



# **Conceptual Physics**

## **Projectiles**

## **Motion of Planets**

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De Anza College

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# Last time

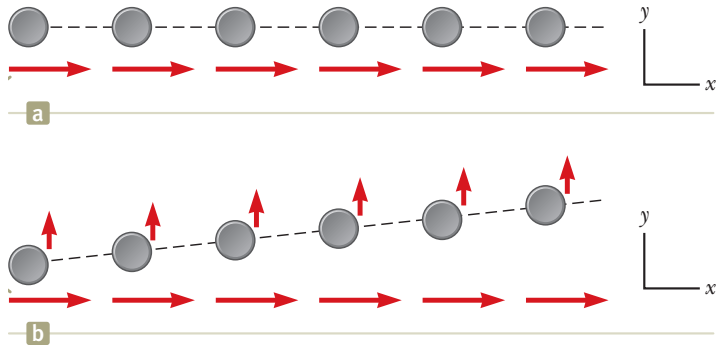
- angular momentum
- gravity
- gravitational field
- black holes

# Overview

- projectile motion
- orbital motion
- Kepler's Laws
- escape speed

## Motion in 2 directions

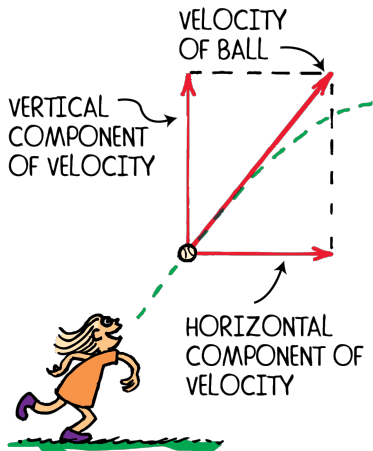
Imagine an air hockey puck moving with horizontally constant velocity:



If it experiences a momentary upward (in the diagram) acceleration, it will have a component of velocity upwards. The horizontal motion remains unchanged!

# Motion in 2 directions

Motion in perpendicular directions can be analyzed separately.



A vertical force (gravity) does not affect horizontal motion.

The horizontal component of velocity is constant.

# Projectiles

## projectile

Any object that is thrown. We will use this word specifically to refer to thrown objects that experience a vertical acceleration  $g$ .

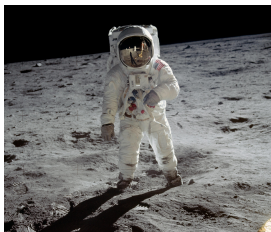
# Projectiles

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For projectile motion, we assume air resistance is negligible. This gives symmetrical parabolic trajectories.

## Why do we care?



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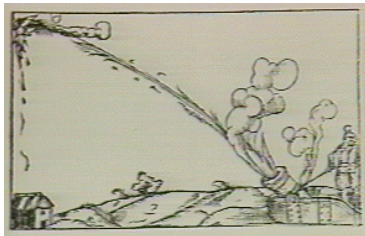
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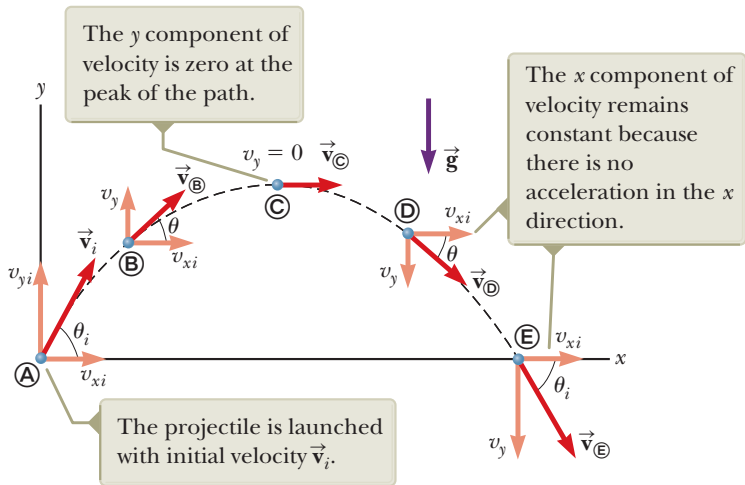
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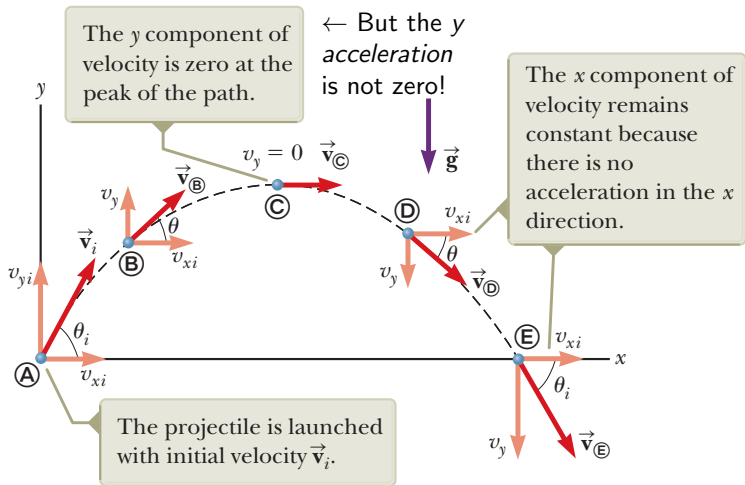
## Why do we care?



