



# **Electricity and Magnetism**

## **Motion of a Charge in an E-field**

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## Last time

- E-field from many charges
- electric fields of charge distribution

# Overview

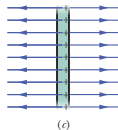
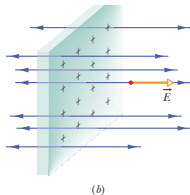
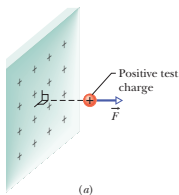
- motion of charges in electric fields

# Electric field due to an Infinite Sheet of Charge

Suppose the sheet is in air (or vacuum) and the charge density on the sheet is  $\sigma$  (charge per unit area):

$$E = \frac{\sigma}{2\epsilon_0}$$

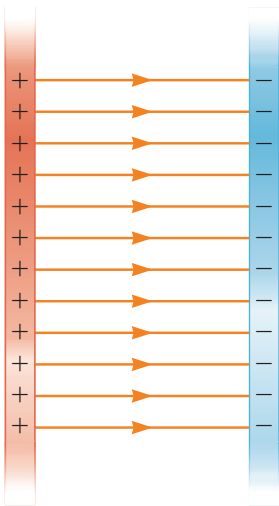
It is uniform! It does not matter how far a point  $P$  is from the sheet, the field is the same.



## Field Lines: Uniform Field

The field from two infinite charged plates is the sum of each field.

$$E = \frac{\sigma}{\epsilon_0}$$



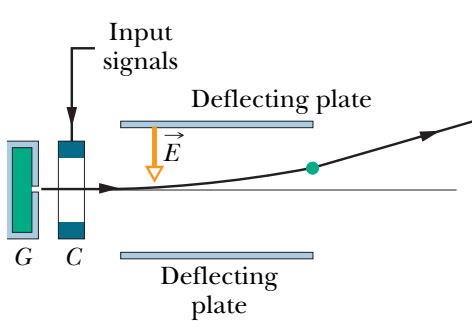
The field in the center of a parallel plate **capacitor** is nearly uniform.

## Free charges in an E-field

The force on a charged particle is given by  $\mathbf{F} = q\mathbf{E}$ .

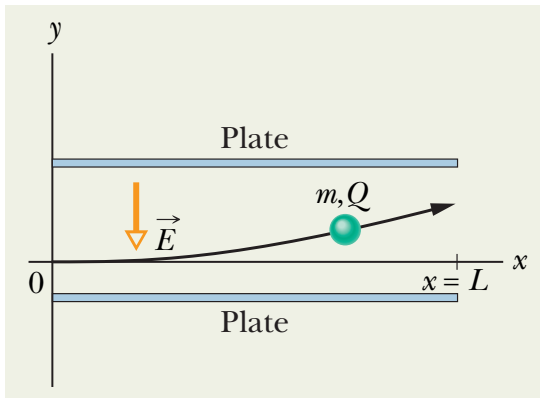
If the charge is free to move, it will accelerate in the direction of the force.

Example: Ink-jet printing



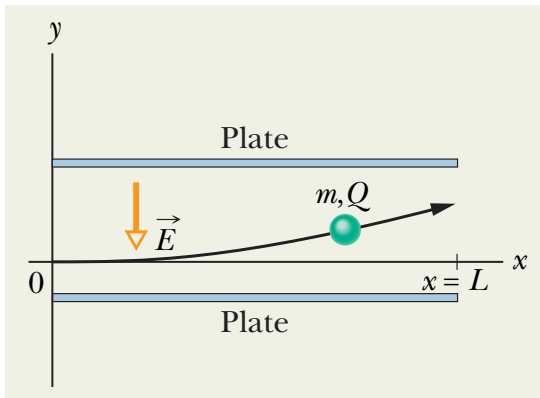
# Motion of a Charged Particle in an E-field

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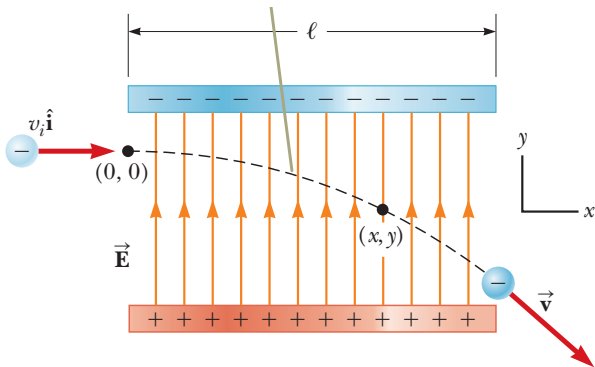


Trajectory is a parabola: similar to projectile motion.



