



Inferential Statistics and Probability a Holistic Approach

Chapter 1

Displaying and Analyzing Data with Graphs


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Introduction

- Syllabus– Homework 0
- Projects
- Computer Lab – S44
 - Minitab
- Website
 - <http://nebula2.deanza.edu/~mo>
- Tutor Lab - S43 (S41 for MPS)
 - Drop in or assigned tutors – get form from lab.
 - Group Tutoring
- Other Questions


2



Descriptive Statistics

- Organizing, summarizing and displaying data
 - Graphs
 - Charts
 - Measure of Center
 - Measures of Spread
 - Measures of Relative Standing


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Problem Solving

- The Role of Probability
- Modeling
- Simulation
- Verification


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Inferential Statistics

- Population – the set of all measurements of interest to the sample collector
- Sample – a subset of measurements selected from the population
- Inference – A conclusion about the population based on the sample
- Reliability – Measure the strength of the Inference

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Raw Data – Apple

Monthly Adjusted Stock Price: 12/1998 to 12/2018

115.82	102.97	106.17	75.50	69.86	52.70	41.97	27.42	11.11	25.77	11.04	9.35	4.19	1.39	0.93	1.42	0.97
110.52	115.73	114.39	74.83	76.83	49.73	40.49	26.01	12.06	23.71	11.93	8.82	4.36	1.36	1.01	1.39	1.07
112.96	116.40	103.43	69.93	77.80	52.67	39.36	24.53	14.00	24.72	10.55	7.49	3.41	1.49	1.05	1.34	1.27
112.47	107.44	96.49	63.79	87.18	49.62	36.92	24.12	14.79	19.97	10.02	6.98	2.52	1.35	0.94	1.01	1.68
105.56	109.84	98.16	65.19	86.93	50.07	31.63	21.89	22.06	18.02	8.83	6.10	2.24	1.47	0.96	1.21	3.96
101.12	117.62	91.10	60.15	79.47	50.81	33.47	21.26	20.68	17.14	8.84	5.55	2.10	1.37	0.99	1.22	3.31
94.60	121.63	88.56	52.71	75.99	43.68	32.73	18.53	21.79	15.88	7.45	4.79	2.12	1.24	1.15	1.51	3.41
98.81	126.33	86.17	59.78	75.17	45.26	33.43	17.67	24.56	15.77	7.78	5.17	1.83	1.17	1.52	1.30	2.73
92.20	120.85	79.89	58.47	75.99	45.56	33.97	16.37	22.63	12.99	9.16	4.69	1.68	0.93	1.58	1.66	4.04
107.20	120.15	72.66	58.45	78.01	45.35	30.58	13.68	18.67	12.09	8.16	5.42	1.76	0.92	1.54	1.44	4.42
95.10	124.05	71.24	58.28	70.38	45.96	26.63	11.62	16.27	11.01	8.91	5.84	1.56	0.98	1.41	1.19	3.73
95.22	112.69	67.37	59.80	59.40	44.15	24.99	11.73	17.61	11.16	9.83	5.00	1.47	0.93	1.61	1.41	3.38

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Crime Rate

- In the last 18 years, has violent crime:
 - Increased?
 - Stayed about the Same?
 - Decreased?

