# Electricity and Magnetism Electric Potential Energy 

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## Last time

- electric flux
- Gauss's law
- implications of Gauss's law
- Coulomb's law from Gauss's law
- some rules to help solve problems


## Warm Up Question

Page 621, \#8
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Rank the spheres according to their volume charge density, greatest first. The figure also shows a point $P$ for each sphere, all at the same distance from the center of the sphere.
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(B) d, c, b, a
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## Some Implications of Gauss's Law

Faraday Ice Pail


A charge placed inside a conducting shell appears on the outside of the conductor.
( $\mathbf{E}=0$ for the Gaussian surface shown.)

## Overview

- electrical potential energy
- dipole energy in a electric field


## Potential Energy

Recall from 2A, there are many kinds of potential or stored energy:

- gravitational ( $U=m g h$ )
- elastic $\left(U=\frac{1}{2} k x^{2}\right)$


## potential energy

energy that a system has as a result of its configuration; stored energy

## mechanical energy

the sum of a system's kinetic and potential energies,
$E_{\text {mech }}=K+U$

## Conservative Forces

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The work done by a conservative force is always related to potential energy:

$$
\Delta U=U_{f}-U_{i}=-W
$$

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W=-\Delta U
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Example: The system is a compressed spring. It does work on a massive block, pushing the block. The amount of work done by the spring is equal to the decrease in potential energy of the spring (ie. $-\Delta U$ ).

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Some forces are dissipative and do not conserve mechanical energy $\left(E_{\text {mech }}=K+U\right)$.

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Examples of non-conservative forces:

- Friction
- Air resistance

Mechanical energy is converted to heat or other inaccessible forms.

## Potential Energy

The work done by gravity pulling down a mass near the Earth's surface:

$$
\begin{aligned}
W & =F d \cos \theta \\
& =F\left(y_{f}-y_{i}\right) \cos \left(180^{\circ}\right) \\
& =-m g\left(y_{f}-y_{i}\right)
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Change in gravitational potential energy

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W_{g}=-\Delta U_{g}
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where $W$ is the work done by gravity and $\Delta U$ is the potential energy change of the system.

## Potential Energy and the Electrostatic Force

The electrostatic force is a conservative force.
We can ask what is the stored energy (potential energy) of some particular configuration of charge.
electric potential energy
The electric potential energy of a system of fixed point charges is equal to the work that must be done on the system by an external agent to assemble the system, bringing each charge in from an infinite distance.

## Potential Energy and the Electrostatic Force

An example!
Consider an infinite sheet of charge, density $\sigma$. It causes and electric field $E$.

Potential energy change of a charge $q$ moving a distance $r_{f}-r_{i}$ ?


Work done bringing $q$ in from $r_{i}$ to $r_{f}$ ?

$$
\begin{aligned}
W & =F d \cos \theta \\
& =(q E)\left(r_{f}-r_{i}\right) \cos (0) \\
& =q E\left(r_{f}-r_{i}\right)
\end{aligned}
$$

Similar to lifting a book.

## Question

In the figure, a proton moves from point $i$ to point $f$ in a uniform electric field directed as shown.
(a) Does the force of the electric field do positive or negative work on the proton?

(A) positive
(B) negative

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## Work done against Gravity by an Applied Force

The work done on the book by an external agent:

$$
\begin{aligned}
W_{\mathrm{app}} & =F d \cos \theta \\
& =F_{\mathrm{app}}\left(y_{f}-y_{i}\right) \cos \left(0^{\circ}\right) \\
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where $W$ is the work done on the system and $\Delta U$ is the potential energy change of the system.

## Question

Now we move the proton from point $i$ to point $f$ in a uniform electric field directed as shown with an applied force.
(a) Does our force do positive or negative work?

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## Potential Energy of two point charges

Consider two charges $q_{1}$ and $q_{2}$ at a distance $r$.
They repel each other. Bringing them to that configuration requires work.


Define $U(\infty)=0$ so that $U(r)=\Delta U=U(r)-U(\infty)$
Then, the potential energy of two point charges is:

$$
U(r)=\frac{k q_{1} q_{2}}{r}
$$

## Potential Energy of many point charges

Suppose we have three point charges.

Let

$$
U_{12}=\frac{k q_{1} q_{2}}{r_{12}}
$$

Then the total potential energy of the configuration is:

$$
U_{\text {net }}=U_{12}+U_{13}+U_{23}
$$

Just add up all the pairwise potential energies!

## Potential Energy

We already talked about the potential energy charge has due to the electric field of other charges in its vicinity.

Now, we think about the potential energy of a dipole in an electric field.

## Electric Dipole in an Electric Field

Remember:

## electric dipole

A pair of charges of equal magnitude $q$ but opposite sign, separated by a distance, $d$.

A water molecule is an example


## Electric Dipole in an Electric Field

Because the net charge of a dipole is zero, the net force is zero also. But there is a torque!


The dipole is being torqued into alignment.

(b)
$\theta$ is the angle between the $\mathbf{p}$ and $\mathbf{E}$

$$
\begin{aligned}
\tau & =F d \sin \theta \\
& =(q E) d \sin \theta
\end{aligned}
$$

and $p=q d$

$$
\tau=p E \sin \theta \quad \text { clockwise }
$$

(It is clockwise for this diagram, but in general you must consider the direction of the field and the orientation of the dipole.)

$$
\boldsymbol{\tau}=\mathbf{p} \times \mathbf{E}
$$

## Electric Dipole in an Electric Field

We can also find an expression for the potential energy of a dipole in an E-field.
Define $U=0$ when $\theta=90^{\circ}$ (the dipole is $\perp$ to the field lines).

$$
U=-p E \cos \theta
$$

$$
U=-\mathbf{p} \cdot \mathbf{E}
$$

## Question: Electric Dipole in an Electric Field

The figure shows four orientations of an electric dipole in an external electric field. Rank the orientations according to the magnitude of the torque on the dipole, greatest first.

(A) $1,2,3,4$
(B) 1 and 3, 2 and 4
(C) 2 and 4, 1 and 3
(D) all the same
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## Microwave Ovens

An application of the fact that a dipole experiences a torque in an electric field is microwave cooking.

Microwave ovens produce electric fields that change direction rapidly.

Since water molecules are dipoles, they begin to rotate to align with the field, back and forth.

This motion becomes thermal energy in the food.

## Summary

- electric potential energy

Homework Halliday, Resnick, Walker:

- work through the sample problems on page 643 and 644
- Ch 24, onward from page 646. Problems: 98, 102
- Ch 22, onward from page 597. Problems: 57


[^0]:    ${ }^{1}$ Halliday, Resnick, Walker, page 628.

