# Introduction to Mechanics <br> Relative Motion and Projectiles 

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## Last time

- trajectory equation
- another projectile example


## Overview

- relative motion and projectiles


## Relative Motion And Projectile Motion

Observer on the skateboard sees the ball fall straight down.


Another observer on the sidewalk sees the ball as a horizontally launched projectile.

## Relative Motion And Projectile Motion

\#73, page 108
To decide who pays for lunch, a passenger on a moving train tosses a coin straight upward with an initial speed of $4.38 \mathrm{~m} / \mathrm{s}$ and catches it again when it returns to its initial level. From the point of view of the passenger, then, the coin's initial velocity is $(4.38 \mathrm{~m} / \mathrm{s}) \hat{\mathbf{y}}$. The train's velocity relative to the ground is $(12.1 \mathrm{~m} / \mathrm{s}) \hat{\mathbf{x}}$.
(a) What is the minimum speed of the coin relative to the ground during its flight? At what point in the coin's flight does this minimum speed occur? Explain.

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$12.1 \mathrm{~m} / \mathrm{s}$, At the top of its path, where the $y$-component of velocity is zero.

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(b) Find the initial speed and direction of the coin as seen by an observer on the ground.

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v_{0}=\sqrt{v_{0 x}^{2}+v_{0, y}^{2}} \quad \theta=\tan ^{-1}\left(\frac{v_{0 y}}{v_{0 x}}\right)
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$\mathbf{v}_{0}=12.9 \mathrm{~m} / \mathrm{s}$, at $19.9^{\circ}$ above the horizontal

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$h=0.978 \mathrm{~m}$

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## Summary

- relative motion and projectiles

Test 2 Monday, Feb 24.

## Homework

Walker Physics:

- prev: Ch 4, onward from page 100. Con. Ques: 7, 9; Problems: 1, 40 \& 41, 43, 71, 77, 87, 67 (projectile in disguise)
- Read ahead in Ch 5.

