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1. (25 points) Consider the circuit in the diagram: two real batteries (of equal Emf, but call them $\operatorname{Emf}_{1}$ and $\operatorname{Emf}_{2}$ for identification purposes) are connected in parallel across a single load resistance $\mathrm{R}_{\mathrm{L}}$. But even though their emf's are the same, their internal resistances are not the same and are $r_{1}$ and $r_{2}$. So in this case the current delivered by each battery is not the same. Find the ratio of the current delivered by $\operatorname{Emf}_{1}, I_{1}$ to the total current delivered to $\mathbf{R}_{\mathrm{L}}$, that is, find $\mathbf{I}_{\mathbf{1}} / \mathbf{I}_{\text {total }}$. Your final answer will be in terms of the two internal resistances only. At the end of the problem, let $\quad r_{2}=2 r_{1}$ and find the final answer as a purely numerical
 fraction. This problem does not have to be algebraically difficult.
2. ( 25 points) Consider the coordinate system shown in the diagram. Two infinite straight lines of current, $\mathrm{I}_{1}$ and $\mathrm{I}_{2}$ are arranged as shown. $\mathrm{I}_{1}$ is on the y axis in the negative direction and $\mathrm{I}_{2}$ is parallel to the z axis a distance L away from it in the positive direction. There is also a uniform electric field present everywhere given as $\mathbf{E}=\mathrm{E}_{0} \mathbf{k}$. A charge, +q , at the shown position has a velocity at that instant of: $\mathbf{V}=$ $-V_{z} k$. Find the Lorentz force on this charge at that time. Your final answer will be in terms of unit vectors. A quick and dirty Ampere's Law is ok here, but fans of the polar form evaluation of the cross product will not find this so easy. In case you're wondering, this is not a "change of frame of reference" problem.

3. ( 25 points) Consider the arrangement shown in the diagram. An infinite straight line of current, $\mathrm{I}_{1}$ creates a magnetic field everywhere. A straight line current "segment" of length L (don't worry about how it completes a circuit here) exists as shown, with a current through it of $\mathrm{I}_{\mathrm{S}}$, to the right, where it is hinged and free to rotate about an axis (out of the paper) through the fixed point as indicated in the diagram. Find the magnitude of the torque from the infinite straight line of current on the segment about the hinge point. Ampere's Law, quick and dirty, is okay. Your final answer can be as an integral completely ready to integrate with limits.

4. (25 points) Referring to the diagram, using the Biot-Savart Law, find the magnetic field magnitude along the $y$ axis, $B(y)$, due to the spinning disk of charge. Note there is only charge present from R/2 to $R$ and consider the charge density constant and given as $\sigma$ (so it would be in your final answer). Say that the disk is spinning with a given angular velocity of $\omega$. Hint: the Biot-Savart Law gives dB in terms of IdL, but in this problem think of dB in terms $\mathrm{LdI}(\mathrm{dI}=\mathrm{dq} / \mathrm{T})$, and L is the circumference of an arbitrary ring of charge. You can make this substitution at the appropriate time. Your final answer is an integral ready to integrate with limits.

