

SCORE: ____ / 20 POINTS

**UNLESS STATED OTHERWISE
 WRITE DOWN THE CALCULATIONS USED TO FIND YOUR ANSWERS**

To find $\lim_{x \rightarrow -5^+} p(x)$, name 3 values of x for which you might want to know the value of $p(x)$.

SCORE: ____ / 2 POINTS

$-4.9, -4.99, -4.999$

Some values for a function f are given in the table below.

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x	-5	-3	-1	1	3	5
$f(x)$	13	5	2	-2	-11	-7

[a] Estimate the slope of the tangent line to $y = f(x)$ at $x = 3$ by finding and averaging the slope of 2 appropriate secant lines.

$$m_1 = \frac{-2 - (-11)}{1 - 3} = -\frac{9}{2}$$

$$m_2 = \frac{-7 - (-11)}{5 - 3} = 2$$

$\frac{1}{2}$ POINT EACH

$$\frac{1}{2} \left(-\frac{9}{2} + 2 \right) = -\frac{5}{4}$$

[b] Do you think your estimate in [a] would be close to the actual slope of the tangent line? Why or why not?

NO 1 AND 5 ARE NOT VERY CLOSE TO 3.

$\frac{1}{2}$

$\frac{1}{2}$

The position of an object travelling along a straight line is given by $s(t) = \sqrt{t+1}$.

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Find the average velocity of the object for the time period beginning when $t = 3$ and lasting 0.1 second.

Round your answer to 3 decimal places.

$$\frac{\sqrt{3.1+1} - \sqrt{3+1}}{3.1 - 3} = \frac{\sqrt{4.1} - 2}{3.1 - 3} \approx 0.248$$

OR



Sketch the graphs of functions that satisfy the following conditions, or write N/A if no such functions exist.

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$$\lim_{x \rightarrow -3^-} f(x) = -1,$$

$$\lim_{x \rightarrow -3} f(x) = 1$$

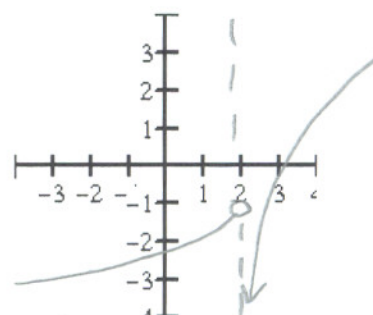
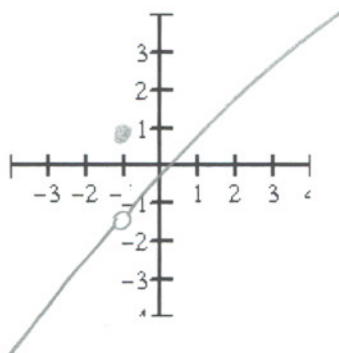
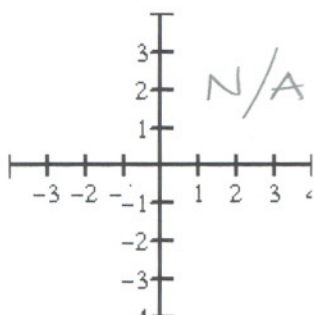
$$g(-1) \text{ exists,}$$

$$\lim_{x \rightarrow -1} g(x) \text{ exists,}$$

$$\lim_{x \rightarrow -1} g(x) \neq g(-1)$$

$$\lim_{x \rightarrow 2^-} h(x) = -1,$$

$$\lim_{x \rightarrow 2^+} h(x) = -\infty$$



The point P lies on the curve $y = \frac{x^3}{1+x}$. The x -coordinate of P is -2 .

SCORE: ___ / 5 POINTS

- [a] If Q is the point $(x, \frac{x^3}{1+x})$, use your calculator to find the slope of the secant line PQ (correct to 3 decimal places) for the following values of x . You do NOT need to write down the calculations you used.

$\frac{1}{2}$ POINT EACH

x	-1.7	-1.97	-1.997	-2.003	-2.03	-2.3
slope of secant line	-3.271	-3.939	-3.994	-4.006	-4.059	-4.531

- [b] Using the results of part (a) (and any additional values), guess the value of the slope of the tangent line to the curve at P .

-4

- [c] Using the slope from part (b), find an equation of the tangent line to the curve at P .

AT $x = -2, y = 8$

$y - 8 = -4(x + 2)$ OR $y = -4x$

FILL IN THE BLANKS. The graph of a function f is shown on the right.

SCORE: ___ / 4 POINTS

State the values of the following expressions, if they exist. Write DNE where appropriate.

You do NOT need to show work.

[a] $\lim_{x \rightarrow 2} f(x) =$

-3

[e] $f(-2) =$

-1

[b] $\lim_{x \rightarrow -2} f(x) =$

1

[f] $\lim_{x \rightarrow 1} f(x) =$

-2

[c] $f(1) =$

DNE

[g] $\lim_{x \rightarrow 3} f(x) =$

DNE

[d] $\lim_{x \rightarrow 3^-} f(x) =$

-4

[h] $f(3) =$

2

$\frac{1}{2}$ POINT EACH