# Projectile Velocity



# Projectile Velocity



# Motion of projectiles

We already considered the motion of objects dropped from rest at time  $t = 0$ , allowed to fall freely. (**Calling down positive.**)

Velocity of the object at time  $t$ :

$$v = v_i + gt$$

Distance the object falls in time  $t$ :

$$d = \frac{1}{2}gt^2$$

# Acceleration due to gravity and kinematics

Let's think about the components of the motion separately.

Vertical (y-direction):

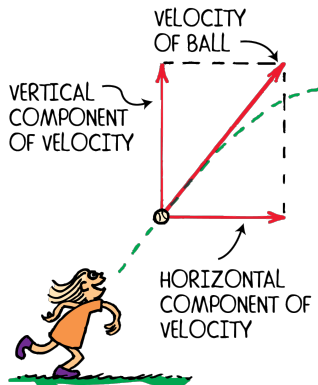
$$v_y = v_{i,y} - gt$$

$$d_y = v_{i,y}t - \frac{1}{2}gt^2$$

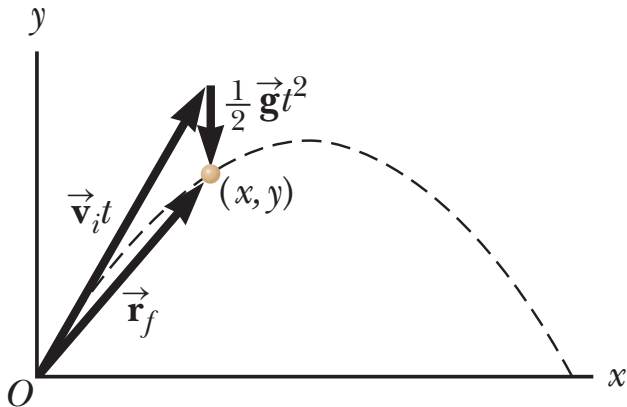
Horizontal (x-direction):

$$a_x = 0, \quad v_x = v_{i,x}$$

$$d_x = v_{i,x}t$$



# Projectile's Trajectory



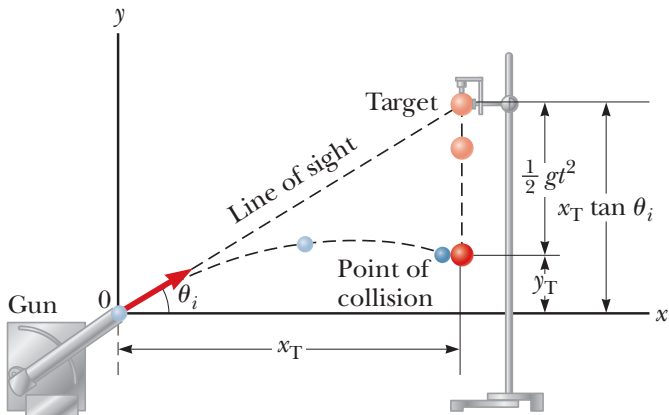
The object would move in a straight line, but the force of gravity causes it to fall as it moves to the right.

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<sup>1</sup>Figure from Serway & Jewett, 9th ed.

# Motion in 2 Dimensions

A method of testing that the vectors add as asserted!



## Example Problem

Suppose the pellet-gun on the previous slide can fire the pellet with an extremely high velocity.

(a) How many meters below the line of sight would the pellet be after 5 seconds?

(b) If the horizontal component of the pellet's velocity is 20 m/s, how far downrange is the pellet after those 5 seconds?

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<sup>0</sup>See Hewitt, page 175.

