

### **HINTS:**

**So, you're only looking at these hints because you tried really hard to solve the problems and got stuck. Right ?**

- [5] If you set  $\Delta x = \frac{\pi}{n}$ , you will need to factor the argument of the sine to get  $a + i\Delta x$  to appear. You can avoid that by setting  $\Delta x$  to a different value, but you have to make a slightly different change to compensate as well.
- [7] Use the properties of definite integrals, geometry, and the relationship between definite integrals and areas.
- [8] Consider the bounds on  $\sin x$  on the interval  $\left[\frac{\pi}{6}, \frac{\pi}{2}\right]$ .
- [10] Fundamental Theorem of Calculus Part 1 and many theorems and definitions from Math 1A (applications of derivatives).
- [11] Fundamental Theorem of Calculus Part 1, of course. But don't forget the chain and product rules. And substitute  $x = 1$  as soon as you get an expression for  $g''(x)$  (no need to simplify  $g''(x)$  first).
- [12] Differentiate both sides of the equation with respect to  $x$ .
- [14] Watch out for the change of sign in the velocity in part [b]. Use algebraic sign analysis on  $v(t)$ , like the algebraic sign analysis you did in Math 1A on  $f'(x)$  or  $f''(x)$  when you wanted to know where  $f(x)$  was increasing/decreasing or concave up/down.
- [15] Use  $u$ -substitution. And remember that the name of the variable in the integral is irrelevant in a definite integral.