  $Q$  is the point  $(x, \frac{x^3}{1+x})$ , use your calculator to find the slope of the secant line  $PQ$  (correct to 3 decimal places) for the following values of  $x$ . You do NOT need to write down the calculations you used.

$\frac{1}{2}$  POINT EACH

$x$	-1.8	-1.98	-1.998	-2.002	-2.02	-2.2
slope of secant line	-3.550	-3.960	-3.996	-4.004	-4.040	-4.367

- [b] Using the results of part (a) (and any additional values), guess the value of the slope of the tangent line to the curve at  $P$ .

$-4$

- [c] Using the slope from part (b), find an equation of the tangent line to the curve at  $P$ .

AT  $x = -2, y = 8$

$y - 8 = -4(x + 2)$  or  $y = -4x$

**FILL IN THE BLANKS.** The graph of a function  $f$  is shown on the right.

SCORE: \_\_\_ / 4 POINTS

State the values of the following expressions, if they exist. Write DNE where appropriate.

You do NOT need to show work.

[a]  $f(-3) = -2$

[e]  $\lim_{x \rightarrow -3^+} f(x) = 4$

[b]  $\lim_{x \rightarrow -3} f(x) = \text{DNE}$

[f]  $f(-1) = \text{DNE}$

[c]  $\lim_{x \rightarrow -1} f(x) = 2$

[g]  $\lim_{x \rightarrow 2} f(x) = -1$

[d]  $f(2) = 1$

[h]  $\lim_{x \rightarrow -2} f(x) = 3$

$\frac{1}{2}$  POINT EACH