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(Hint: we can consider each component of the velocity separately.)

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<sup>0</sup>See Hewitt, page 175.

## Another example, problem 1, page 192

A ball is thrown horizontally from a cliff at a speed of 10 m/s.  
What will its speed be (roughly) after 1s?

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<sup>0</sup>See Hewitt, page 192.

## Last one, # 4, page 192

A steel ball is fired horizontally at  $8.0 \text{ m/s}$  from a  $1.0 \text{ m}$ -high table top.

Show that a  $20 \text{ cm}$  tall coffee can placed on the floor  $3.2 \text{ m}$  from the base of the table will catch the ball.

## Last one, # 4, page 192

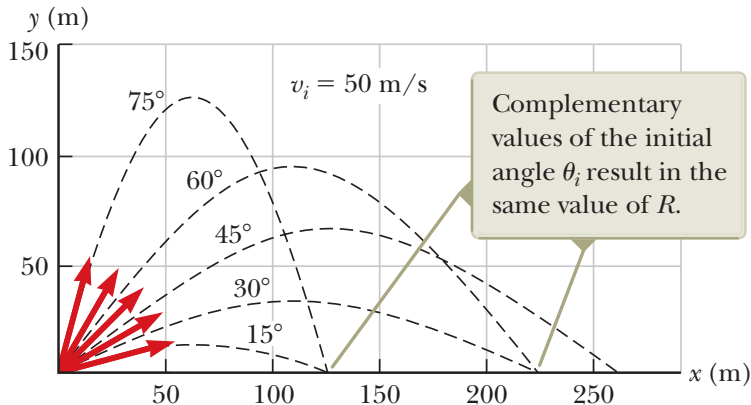
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for a falling object

$$d = \frac{1}{2}at^2$$

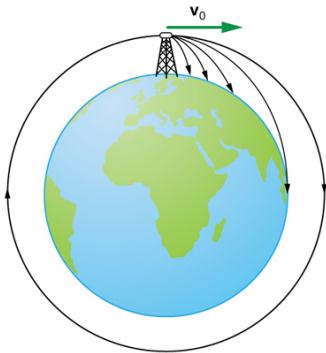
# Effect of changing launch angle



# Satellites

Imagine now that you could throw an object straight out horizontally so fast that as it falls it matches the Earth's curvature.

The object falls 1 m in 0.45 s. If it goes forward 3,570 m in that time, then the Earth's surface has also curved one meter away over that distance.



This corresponds to a speed of 7,900 m/s.

<sup>1</sup>Figure from "College Physics", OpenStax College, Ch 3, pg 110.

# Satellites

This is the same principle by which the Moon stays in orbit around the Earth. The Moon is the Earth's natural satellite.

The same idea is applied to artificial satellites that are put into orbit around the Earth.

They are moving at very high speeds and continuously falling around the Earth.

Satellites can have many purposes, eg.

- telecommunications
- weather and Earth-monitoring
- GPS (global positioning system)
- human spaceflight and experiments

## Some Types of Earth-Orbit

- **Low Earth Orbit (LEO)** - altitude from 160 km to 2,000 km with a period of 90–130 minutes; all human spaceflight except Apollo has been in this orbit (or suborbital), also Earth observation satellites

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# Motion of the Planets

The planets in our solar system orbit the Sun. (As planets in other systems orbit their stars.)

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Nicolaus Copernicus (early 1500s A.D.) is credited with the paradigm since he developed a mathematical model and took seriously the idea that the implication was that the Earth moved around the Sun, but others had similar thoughts:

- Aristarchus of Samos (c. 270 BCE)
- Martianus Capella (400s A.D.)
- Aryabhata (500s A.D.), Nilakantha Somayaji (1500s A.D.)
- Najm al-Dīn al-Qazwīnī al-Kātibī (1200s A.D.)

# Motion of the Planets

After Copernicus's proposal, Tycho Brahe gathered a lot of data about the positions of stars and planets.

Johannes Kepler inherited Brahe's data and did the calculations to deduce a complete model.

Galileo gathered additional data that supported the heliocentric model and popularized it.