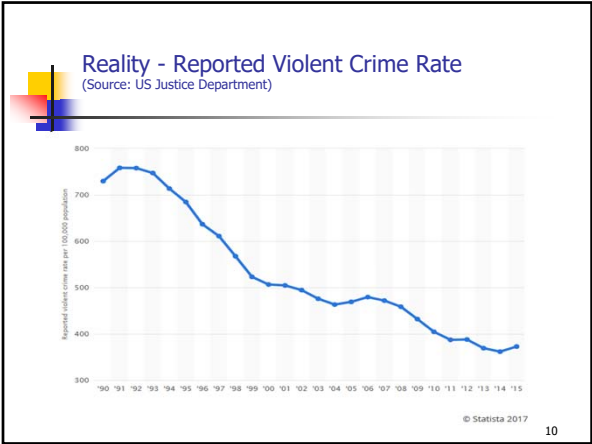
8

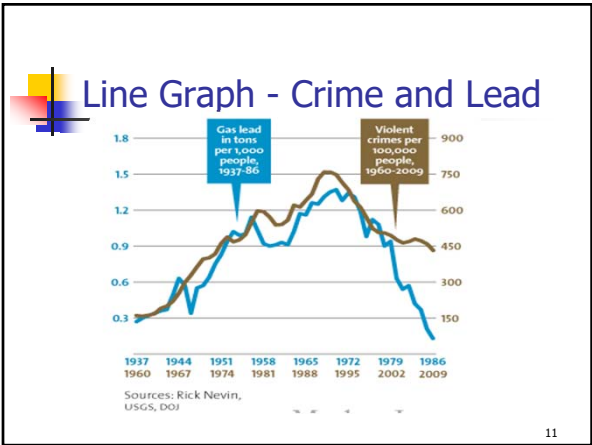
Perception – Gallup Poll

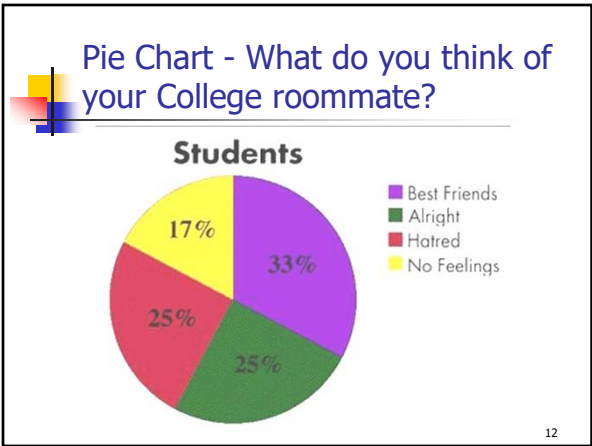
Is there more crime in the U.S. than there was a year ago, or less?

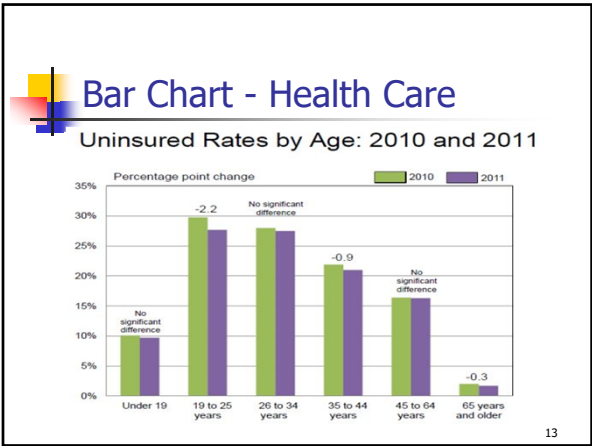
	More	Less	Same (incl.)	No opinion
	%	%	%	%
2018 Oct 5-9	70	20	6	4
2018 Oct 7-11	70	18	8	4
2014 Oct 12-15	63	21	9	7
2013 Oct 3-6	64	19	9	7
2011 Oct 6-9	66	17	8	6
2010 Oct 7-10	66	17	8	9
2008 Oct 1-4	74	15	6	5
2008 Oct 3-5	67	15	9	9
2007 Oct 4-7	71	14	8	6
2006 Oct 9-12	68	16	8	6
2006 Oct 13-16	67	21	9	3
2004 Oct 11-14	63	28	14	5
2003 Oct 6-8	60	25	11	4
2002 Oct 14-17	62	21	11	6
2001 Oct 11-14	41	43	10	6
2000 Aug 29-Sep 5	47	41	7	5
1998 Oct 23-25	52	35	8	5
1997 Aug 22-25	64	25	6	5
1996 Jul 25-28	71	15	8	6
1993 Oct 13-18	67	4	5	4
1992 Feb 28-Mar 1	69	3	4	4
1990 Sep 10	64	3	7	6

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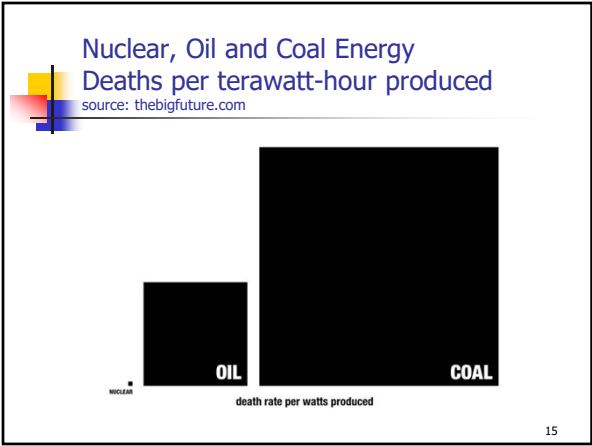


