

$$(4) \quad O(2^n \cdot 3^m \cdot 11^k) = \overbrace{(2-1) \cdot 2^{n-1}}^{1 \cdot 2^{n-1}} \cdot \overbrace{(3-1) \cdot 3^{m-1}}^{2 \cdot 3^{m-1}} \cdot \overbrace{(11-1) \cdot 11^{k-1}}^{2 \cdot 5 \cdot 11^{k-1}} = 2^{n-1} \cdot 3^{m-1} \cdot 5 \cdot 11^{k-1}$$

$$720 = O(J) = 2^4 \cdot 3^2 \cdot 5^1, \text{ so } n=3, m=3, k=1$$

$$\text{and } J = 2^3 \cdot 3^3 \cdot 11^1 = 2376$$

(5)

p	q	r	$q \wedge (r \rightarrow p)$	$v \vee r$
1	1	1	1	1
1	1	0	1	0
1	0	1	0	1
1	0	0	0	0
0	1	1	1	1
0	1	0	1	0
0	0	1	0	1
0	0	0	0	0

$$(6) \quad \sim (\forall k)(\exists n)(\forall m) K_n \leq m = (\exists k)(\forall n)(\exists m) K_n \not\leq m$$

$$= (\exists k)(\forall n)(\exists m) K_n > m$$

$(\forall k)(\exists n)(\forall m) K_n \leq m$ says that for any k we can find an n -value such that $K_n \leq m$ works for all m .

But suppose $k=2$; the smallest n we can find in this universe is $n=1$, but $K_n = 2 \cdot 1 \not\leq m$ for all m , for instance in the case $m=3$.

The negation says that we can find a value k such that for all n there is an m with $K_n > m$.

Take $k=2$; then for all n , $2n > m$ for the m -value $m=1$, so this statement is true.