

SCORE: \_\_\_ / 20 POINTS

**UNLESS STATED OTHERWISE  
 WRITE DOWN THE CALCULATIONS USED TO FIND YOUR ANSWERS**

To find  $\lim_{x \rightarrow -5^-} p(x)$ , name 3 values of  $x$  for which you might want to know the value of  $p(x)$ .

SCORE: 0 / 2 POINTS

~~$x$~~   
~~-5.1~~  
~~-5.01~~  
~~-5.001~~

Some values for a function  $f$  are given in the table below.

SCORE: 4 / 4 POINTS

$x$	-5	-3	-1	1	3	5
$f(x)$	13	5	2	-2	-11	-7

[a] Estimate the slope of the tangent line to  $y = f(x)$  at  $x = 3$  by finding and averaging the slope of 2 appropriate secant lines.

$$\begin{aligned} \frac{-2 - (-11)}{1 - 3} &= \frac{9}{-2} = -\frac{9}{2} + 2 = -\frac{9}{2} + \frac{4}{2} \\ &= -\frac{5}{2} \div 2 = -\frac{5}{2} \cdot \frac{1}{2} \\ &= -\frac{5}{4} \text{ or } -1.25 \end{aligned}$$

$$\begin{aligned} \frac{-7 - (-11)}{5 - 3} &= \frac{4}{2} = 2 \end{aligned}$$

[b] Do you think your estimate in [a] would be close to the actual slope of the tangent line? Why or why not?

No, because the values I used for  $x$  are far away (2 units) from 3. If I had wanted a more accurate slope, I should've used numbers such as 3.001 or 2.999 for  $x$ .

The position of an object travelling along a straight line is given by  $s(t) = \sqrt{t+1}$ .

SCORE: \_\_\_ / 2 POINTS

Find the average velocity of the object for the time period beginning when  $t = 3$  and lasting 0.1 second.

Round your answer to 3 decimal places.

$$\begin{aligned} \frac{s(3+0.1) - s(3)}{(3+0.1) - 3} &= \frac{2.024846 - 2}{0.1} = \frac{0.024846}{0.1} \\ &= 0.248 \end{aligned}$$

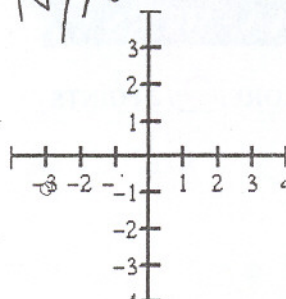
Sketch the graphs of functions that satisfy the following conditions, or write N/A if no such functions exist.

SCORE: 2 / 3 POINTS

$$\lim_{x \rightarrow -3^-} f(x) = -1,$$

$$\lim_{x \rightarrow -3} f(x) = 1$$

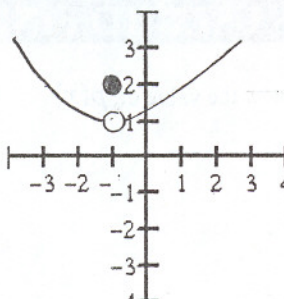
N/A



$$g(-1) \text{ exists,}$$

$$\lim_{x \rightarrow -1} g(x) \text{ exists,}$$

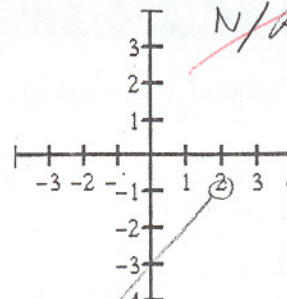
$$\lim_{x \rightarrow -1} g(x) \neq g(-1)$$



$$\lim_{x \rightarrow 2^-} h(x) = -1,$$

$$\lim_{x \rightarrow 2^+} h(x) = -\infty$$

N/A



The point  $P$  lies on the curve  $y = \frac{x^3}{1+x}$ . The  $x$ -coordinate of  $P$  is  $-2$ .

SCORE: 2 / 5 POINTS

- [a] If  $Q$  is the point  $(x, \frac{x^3}{1+x})$ , use your calculator to find the slope of the secant line  $PQ$  (correct to 3 decimal places) for the following values of  $x$ . You do NOT need to write down the calculations you used.

$x$	-1.7	-1.97	-1.997	-2.003	-2.03	-2.3
slope of secant line	-5.305	-5.016	-5.002	-4.999	-4.986	-4.939

- [b] Using the results of part (a) (and any additional values), guess the value of the slope of the tangent line to the curve at  $P$ .

$$\text{slope} = -5$$

- [c] Using the slope from part (b), find an equation of the tangent line to the curve at  $P$ .

$$\begin{aligned} -2 &= (-5)(-2) + b \\ -2 &= b \end{aligned} \quad \begin{aligned} y &= -5x - 2 \\ \text{OR} \\ y + 2 &= -5x \end{aligned}$$

**FILL IN THE BLANKS.** The graph of a function  $f$  is shown on the right.

State the values of the following expressions, if they exist. Write DNE where appropriate.

You do NOT need to show work.

[a]  $\lim_{x \rightarrow 2} f(x) = \underline{\text{DNE}}$

[e]  $f(-2) = \underline{-1} \left] \frac{1}{2} \right.$

[b]  $\lim_{x \rightarrow -2} f(x) = \underline{\text{DNE}}$

[f]  $\lim_{x \rightarrow 1} f(x) = \underline{-2} \left] \frac{1}{2} \right.$

[c]  $f(1) = \underline{\text{DNE}} \left] \frac{1}{2} \right.$

[g]  $\lim_{x \rightarrow 3} f(x) = \underline{\text{DNE}} \left] \frac{1}{2} \right.$

[d]  $\lim_{x \rightarrow 3^-} f(x) = \underline{-4} \left] \frac{1}{2} \right.$

[h]  $f(3) = \underline{2} \left] \frac{1}{2} \right.$

SCORE: 3 / 4 POINTS