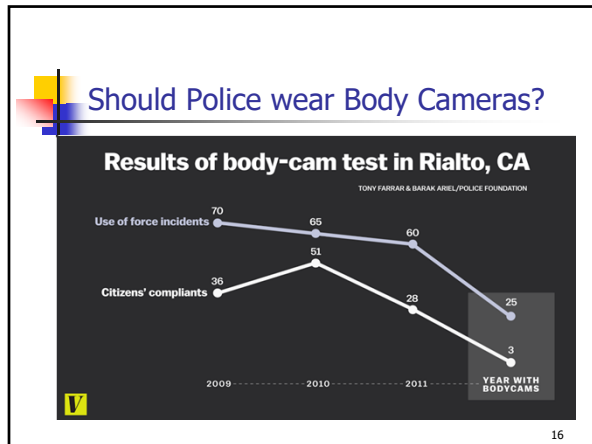


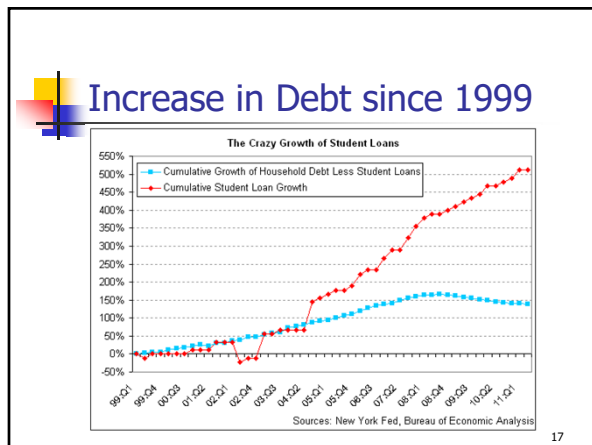


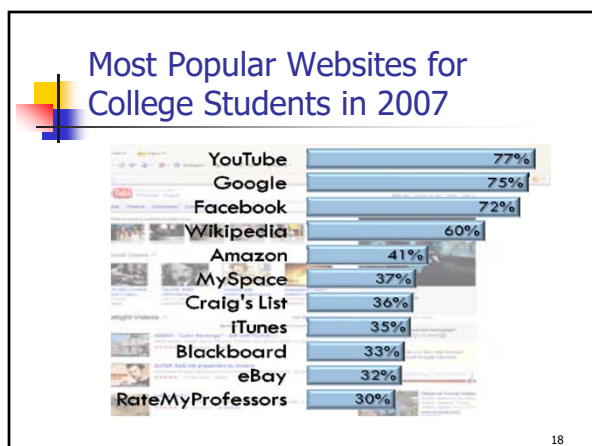


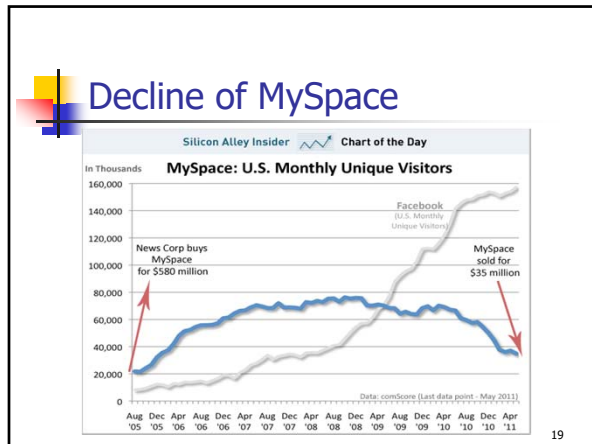












RATE MY PROFESSORS

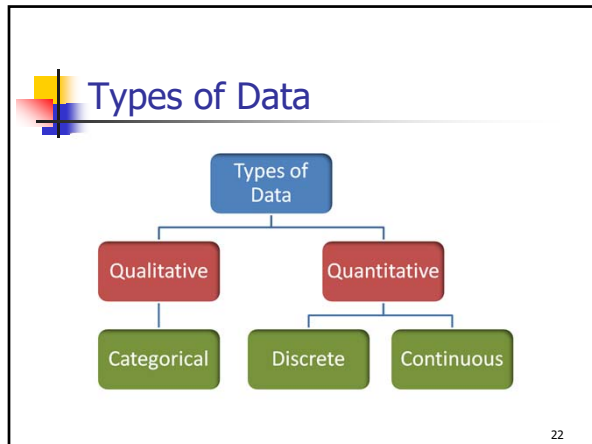
Over 6,000 Schools, 4 million professors, 6 million opinions

