

Find the inverse of $\begin{bmatrix} 3 & 9 & 7 \\ -1 & -7 & -4 \\ 1 & 2 & 2 \end{bmatrix} \cdot \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} \quad R_1 \leftrightarrow R_3$

SCORE: ___ / 7 PTS

$$\left[\begin{array}{ccc|ccc} 1 & 2 & 2 & 0 & 0 & 1 \\ -1 & -7 & -4 & 0 & 1 & 0 \\ 3 & 9 & 7 & 1 & 0 & 0 \end{array} \right] \begin{array}{l} \\ R_2 + R_1 \\ R_3 + (-3)R_1 \end{array}$$

$$\left[\begin{array}{ccc|ccc} 1 & 2 & 2 & 0 & 0 & 1 \\ 0 & 1 & \frac{2}{5} & 0 & -\frac{1}{5} & -\frac{1}{5} \\ 0 & 0 & -\frac{1}{5} & 1 & \frac{2}{5} & -\frac{12}{5} \end{array} \right] -5R_3$$

$$\left[\begin{array}{ccc|ccc} 1 & 2 & 2 & 0 & 0 & 1 \\ 0 & -5 & -2 & 0 & 1 & 1 \\ 0 & 3 & 1 & 1 & 0 & -3 \end{array} \right] -\frac{1}{5}R_2$$

$$\left[\begin{array}{ccc|ccc} 1 & 2 & 2 & 0 & 0 & 1 \\ 0 & 1 & \frac{2}{5} & 0 & -\frac{1}{5} & -\frac{1}{5} \\ 0 & 0 & 1 & -5 & -3 & 12 \end{array} \right] \begin{array}{l} R_1 + (-2)R_3 \\ R_2 + (-\frac{2}{5})R_3 \\ \end{array}$$

$$\left[\begin{array}{ccc|ccc} 1 & 2 & 2 & 0 & 0 & 1 \\ 0 & 1 & \frac{2}{5} & 0 & -\frac{1}{5} & -\frac{1}{5} \\ 0 & 3 & 1 & 1 & 0 & -3 \end{array} \right] R_3 + (-3)R_2$$

$$\left[\begin{array}{ccc|ccc} 1 & 2 & 0 & 10 & 6 & -23 \\ 0 & 1 & 0 & 2 & 1 & -5 \\ 0 & 0 & 1 & -5 & -3 & 12 \end{array} \right] R_1 + (-2)R_2$$

$$\left[\begin{array}{ccc|ccc} 1 & 0 & 0 & 6 & 4 & -13 \\ 0 & 1 & 0 & 2 & 1 & -5 \\ 0 & 0 & 1 & -5 & -3 & 12 \end{array} \right]$$

Find and use an inverse matrix to solve the system

$$12x - 13y = 8$$

$$7x + 5y = -1$$

SCORE: ___ / 5 PTS

$$\begin{bmatrix} 12 & -13 \\ 7 & 5 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 8 \\ -1 \end{bmatrix}$$

$$\begin{bmatrix} x \\ y \end{bmatrix} = \frac{1}{60 - (-91)} \begin{bmatrix} 5 & 13 \\ -7 & 12 \end{bmatrix} \begin{bmatrix} 8 \\ -1 \end{bmatrix}$$

$$= \frac{1}{151} \begin{bmatrix} 40 - 13 \\ -56 - 12 \end{bmatrix}$$

$$= \begin{bmatrix} \frac{27}{151} \\ \frac{-68}{151} \end{bmatrix}$$

Find $\begin{vmatrix} 2 & 0 & 1 & -2 \\ -1 & 4 & -3 & 0 \\ -2 & 3 & 0 & 4 \\ 3 & 1 & -4 & 0 \end{vmatrix}$

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$$= -(-2) \begin{vmatrix} -1 & 4 & -3 \\ -2 & 3 & 0 \\ 3 & 1 & -4 \end{vmatrix} - 4 \begin{vmatrix} 2 & 0 & 1 \\ -1 & 4 & -3 \\ 3 & 1 & -4 \end{vmatrix}$$

$$= 2(12 + 0 + 6 - (-27 + 0 + 32)) - 4(-32 + 0 - 1 - (12 - 6 + 0))$$

$$= 2(18 - 5) - 4(-33 - 6)$$

$$= 2(13) - 4(-39)$$

$$= 26 + 156$$

$$= 182$$

$$x^2 + y^2 \geq 5$$

Graph, and find the vertices of the solution set of $x - y > -1$. $x - 1 \text{ NT} = -1$ $y - 1 \text{ NT} = 1$

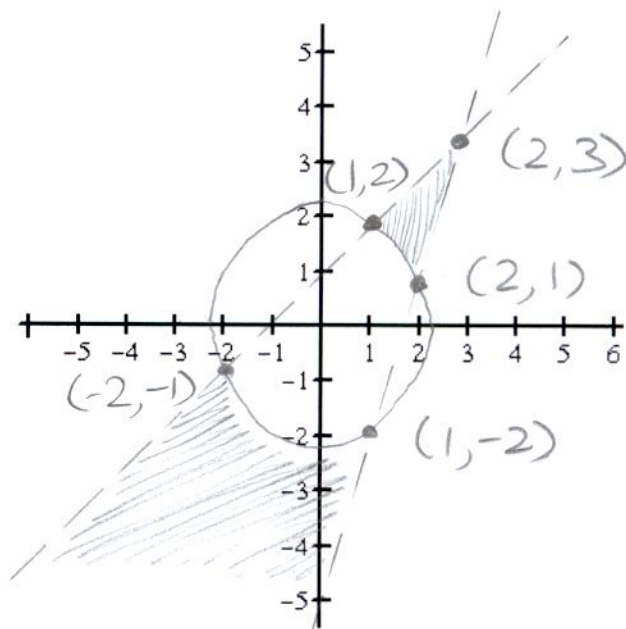
SCORE: ___ / 12 PTS

$$3x - y < 5 \quad = \frac{5}{3} \quad -5$$

Show proper algebra work for full credit. **NO CREDIT FOR GUESS & CHECK.**

$$\begin{aligned} x - y &= -1 \\ 3x - y &= 5 \\ \hline -2x &= -4 \\ x &= 2 \\ y &= 3 \quad (2, 3) \end{aligned}$$

$$\begin{aligned} x - y &= -1 \rightarrow x = y - 1 \\ x^2 + y^2 &= 5 \\ (y - 1)^2 + y^2 &= 5 \\ 2y^2 - 2y + 1 &= 5 \\ 2y^2 - 2y - 4 &= 0 \\ y^2 - y - 2 &= 0 \\ (y - 2)(y + 1) &= 0 \\ y &= 2 \text{ or } y = -1 \\ x &= 1 \quad x = -2 \\ (1, 2) \quad (-2, -1) \end{aligned}$$



$$\begin{aligned} 3x - y &= 5 \rightarrow y = 3x - 5 \\ x^2 + y^2 &= 5 \\ x^2 + (3x - 5)^2 &= 5 \\ 10x^2 - 30x + 25 &= 5 \\ 10x^2 - 30x + 20 &= 0 \\ x^2 - 3x + 2 &= 0 \\ (x - 2)(x - 1) &= 0 \end{aligned}$$

$$(2, 1) \quad x = 2 \text{ or } x = 1 \quad y = 1 \quad y = -2 \quad (1, -2)$$