## Math 10 - Homework 4 MPS

- High Fructose Corn Syrup (HFCS) is a sweetener in food products that is linked to obesity and type II diabetes. The mean annual consumption in the United States in 2008 of HFCS was 60 lbs with a standard deviation of 20 lbs. Assume the population follows a Normal Distribution.
  - a. Find the probability a randomly selected American consumes more than 50 lbs of HFCS per year. P(X>50) = P(Z>(50-60)/20)=P(Z>-0.50)=1-.3085=.6915
  - b. Find the probability a randomly selected American consumes between 30 and 90 lbs of HFCS per year. P(30<X<90) = P((30-60)/20)<Z<(90-60)/20)=P(-1.50<Z<1.50)=.9332-.0668=.8664
  - c. Find the 80<sup>th</sup> percentile of annual consumption of HFCS.  $Z_{80}$ =0.84  $X_{80}$ =60+(0.84)(20)=76.8 lbs. per year
  - d. In a sample of 40 Americans how many would you expect consume more than 50 pounds of HFCS per year.
    P(X>50) = .6915 from part A. Expected Value = 40(.6915) = 27.7 or about 28 out of 40.
  - e. Between what two numbers would you expect to contain 95% of Americans HFCS annual consumption? (60-1.96(20), 60+1.96(20)) or 20.8 to 99.2 lbs. per year
  - Find the quartiles and Interquartile range for this population.
    Z<sub>25</sub>=-0.67 Z<sub>50</sub>=0 Z<sub>75</sub>=0.67 X<sub>25</sub>=60-(0.67)(20)=46.6 lbs X<sub>50</sub>=60 lbs X<sub>75</sub>=60+(0.67)(20)=73.4 lbs IQR=73.4-46.6= 26.8 lbs per year
  - g. A teenager who loves soda consumes 105 lbs of HFCS per year. Is this result unusual? Use probability to justify your answer.
    P(X>105) = P(Z>(105-60)/20)=P(Z>2.25)=1-.9878=.0122 Unusual result
  - In a sample of 16 Americans, what is the probability that the sample mean will exceed 57 pounds of HFCS per year?
    P(XBAR>57) = P(Z>(57-60)/(20/sqrt(16))=P(Z>-0.60)=1-.2743 = .7257
  - i. In a sample of 16 Americans, what is the probability that the sample mean will be between 50 and 70 pounds of HFCS per year.
    P(50<XBAR<70) = P((50-60)/(20/sqrt(16))<Z<(70-60)/(20/sqrt(16)) = P(-2.00<Z<2.00) = 0.9772 0.0228 = 0.9544</li>
  - j. In a sample of 16 Americans, between what two values would you expect to see 95% of the sample means?
    60 1.96\*20/sqrt(16) , 60 + 1.96\*20/sqrt(16)
    Between 50.2 and 69.8 lbs

- 2. A normally distributed population of package weights has a mean of 63.5 g and a standard deviation of 12.2 g.
  - a. What percentage of this population weighs 66 g or more? P(X>66) = P(Z>(66-63.5)/12.2)=P(Z>0.20)=1-.5793=.4207
  - b. What percentage of this population weighs 41 g or less?
    P(X<41) = P(Z<(41-63.5)/12.2)=P(Z<-1.84)=.0329</li>
  - c. What percentage of this population weighs between 41 g and 66 g?
    P(41<X<66) = P((41-63.5)/12.2)<Z<(66-63.5)/12.2)=P(-1.84<Z<0.20)=.5793-.0329=.5464</li>
  - d. Find the  $60^{th}$  percentile for distribution of weights. Z<sub>60</sub>=0.25 X<sub>60</sub>=63.5+(0.25)(12.2)=66.55 g
  - e. Find the three quartiles and the interquartile range.  $Z_{25}$ =-0.67  $Z_{50}$ =0  $Z_{75}$ =0.67  $X_{25}$ =63.5-(0.67)(12.2)=55.3g  $X_{50}$ =63.5  $X_{75}$ =63.5+(0.67)(12.2)=71.7g IQR=71.7-55.3=16.4 g
  - f. If you sample 49 packages, find the probability the sample mean is over 66 g. Compare this answer to part a. P(Xbar>66) = P(Z>(66-63.5)/[12.2/sqrt(16)]=P(Z>0.82)=1-.7939=.2061 lower since sdev is lower.
  - g. If you sample 49 packages, find the probability the sample mean is over 66 g. Compare this answer to part a. P(Xbar>66) = P(Z>(66-63.5)/[12.2/sqrt(49)]=P(Z>1.43)=1-.9236=.0764 lower since sdev is lower.
- A pollster sampled 100 adults in California and asked a series of questions. The Central Limit Theorem for Proportions requires that np > 10 and n(1-p) > 10. Determine if these conditions are met for the following statements.
  - a. 61% of Californians live in Southern California. np=61, n(1-p)=39 – both more than 10 - yes
  - b. 92% of Californians support Deferred Action for Childhood Arrivals (DACA) np=92, n(1-p)=8 – n(1-p) less than 10 - no
  - c. 8% of Californians have a felony conviction.
    np=8, n(1-p)=92 np less than 10 no
- 4. 24% of Californians have visited Yosemite National Park. A pollster samples 1000 Californians.
  - a. Determine the expected value and standard deviation of the sample proportion.
    Mean = p = 0.24 std dev = sqrt(0.24(1-0.24)/1000) = 0.0135
  - b. Determine that the condition for normality is satisfied. np=240, n(1-p)=760 – both more than 10 - yes
  - c. Determine the probability the sample proportion exceeds 0.40.
    P(p-hat>0.40) = P(Z>(0.40 0.24)/0.0135) = P(Z>11.85) = 0