De Anza College

Professor's Name	Department	Total Ratings	Overall Quality	Ease	Hot?
	Mandarin	3	4.3	2.0	
	Mandarin	8	1.6	1.6	
	Marketing	1	5.0	5.0	
	Mathematics	66	4.7	4.0	
	Mathematics	73	1.4	1.7	
	Mathematics	15	2.7	2.6	
	Mathematics	41	1.6	2.1	

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- ### Types of Data
- Qualitative
 - Non-numeric
 - Always categorical
 - Quantitative
 - Numeric
 - Categorical numbers are actually qualitative
 - Continuous or discrete
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- A hierarchical diagram titled "Levels of Data Measurement". The root node is "Levels of Data Measurement" in a blue box. It branches into two red boxes: "Qualitative" and "Quantitative". "Qualitative" branches into two green boxes: "Nominal" and "Ordinal". "Quantitative" branches into two green boxes: "Interval" and "Ratio".
- ```
graph TD; A[Levels of Data Measurement] --> B[Qualitative]; A --> C[Quantitative]; B --> D[Nominal]; B --> E[Ordinal]; C --> F[Interval]; C --> G[Ratio];
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- **Nominal:** Names or labels only
    - Example: What city do you live in?
  - **Ordinal:** Data can be ranked, but no quantifiable difference.
    - Example: Ratings Excellent, Good, Fair, Poor
  - **Interval:** Data can be ranked with quantifiable differences, but no true zero.
    - Example: Temperature
  - **Ratio:** Data can be ranked with quantifiable differences and there is a true zero.
    - Example: Age

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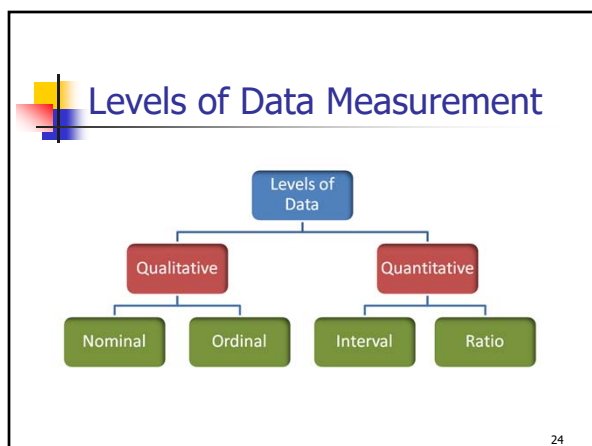
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## Examples of Data

- Distance from De Anza College
- Number of Grandparents still alive
- Eye Color
- Amount you spend on food each week.
- Number of Facebook "Friends"
- Zip Code
- City you live in.
- Year of Birth
- How to prepare Steak? (rare, medium, well-done)
- Do you drive to De Anza?

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## Graphical Methods

- Qualitative Data
  - Pie Chart
  - Bar Chart
- Quantitative Data
  - Stem and Leaf Chart
  - Histogram
  - Ogive
  - Dot Plot

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## Graphing Categorical Data

A sample of 500 adults (age 18 and over) from Santa Clara County, California were taken from the year 2000 United States Census.

| Marital Status           | Frequency |
|--------------------------|-----------|
| Married                  | 270       |
| Widowed                  | 22        |
| Divorced - not remarried | 42        |
| Separated                | 10        |
| Single - never married   | 156       |
| Total                    | 500       |

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## Graphing Categorical Data

