Let $g(x) = \int_{S} f(t) dt$, where f is the function whose graph is shown on the right.

[a]

[b]

[c]



9'= f CHANGES FROM NEGATIVE TO POSITIVE AT X=2

Evaluate $\int_{0}^{1} \frac{1}{1-\sin x} dx$ by first multiplying the numerator and denominator of the integrand by $1 + \sin x$. SCORE: 5 PTS # (sec2x+secxtanx) dx = I-SMX ItSMX (tanx+secx)] = -Ja 1+ 5m X dx GIVE YOURSELF THIS I POINT -SKIPPED THUS. BUT GOT RIGHT FINAL ANSWER

If
$$f(x) = \int_{-\infty}^{\sinh x} \sqrt{1+t^2} dt$$
 and $g(y) = \int_{-\infty}^{y} f(x) dx$, find $g''(x)$.

For full credit, you must clearly show the use of all necessary properties of the definite integral.



SCORE:

4 PTS

Find the error in the logic below. HINT: It is NOT an arithmetic error.





SO FTC PART Z CAN'T BE USED

Find the following indefinite integrals.

SCORE: ____ / 8 PTS

[a]
$$\int \frac{6x^2 - 5}{\sqrt[3]{1 + 10x - 4x^3}} dx.$$

$$\underbrace{\bigcup = 1 + 10x - 4x^3}_{dx} = 10 - 12x^2$$

$$- \frac{1}{2} d \cup = (6x^2 - 5) d x$$

$$-\frac{1}{2} \int \frac{1}{\sqrt[3]{0}} d \cup (1)$$

$$= -\frac{1}{2} \cdot \frac{3}{2} \cup \frac{2}{3} + C$$

CAN BE SIMPLIFIED

$$= -\frac{3}{4} (1 + 10x - 4x^3)^3 + C$$

(1) (4)

[b] Find $\int \operatorname{csch}^2 x \operatorname{coth}^4 x \, dx$.

 $U = \operatorname{coth} X(I)$ $dv = -csch^2 x$ $-du = csch^2 x dx$ - (utdu -=- +C =- toth 5x+C

A town decided to build a scenic path from its tourist center to its rose garden. If C(l) = linear cost (in thousands SCORE: _____ / 2 PTS of dollars per meter) of building the part of the path l meters from the tourist center, explain the meaning of the equation $\int_{200}^{600} G(h) dh = 100$.

In your explanation, give the meaning and units of all numbers in the equation.

Answer the following questions about the definition of the definite integral as presented in lecture. SCORE: ____ / 3 PTS (Your answers may refer to the fact that the definite integral equals the area under a curve which is above the x - axis.)

[a] Why is there a limit (lim) in the definition and why does the index of the limit approach the value that it does? THE SUM OF THE AREAS OF THE RECTANCIES APPROACHES THE AREA UNDER THE CURVE AS EACH RECTANCIES APPROACHES AN NARROLLER AND THE NUMBER OF RECTANCIES APPROACHES AN (IE. Im.) What is the difference between using f(x;) and f(a + iΔx) in the definition? f(a+iΔx) USES ENDPOINTS OF EACH SUBINTERVAL TO DETERMINE HEIGHTS OF RECTANCIES; f(x*) USES ANY POINT IN EACH SUBINTERVAL