

1. A matrix  $A$  is non-singular if

**... it is the matrix of coefficients of a homogeneous system of linear equations with a unique solution.**

2. A linear equation is homogeneous if it can be written

$$\dots a_1x_1 + a_2x_2 + \dots + a_nx_n = 0$$

3.  $V$  is a vector subspace of  $W$  if

**... it is a subset of  $W$  and is a vector space itself under the (inherited) operations from  $W$ .**

4. The set of vectors  $u_1, u_2, \dots, u_n$ , spans the space  $V$  if

**... all vectors in  $V$  are linear combinations of  $u_1, u_2, \dots, u_n$**

5. The set of vectors  $u_1, u_2, \dots, u_n$ , is a basis for vector space  $V$  if

**... it is linearly independent and spans  $V$ .**

6. The set of vectors  $u_1, u_2, \dots, u_n$  is linearly independent if

**...  $a_1u_1 + a_2u_2 + \dots + a_nu_n = 0$  implies that all  $a_i$  are equal to 0.**

7. The set of vectors  $u_1, u_2, \dots, u_n$  is linearly dependent if

**... one can be written as a linear combination of the others, or if there are non-zero solutions to  $a_1u_1 + a_2u_2 + \dots + a_nu_n = 0$  such that at least some  $a_i$  are not equal to 0.**

8. The vector  $w$  is a linear combination of  $u_1, u_2, \dots, u_n$  if

$$w = a_1u_1 + a_2u_2 + \dots + a_nu_n$$

9. Function  $f$  from space  $V$  to  $W$  is an onto mapping if

**... for every vector  $w$  in  $W$  there is a vector  $v$  in  $V$  such that  $f(v) = w$**

10. Function  $f$  from space  $V$  to  $W$  is a 1 to 1 mapping if

**$f(v) = w$  and  $f(u) = w$  implies that  $u = v$**

11. The rank of a matrix is

**... the dimension of the row space**

12. The dimension of a vector space is

**... the number of vectors in a basis**

13. Function  $f$  from space  $V$  to  $W$  is an isomorphism if

**... it is one to one and onto and  $f(rv + sw) = f(rv) + f(sw)$  for all scalars  $r$  and  $s$  and all vectors  $v$  and  $w$  in  $V$ .**

14. Function  $f$  from space  $V$  to  $W$  is a homomorphism if

**...  $f(rv + sw) = f(rv) + f(sw)$  for all scalars  $r$  and  $s$  and all vectors  $v$  and  $w$  in  $V$ .**

15. The null space of a linear mapping from  $V$  to  $W$  is

**... the set of vectors  $v$  in  $V$  such that  $v$  is mapped onto the zero vector of  $W$ .**