



M	lathematic	al Model -	Table
-	X=marketing	Y=revenue	
	\$0	\$1000	
	\$500	\$2000	
	\$1000	\$3000	
	\$1500	\$4000	
	\$2000	\$5000	
			3















	Statistical Model - Table									
_	X=Marketing	Expected Revenue	Y=Actual Revenue	ε=Residual Error						
	\$0	\$1000	\$1100	+\$100						
	\$500	\$2000	\$1500	-\$500						
	\$1000	\$3000	\$3500	+\$500						
	\$1500	\$4000	\$3900	-\$100						
	\$2000	\$5000	\$4900	-\$100						























Assumptions Underlying Linear Regression

- For each value of X, there is a group of Y values, and these Y values are *normally distributed*.
- The *means* of these normal distributions of Y values all lie on the straight line of regression.
- The *standard deviations* of these normal distributions are equal.
- The Y values are statistically independent. This means that in the selection of a sample, the Y values chosen for a particular X value do not depend on the Y values for any other X values.

16

16



17



Exa	imple	cont	tinuea	/	
	Х	Y	X ²	Y ²	XY
	10	40	100	1600	400
	15	35	225	1225	525
	20	25	400	625	500
	30	25	900	625	750
	40	15	1600	225	600
Σ	115	140	3225	4300	2775











Example co	nti	inu	ed		
 Find SSE and the 					
	х	у	ŷ	y - ŷ	$(y - \hat{y})^2$
SSR = 341.422	10	40	37.97	2.03	4.104
SSE = 38.578	15	35	34.14	0.86	0.743
	20	25	30.30	-5.30	28.108
	30	25	22.63	2.37	5.620
	40	15	14.96	0.04	0.002
				Total	38.578
					23
					25







26



Example <i>continued</i>						
• Test the Hypothesis $H_0: \beta_1 = 0, \alpha = 5\%$						
Source	SS	df	MS	F	p-value	
Regression	341.422	1	341.422	26.551	0.0142	
Error	38.578	3	12.859			
TOTAL	380.000	4				
Reject Ho p-value < α						



Example <i>co</i>	nti	nu	ed		
Find SSE and the					
standard error:	х	у	ŷ	y - ŷ	$(y - \hat{y})^2$
	10	40	37.97	2.03	4.104
SSR = 341.422	15	35	34.14	0.86	0.743
SSE = 38.578	20	25	30.30	-5.30	28.108
MSE = 12.859	30	25	22.63	2.37	5.620
■ s _e = 3.586	40	15	14.96	0.04	0.002
				Total	38.578
					30

















0 1 2 3 4 5 6 7 5 X 36













- E	Xamp x 10 15 20 30 40	Die cor Y 40 35 25 25 15	x ² 100 225 400 900 1600	Y ² 1600 1225 625 625 225	XY 400 525 500 750 600		
	115	140	3225	4300	2775		
• SSX = $3225 - 115^2/5$ = 580 • SSY = $4300 - 140^2/5$ = 380 • SSYY = $2775 - (115)(140)/5 = -445$							
			5,2.0,0	. 15		40	





































Using Minitab to Run Regression Data shown is engine size in cubic inches (X) and MPG (Y) for 20 cars. **x x у y** 25







Usir Selec choos variat	ng Minitab to Run Regressio t Statistics>Regression>Regression, then se the Response (Y-variable) and model (X- ble)	n
	Regression	
	C2 Sales C4 EngineSize C5 mpg	
	w .	
	Graphs Options	
	Select Results Storage	
	Help OK Cancel	
		55

Using Minitab to Run Regression
Click the results box, and choose the fits and residuals to get all predictions.
Regression - Results
Control the Dipolary of Results C Deplay nothing Resplay nothing Resplay nothing Resplay of example C In addition, page.enthil arms of focusers and the unusual C In addition, page.enthil arms of focus of sales of sales C In addition, page.enthil arms of focus of focus of the International Additional Additi
C In addition, the full table of fits and residuals Help OK Cancel
56
56

 Using Minitab to Run Regression

 quation, the intercept and slope, the standard error of the residuals, and the r²

 The regression equation is mg = 30.2 - 0.0466 EngineSize

 Predictor
 Coef SE Coef T P Constant 30.0203 1.361 22.20 0.000 EngineSize -0.046598 0.005378 -8.66 0.0000

 S = 2.95688
 R-Sq = 80.7%
 R-Sq(adj) = 79.6%

Using M	lini	itab t	o Rui	n Re	gress	ion
Next is the A significance Analysis of Var	ANO of th	VA table, ne regres	, which t ssion mo	ests the del.	2	
Source	DF	SS	MS	F	Р	
Regression	1	656.42	656.42	75.08	0.000	
Residual Error	18	157.38	8.74			
Total	19	813.80				
						58

U _	sir	ng Mi	nita	ıb to	o Ri	un R	egres	sion
Fii	nall	y, the re	sidual	s shov	v the	potentia	al outliers	5.
	Obs	EngineSize	mpg	Fit	SE Fit	Residual	St. Resid	
	1	400	15.000	11.564	1,167	3,436	1.26	
	2	455	14.000	9,001	1,421	4,999	1,93	
	3	113	24.000	24.937	0.880	-0.937	-0.33	
	4	198	22.000	20.976	0.673	1.024	0.36	
	5	199	18.000	20.930	0.672	-2.930	-1.02	
	6	200	21.000	20.883	0.671	0.117	0.04	
	7	97	27.000	25.683	0.939	1.317	0.47	
	8	97	26.000	25.683	0.939	0.317	0.11	
	9	110	25.000	25.077	0.891	-0.077	-0.03	
	10	107	24.000	25.217	0.902	-1.217	-0.43	
	11	104	25.000	25.357	0.913	-0.357	-0.13	
	12	121	26.000	24.565	0.853	1.435	0.51	
	13	199	21.000	20.930	0.672	0.070	0.02	
	14	360	10.000	13.427	0.998	-3.427	-1.23	
	15	307	10.000	15.897	0.807	-5.897	-2.07R	
	16	318	11.000	15.385	0.842	-4.385	-1.55	
	17	400	9.000	11.564	1.167	-2.564	-0.94	
	18	97	27.000	25.683	0.939	1.317	0.47	
	19	140	28.000	23.679	0.792	4.321	1.52	
	20	400	15.000	11.564	1.167	3.436	1.26	59

