

# Physics 50 Introduction to Mechanics Physics Background, Units, Dimension

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#### Last time

- course info
- science, science terms, and the scientific method

### **Overview**

- physics
- scientific terms
- definitions of the base units
- dimensional analysis

Physics is the science of fundamental interactions of matter and energy.

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Physicists (and others who use physics) want to predict accurately how an object or collection of objects will behave when interacting.

Why?

- to better understand the universe
- to build new kinds of technology (engines, electronics, imaging devices, mass manufacturing, energy sources)
- to build safer and more efficient infrastructure
- to go new places and explore
- to prepare for the future

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#### How?

Amazingly, relatively simple mathematics can represent interacting physical objects.

The results of calculations give accurate predictions, provided the mathematical model is a good one.

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*eg.* a pool table. The system might include the balls, the sides of the table, but maybe not the whole Earth. And certainly not the Andromeda galaxy.

#### Model

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#### Hypothesis

An educated guess about a relationship between measurable quantities. It must be *falsifiable* by observations or experiments.

## The Scientific Hypotheses

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This is a scientific hypothesis:

Near the surface of the Earth, if two objects are dropped from the same height at the same time in a vacuum they will strike the ground at the same time, regardless of their masses.

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Valid when

- v << c,
- gravitational fields are not too strong,
- distances are much bigger than  $\ell_p$  (Planck length), etc.

#### Law

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eg. 
$$\vec{\mathbf{F}}_{net} = m \vec{\mathbf{a}}$$

("If I push this shopping cart twice as hard, it will accelerate twice as fast." )  $% \left( \frac{1}{2} + \frac{1}{2$ 

In science, a theory is

- (A) an educated guess.
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#### Quantities, Units, Measurement

If we want to make precise *quantitative* statements we need to agree on measurements: standard reference units.

We will mostly use SI (Système International) units:

Length	meter, m
Mass	kilogram, kg
Time	second, s

and many more!

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In all your numerical answers, make sure you include the appropriate units!

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Physicists now strive to chose definitions for units that are based on **fundamental physical phenomena** - things anyone, anywhere could in principle observe consistently.

### **Units: Length**

The meter, m, is the SI unit of length. It is about 3.28 feet.

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The current definition of the meter (since 1983) is more precise and more convenient for experiments:

#### meter

One meter is the distance light travels in 1/299,792,458-ths of a second.

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<sup>1</sup>Atomic clock FOCS-1, METAS, Bern, Switzerland; Chip photo, NIST.

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 $\rightarrow$  The atomic clocks at the National Institute for Standards and Technology (NIST) are principle references for International Atomic Time.

#### second

One second is the time for the radiation corresponding to the transition between the two hyperfine energy levels of the ground state of the caesium-133 atom to complete 9,192,631,770 oscillations.
The kilogram, kg, is the SI unit of mass.

Loosely speaking, mass is a measure of the amount of matter in an object.

<sup>&</sup>lt;sup>1</sup>A replica of the prototype kilogram, Wikipedia, user Japs 88.

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Before May 20th, the official 1-kilogram sample, the *international prototype kilogram* was a cylinder of platinum and iridium stored near Paris.



<sup>1</sup>A replica of the prototype kilogram, Wikipedia, user Japs 88.

1 kilogram is 1,000 grams.

Originally, the gram was defined to be the mass of one cubic centimeter of water at the melting point of water.

The international prototype kilogram was designed to follow this definition.

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The Kibble balance measures mass by way of current and voltage measurements. Both current and voltage in this device are *quantized*, meaning they have a **smallest unit** and cannot take any value. The smallest units depend on a fundamental constant of nature, Planck's constant, *h*.

Thus, the kilogram is defined so that Planck's constant is exactly:

$$h = 6.626\,070\,15 \times 10^{-34}$$
 kg m<sup>2</sup>/s.



<sup>1</sup>Figure by Emilio Pisanty.



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# **Dimensional Analysis**

All measurement values have associated units.

Equations relating measurable physical values also relate units.

This means units on each side of the equals sign must be equal.

Dimensional analysis allows us to:

- check our equation is correct
- check our calculation
- figure out the final units of an answer if we can't remember what they should be

This is very important!

distance traveled = speed  $\times$  time

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Equation:

x = vt

Distance is a length. In the textbook, a value with units length is written [L]. Time units would be [T].

Speed is a length covered in an amount of time: [L]/[T].

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The dimensions of our equation:

$$[\mathsf{L}] = \frac{[\mathsf{L}]}{[\mathsf{T}]}[\mathsf{T}]$$

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The dimensions of our equation:

$$[\mathsf{L}] = \frac{[\mathsf{L}]}{[\mathsf{F}]}[\mathsf{F}]$$

So,

$$[\mathsf{L}] = [\mathsf{L}] \quad \checkmark$$

Another one,

$$v^2 = v_0^2 + 2ax$$

a is an acceleration, a rate of change of speed. Units: [L]/[T]/[T] = [L]/[T^2]

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$$\left(\frac{[\mathsf{L}]}{[\mathsf{T}]}\right)^2 = \left(\frac{[\mathsf{L}]}{[\mathsf{T}]}\right)^2 + \frac{[\mathsf{L}]}{[\mathsf{T}^2]}[\mathsf{L}]$$

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$$\begin{pmatrix} \begin{bmatrix} \mathsf{L} \\ \hline \mathsf{T} \end{bmatrix} \end{pmatrix}^2 = \left( \frac{\begin{bmatrix} \mathsf{L} \\ \hline \mathsf{T} \end{bmatrix} \right)^2 + \frac{\begin{bmatrix} \mathsf{L} \\ \hline \mathsf{T}^2 \end{bmatrix}}{\begin{bmatrix} \mathsf{T}^2 \end{bmatrix}} \begin{bmatrix} \mathsf{L}^2 \\ \hline \mathsf{T}^2 \end{bmatrix} + \frac{\begin{bmatrix} \mathsf{L}^2 \\ \hline \mathsf{T}^2 \end{bmatrix} \checkmark$$

Units for each term are the same.

The other way to do dimensional analysis is directly in terms of the SI units that will be used.

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$$[m^2/s^2] = [m^2/s^2] + [m^2/s^2] \checkmark$$

# Summary

- physics
- hypotheses and theories
- definitions of the base units
- dimensional analysis

Quiz Monday, in class.

#### **Homework** (not handed in, but do it)

- Get the textbook, James S. Walker, "Physics"
- Read chapter 1
- Ch 1, onward from page 14. Questions: 1; Problems: 5, 7, 9, 11, 12\*, 41, 51 (compare the answers to 12 and 51)

\*Ans for 12: [M]/[T<sup>2</sup>]