- **n = sample size** - The number of observations in your sample size.
- **Frequency** - the number of times a particular value is observed.
- **Relative frequency** - The proportion or percentage of times a particular value is observed.
- **Relative Frequency = Frequency / n**

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## Graphing Categorical Data

A sample of 500 adults (age 18 and over) from Santa Clara County, California were taken from the year 2000 United States Census.

| Marital Status           | Frequency | Relative Frequency        |
|--------------------------|-----------|---------------------------|
| Married                  | 270       | 270/500 = 0.540 or 54.0%  |
| Widowed                  | 22        | 22/500 = 0.044 or 4.4%    |
| Divorced - not remarried | 42        | 42/500 = 0.084 or 8.4%    |
| Separated                | 10        | 10/500 = 0.020 or 2.0%    |
| Single - never married   | 156       | 156/500 = 0.312 or 31.2%  |
| Total                    | 500       | 500/500 = 1.000 or 100.0% |

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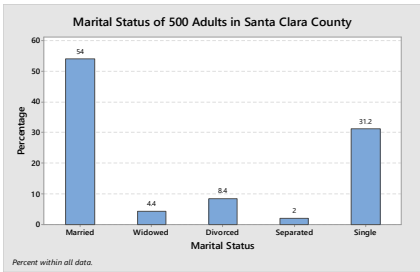
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## Bar Graph of Categorical Data



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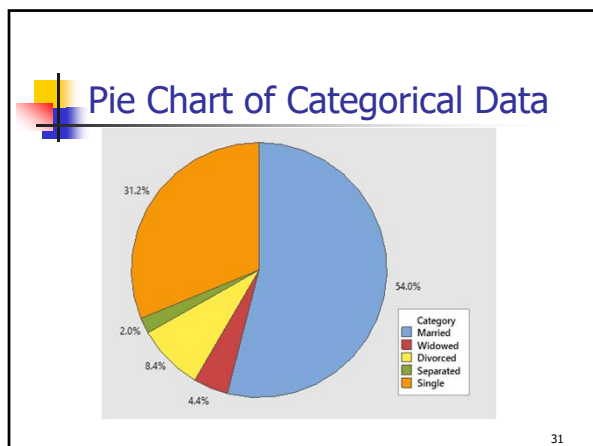
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### Daily Minutes spent on the Internet by 30 students

|     |     |     |     |     |
|-----|-----|-----|-----|-----|
| 102 | 104 | 85  | 67  | 101 |
| 71  | 116 | 107 | 99  | 82  |
| 103 | 97  | 105 | 103 | 95  |
| 105 | 99  | 86  | 87  | 100 |
| 109 | 108 | 118 | 87  | 125 |
| 124 | 112 | 122 | 78  | 92  |

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- ### Describing Numeric Data
- Center?
    - Where is an "average" value
  - Spread?
    - How far are data spread from the center
  - Shape?
    - Symmetric or skewed?
  - Anything Unusual?
    - Outliers, more than 1 peak?
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## Stem and Leaf Graph

|    |             |
|----|-------------|
| 6  | 7           |
| 7  | 18          |
| 8  | 25677       |
| 9  | 25799       |
| 10 | 01233455789 |
| 11 | 268         |
| 12 | 245         |

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## Back-to-back Example

- Passenger loading times for two airlines

|                                                                         |                                                                        |
|-------------------------------------------------------------------------|------------------------------------------------------------------------|
| 11, 14, 16, 17,<br>19, 21, 22, 23,<br>24, 24, 24, 26,<br>31, 32, 38, 39 | 8, 11, 13, 14,<br>15, 16, 16, 18,<br>19, 19, 21, 21,<br>22, 24, 26, 31 |