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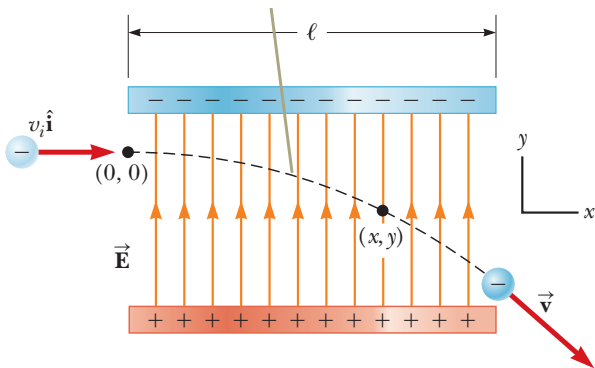
(a) What is the acceleration of an electron in the field of strength  $E$ ?



(b) The charge leaves the field at the point  $(\ell, y_f)$ . What is  $y_f$  in terms of  $\ell$ ,  $v_i$ ,  $E$ ,  $e$ , and  $m_e$ ?

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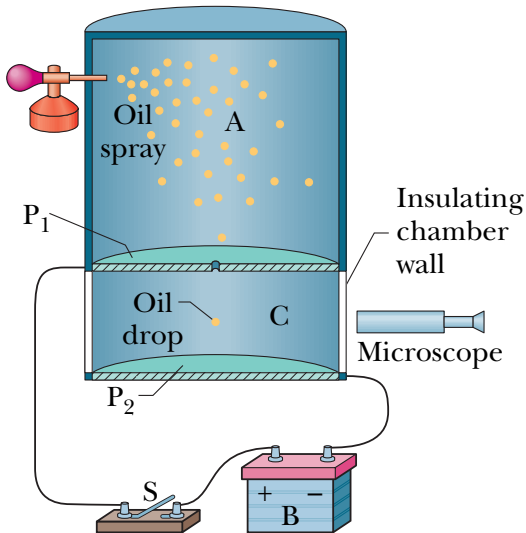
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$$y_f = -\frac{eE\ell^2}{2m_e v_i^2}$$

# Millikan's Oil Drop Experiment: Measuring $e$



## Sparking: Electrical Breakdown

Electric fields can cause forces on charges.

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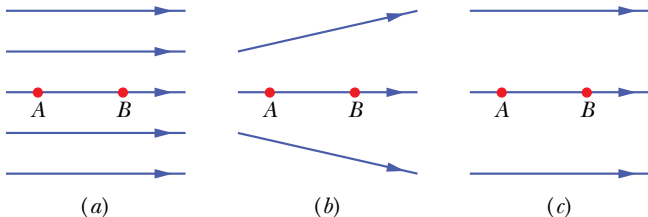
The air along the spark becomes a **plasma** of free charges and can conduct electricity.

Sparks look like bright streaks because the air molecules becomes so hot. Accelerating charges radiate, so lightning can also cause radio interference.

# Question

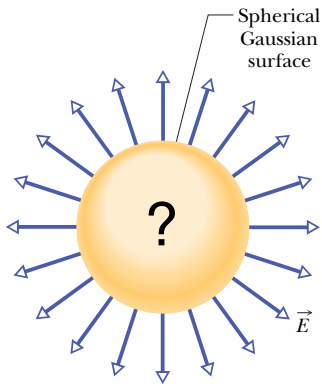
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**1** Figure 22-20 shows three arrangements of electric field lines. In each arrangement, a proton is released from rest at point  $A$  and is then accelerated through point  $B$  by the electric field. Points  $A$  and  $B$  have equal separations in the three arrangements. Rank the arrangements according to the linear momentum of the proton at point  $B$ , greatest first.



## For next time: Gauss's Law basic idea

Gauss's law relates the electric field across a closed surface (eg. a sphere) to the amount of net charge enclosed by the surface.



Can we quantify the “electric field across a boundary”?



# Summary

- motion of charges in E-fields

## Homework Halliday, Resnick, Walker:

- Read up through Chapter 23.
- Ch 22, onward from page 597. Problems: 39, 43