## A two dimensional kinematics homework set 2.

1. Find the angle such that the maximum height of a projectile is equal to its horizontal range.
2. Car A is traveling east at $20 \mathrm{~m} / \mathrm{s}$. As car A crosses the intersection shown in the diagram, car B starts from rest 40 m north of the intersection and moves south with a constant acceleration of 2 $\mathrm{m} / \mathrm{s}^{2}$.
a. What is the position of B relative to A 6 s after A crosses the intersection?
b. What is the velocity of $B$ relative to $A$ for $t=6 s$ ?
c. What is the acceleration of $B$ relative to $A$ for $t=6 s$ ?

3. Derive a general formula for the horizontal distance covered by a projectile launched horizontally at speed vo from height $h$.
4. A freight train is moving at a constant speed of Vt. A man standing on a flatcar throws a ball into the air and catches it as it falls. Relative to the flatcar, the initial velocity of the ball is Vib straight up.
a. What are the magnitude and direction of the initial velocity of the ball as seen by a second man standing on the ground next to the track?
b. How much time is the ball in the air according to the man on the train? According to the man on the ground? Mathematically prove your two answers.
c. What horizontal distance has the ball traveled by the time it is caught according to the man on the train? According to the man on the ground?
d. What is the minimum speed of the ball during its flight according to the man on the train?

According to the man on the ground?
e. What is the acceleration of the ball according to the man on the train? According to the man on the ground?
5. Galileo, in his Two New Sciences, states that "for elevations (angles of projection) which exceed or fall short of 45 degrees by equal amounts, the ranges are equal. Prove it.
6. A rifle with a muzzle velocity of Vo shoots a bullet at a target R away at the level of the muzzle. How high above the target must the rifle be aimed so that the bullet will hit the target? (Neglect air resistance.)

Let $\mathrm{Vo}=250 \mathrm{~m} / \mathrm{s}$ and $\mathrm{R}=100 \mathrm{~m}$. Find H
7. A bus with a vertical windshield moves along in a rainstorm at speed V relative to the ground. The raindrops fall vertically with a terminal speed of V' relative to the ground. At what angle do the raindrops strike the windshield?
8. A projectile launched at an angle "theta" to the horizontal reaches a maximum height
h. Show that its horizontal range is $4 \mathrm{~h} / \tan$ (theta).
9. A jetliner with an airspeed of $1000 \mathrm{~km} / \mathrm{hr}$ sets out on a 1500 km flight due south. To maintain a southward direction, however, the plane must be pointed fifteen degrees west of south. If the flight takes 100 min , what is the wind velocity?
10. If you can throw a stone straight up to a height of 16 m , how far could you throw it horizontally over level ground? Assume the same throwing speed and optimum launch angle.
11. A hammer slides down a roof of angle theta (with respect to the ground). It slides along the roof distance D . As it leaves the roof, a height H above the ground, it has velocity in both directions. Find how far from the base of the building the hammer lands.