|-------------------------------------------------------------------------|------------------------------------------------------------------------|

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## Back to Back Example

|        |   |        |
|--------|---|--------|
|        | 0 |        |
|        | 0 | 8      |
| 14     | 1 | 134    |
| 679    | 1 | 566899 |
| 123444 | 2 | 1124   |
| 6      | 2 | 6      |
| 12     | 3 | 1      |
| 89     | 3 |        |

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Grouping Data

- Choose the number of groups
  - between 5 and 10 is best
- Interval Width = (Range+1)/(Number of Groups)
  - Round **up** to a convenient value
- Start with lowest value and create the groups.
- Example – for 5 categories  
Interval Width = (58+1)/5 = 12 (rounded up)

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Grouping Data

| Class Interval | Frequency | Relative Frequency |
|----------------|-----------|--------------------|
| 67 to 79       | 3         | 0.100 or 10.0%     |
| 79 to 91       | 5         | 0.167 or 16.7%     |
| 91 to 103      | 8         | 0.266 or 26.6%     |
| 103 to 115     | 9         | 0.300 or 30.0%     |
| 115 to 127     | 5         | 0.167 or 16.7%     |
| Total          | 30        | 1.000 or 100%      |

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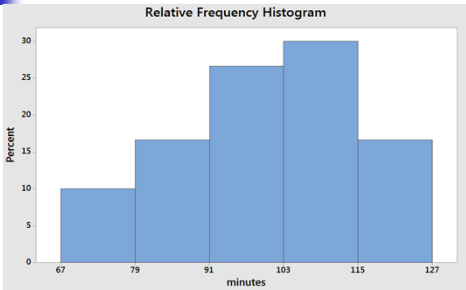
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Histogram – Relative Frequency



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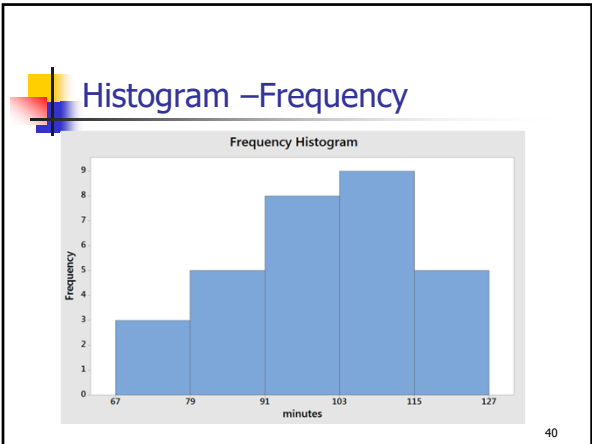
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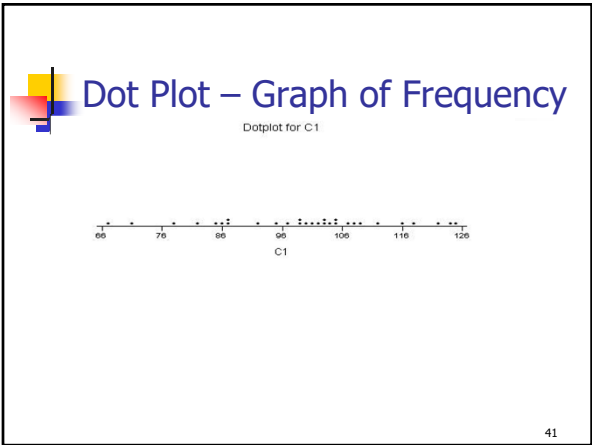
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Cumulative Relative Frequency

| Class Interval | Frequency | Relative Frequency | Cumulative Frequency | Cumulative Relative Frequency |
|----------------|-----------|--------------------|----------------------|-------------------------------|
| 67 to 79       | 3         | 0.100 or 10.0%     | 3                    | 0.100 or 10.0%                |
| 79 to 91       | 5         | 0.167 or 16.7%     | 8                    | 0.267 or 26.7%                |
| 91 to 103      | 8         | 0.266 or 26.6%     | 16                   | 0.533 or 53.3%                |
| 103 to 115     | 9         | 0.300 or 30.0%     | 25                   | 0.833 or 83.3%                |
| 115 to 127     | 5         | 0.167 or 16.7%     | 30                   | 1.000 or 100%                 |
| Total          | 30        | 1.000 or 100%      |                      |                               |

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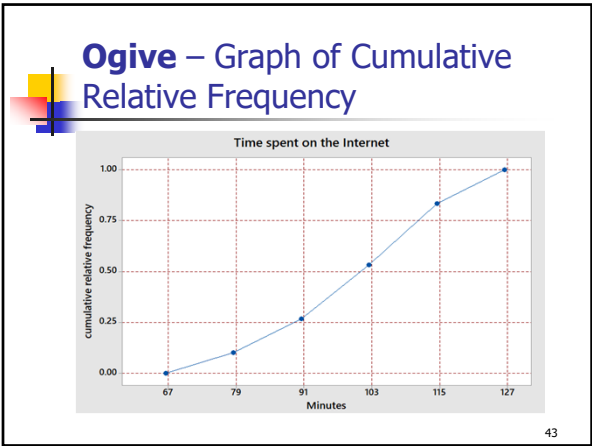
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