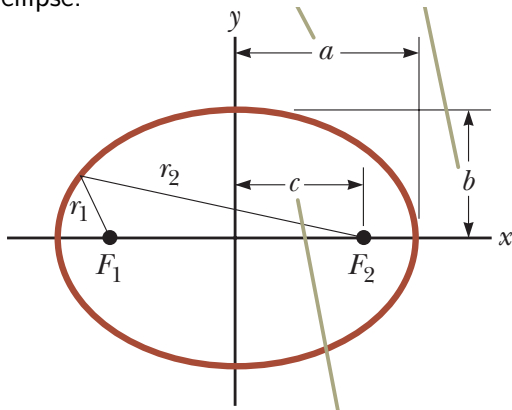
# Kepler's Laws

Kepler's Three laws give simple rules for predicting stable planetary orbits.

1. All planets move in elliptical orbits with the Sun at one focus.
2. The a line from the Sun to a planet sweeps out equal areas of space in equal time intervals.
3. The square of the orbital period of any planet is proportional to the cube of the distance from the planet to the Sun. ( $T^2 \sim r^3$ )

# Kepler's First Law: Elliptical Orbits

Defining an ellipse:



$a$  is the *semimajor axis*

$b$  is the *semiminor axis*

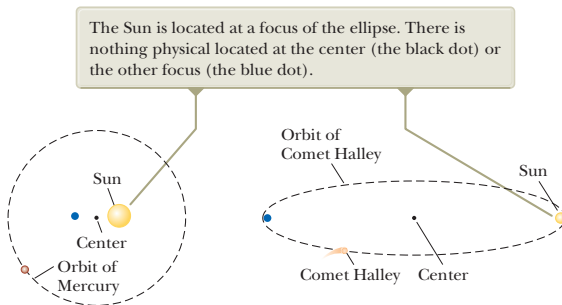
$c$  is the distance from the center of the ellipse to the focus

$e$  is the *eccentricity* of the ellipse  $e = c/a$

$$a^2 = b^2 + c^2$$

# Kepler's First Law: Elliptical Orbits

“All planets move in elliptical orbits with the Sun at one focus.”

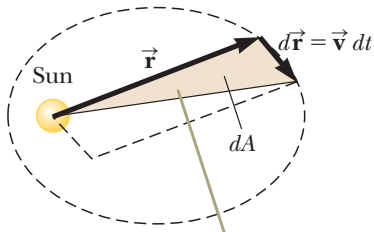
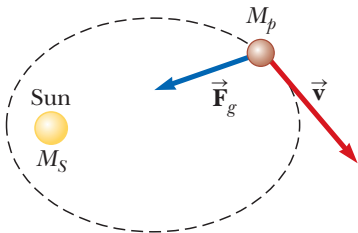


- The planets' orbits are close to circular. (Mercury's is the least circular.)
- Halley's Comet has an orbit with a high eccentricity.

# Kepler's Second Law: Equal Areas in Equal Time

“The radius vector drawn from the Sun to a planet sweeps out equal areas in equal time intervals.”

What does it mean?



When the planet is closer to the Sun, it must be moving faster.

## Kepler's Third Law: $T^2 \sim r^3$

“The square of the orbital period of any planet is proportional to the cube of the distance from the planet to the Sun.”

$$T^2 = K_s r^3$$

where  $K_s$  is a constant,

$$K_s = \frac{4\pi^2}{GM_s} = 2.97 \times 10^{-19} \text{ s}^2 \text{ m}^{-3}.$$

# Escape Speed

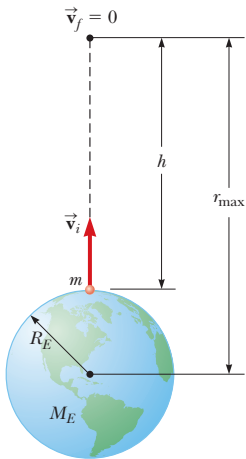
## escape speed

The speed an object would need to have at Earth's surface to have enough kinetic energy to leave Earth, overcoming the attraction of Earth's gravity.

The object will convert its kinetic energy to potential energy as it moves higher and higher, away from the Earth.

# Escape Speed

How fast does an object need to be projected with to escape Earth's gravity?



# Escape Speed

To escape the surface of the Earth, an object must have a starting speed of

$$v_e = 1.12 \times 10^4 \text{ m/s} = 11.2 \text{ km/s}$$

For other planets / celestial bodies the escape speeds can also be defined.

The escape speed depends on the radius of the body and its mass.

For the Sun, the escape speed at its surface is much higher:

$$v_e = 620 \text{ km/s}$$

# Summary

- projectile motion
- orbits
- motion of planets and satellites
- Kepler's laws
- escape speed

## Homework Hewitt,

- Ch 10, onward from page 190. Exercises: 15, 19, 23, 45, 59;  
Problems: 3
- Study!
- read through the textbook